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Pedotransfer Functions for Field Capacity, Permanent Wilting Point, and Available Water Capacity Based on Random Forest Models for Routine Soil Health Analysis

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ABSTRACT

Available water capacity (AWC), field capacity (θ_{FC}), and permanent wilting point (θ_{PWP}) are regarded as key physical soil health indicators that directly capture the soil's capacity to store plant available water but are expensive components of a comprehensive soil health analysis. To reduce costs, pedotransfer functions for θ_{FC}, θ_{PWP}, and AWC were developed from a dataset of 7,232 soil samples with texture, soil organic matter (SOM), permanganate-oxidizable carbon, soil respiration, AWC, θ_{FC}, θ_{PWP}, wet aggregate stability, and extractable potassium, magnesium, iron, and manganese. Three functions were developed for each property: a full random forest (RF) model containing all variables, a reduced RF model and a multiple linear regression model containing texture and SOM. Pedotransfer functions were validated with an independent dataset that contained 1,406 samples. The full RF models for θ_{FC}, θ_{PWP}, and AWC reduced the root mean square error (RMSE) by 16.3, 13.3, and 12.8%, compared to multiple linear regression models, respectively. Furthermore, the full RF models for θ_{FC}, θ_{PWP}, and AWC reduced RMSE by 11.6, 6.7, and 12.8%, compared to the reduced RF model, respectively. Permanganate-oxidizable carbon, wet aggregate stability, and extractable magnesium, potassium, and iron were useful novel predictor variables for improving prediction of θ_{FC} and AWC. AWC was sensitive in 20/57 long-term experiments, and full RF models were able to replicate 5/20 of those significant results. New RF pedotransfer functions for θ_{FC}, θ_{PWP}, and AWC can enhance prediction compared to traditional modeling techniques, fits into existing interpretative frameworks, and improves cost-effectiveness of comprehensive assessments of soil health.

Introduction

Available water capacity (AWC), a measure of the amount of plant available water a soil can hold, is regarded as a key physical soil health indicator that is sensitive to inherent and dynamic soil properties. It is calculated as the difference between the water held at field capacity (θ_{FC}) and the water held at the permanent wilting point (θ_{PWP}; Reynolds and Topp 2008a). Therefore, AWC is a physical soil health measurement that provides the only direct indicator of water supply capacity to plant roots, which can be a yield limiting factor during prolonged dry weather conditions (Kukal et al. 2023).

AWC is included in several soil health assessment frameworks: Soil Management Assessment Framework (SMAF; Andrews, Karlen, and Cambardella 2004), Comprehensive Assessment of Soil Health (CASH; Moebius-Clune et al. 2017), and Open Soil Index (OSI; Ros et al. 2022). The

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Cornell Soil Health Laboratory has included AWC measured on repacked samples as the difference in gravimetric soil water content between −10 kPa (θ_{FC}) and −1500 kPa (θ_{PWP}) water potentials since 2006 (Idowu et al. 2009). The decision to measure AWC on repacked soil samples rather than on in-tact cores was necessary to facilitate sample collection (from disturbed soil similar to traditional soil sampling) and increase sample throughput rate in a commercial soil health laboratory. Nevertheless, of the commonly measured soil health indicators, AWC and its components θ_{FC} and θ_{PWP}, are the most time-consuming and expensive to measure, which makes them poor candidates for measurement by high throughput soil health laboratories. Alternatively, laboratories may predict these water retention parameters using machine learning algorithms based on a suite of other (more inexpensively measured) properties in standard soil health packages including sand, silt, clay, wet aggregate stability (WAS), soil organic matter (SOM), permanganate oxidizable carbon (POXC), soil respiration (Resp), and extractable potassium (K), magnesium (Mg), iron (Fe), and manganese (Mn; Amsili, Van Es, and Schindelbeck 2022).

Soil scientists have a long history of developing predictive models to estimate soil physical properties that are costly, time intensive, and difficult to measure from properties that are easier to measure (Kinoshita et al. 2012; Van Looy et al. 2017). Predictive models that relate properties that are easy to measure or access to those that are more difficult to measure are known in soil science as pedotransfer functions. They have been developed to estimate soil physical properties such as bulk density, saturated hydraulic conductivity (Ksat), and moisture retention characteristics, among others (Kinoshita et al. 2012; Ramcharan et al. 2017; Saxton and Rawls 2006; Zhang and Schaap 2019). Input variables for these pedotransfer functions often include soil particle size distribution (percent sand, silt, clay, and derived properties: mean or median particle diameter), SOM or soil organic carbon (SOC), diffuse reflectance spectroscopy (i.e. visible and near-infrared or mid-infrared), soil horizonation, qualitative soil structure categories, bulk density, and can also include non-soil covariates such as region, land cover, and climate variables that can be extracted from existing maps (Navidi, Seyedmohammadi, and Seyed Jalali 2022; Ramcharan et al. 2017; Sanderman, Savage, and Dangal 2020; Van Looy et al. 2017).

Some of the earliest pedotransfer functions were developed in the early 1900s to relate soil moisture retention characteristics to soil texture (Van Looy et al. 2017). Therefore, it has been known for a long time that soil moisture retention properties such as θ_{FC} and θ_{PWP} can be estimated using soil particle size distribution information (percent sand, silt, clay, and mean or median particle diameter), which are widely recognized as the most important predictor variables for moisture retention characteristics (Saxton and Rawls 2006; Wösten, Pachepsky, and Rawls 2001). By the latter half of the century, pedotransfer functions for soil moisture retention at θ_{FC} and θ_{PWP} began including SOM, bulk density, and carbonates in addition to particle size fractions (Gupta and Larson 1979; Rawls et al. 2003). Kinoshita et al. (2012) found improved prediction of water retention parameters by combining soil texture analysis with proxy estimates from visible and near-infrared reflectance spectroscopy. Early pedotransfer functions generally used linear regression techniques or were as simple as look up tables to relate soil texture class to mean hydrologic property (e.g., Ksat; Van Looy et al. 2017; Wösten, Pachepsky, and Rawls 2001). Commonly used linear regression-based pedotransfer functions for estimating moisture retention at θ_{FC} and θ_{PWP} include those by Rawls, Brakensiek, and Saxton (1982), Saxton and Rawls (2006), and more recently by Tóth et al. (2015) and Bagnall et al. (2022). Linear regression and look up tables have the advantage of being parsimonious, easy to interpret and implement, but nonlinear regression and machine learning techniques may provide greater predictive power (Bagnall et al. 2022; Padarian, Minasny, and Mcbratney 2020; Van Looy et al. 2017; Wösten, Pachepsky, and Rawls 2001). Beginning in the 1990s, researchers began to explore non-linear regression and machine learning techniques to predict θ_{FC} and θ_{PWP}. Two commonly cited pedotransfer functions include Schaap, Leij, and Van Genuchten (2001; Zhang and Schaap 2017; ROSETTA) based

on neural network algorithm and Nemes, Rawls, and Pachepsky (2006; 2008; kNearest Neighbor) based on k-nearest neighbors. These early machine learning models required software development to enable their use, but now machine learning models are easier to implement.

The use of machine learning algorithms such as random forest (RF) in soil science has grown exponentially in the last 20 years (Padarian, Minasny, and Mcbratney 2020). This rise is due to the increased adoption of open-source, rapidly evolving, and accessible coding languages like R and Python by the academic community (Robinson 2017). Furthermore, the growth of machine learning approaches is due to consistent evidence that they generally provide greater predictive power than traditional approaches like multiple linear regression (Padarian, Minasny, and Mcbratney 2020). Machine learning enables researchers to capture non-linear effects and to effectively utilize a larger number of predictor variables than linear regression (Wösten, Pachepsky, and Rawls 2001). Commonly used machine learning techniques in soil science to develop pedotransfer functions include neural networks, support vector machines, k-nearest neighbors, multivariate adaptive regression spline, regression trees, random forest, boosted regression trees (e.g., extreme gradient boosting), cubist regression, and deep learning (Navidi, Seyedmohammadi, and Seyed Jalali 2022; Padarian, Minasny, and Mcbratney 2020; Rubio et al. 2024; Van Looy et al. 2017). Scientists have used machine learning algorithms to predict bulk density, soil moisture retention parameters, root zone soil moisture, Ksat, aggregate stability (Araya and Ghezzehei 2019; Carranza et al. 2021; Navidi, Seyedmohammadi, and Seyed Jalali 2022; Nemes et al. 2008; Ramcharan et al. 2017; Rivera and Bonilla 2020; Shiri et al. 2017).

This study focuses on developing pedotransfer functions in the context of comprehensive soil health assessment where a range of other physical, biological, and chemical indicators are routinely measured. The objectives of this research were to (i) develop pedotransfer functions for the prediction of θ_{FC}, θ_{PWP}, and AWC for comprehensive soil health assessment, (ii) extract variable importance insights from pedotransfer functions with a goal of determining if novel predictor variables improve the prediction of θ_{FC}, θ_{PWP}, and AWC, (iii) validate pedotransfer functions using an independent dataset, (iv) assess ability of models to be sensitive to management.

Materials and methods

Training dataset

A soil health dataset was compiled from 7,232 soil samples (0–15 cm depth) from across the continental U.S. that were collected and analyzed between 2015 and 2019 (Figure 1; Table S1). The dataset was derived from routine soil sample submission to the Cornell Soil Health Laboratory. While all regions of the continental U.S. were represented in the Training Dataset, most samples derived from the Midwest, Northeast, Mid-Atlantic, and Northern Plain regions (Figure 1; Table S1; Figure S1). Soil samples were, per guidelines, assumed to have been collected by composing five or more soil slices (0-to-15 cm depth) from different locations in a field or plot (Cornell Soil Health Laboratory 2022). Samples were analyzed for soil texture and a suite of physical, biological, and chemical soil health indicators according to the CASH protocol (Moebius-Clune et al. 2017). Therefore, all samples contained measurements for the following co-variate properties that were used in this analysis: sand, silt, clay, wet aggregate stability (WAS), SOM, permanganate oxidizable carbon (POXC), soil respiration (Resp), and Modified Morgan extractable K, Mg, Fe, and Mn. Previous AWC RF model development determined that pH, P, and Zn added little predictability to the model and therefore were not included as predictor variables (Amsili, Van Es, and Schindelbeck 2022). Additionally, field capacity (θ_{FC}) and permanent wilting point (θ_{PWP}), which are not reported in CASH, but are used to calculate AWC, were aggregated with this dataset. Soils with SOM values greater than 10.0% were removed from the dataset to develop models that are appropriate for mineral agricultural soils. All soil analysis procedures are described in Schindelbeck et al. (2022).

Figure 1. Distribution of soil samples by state across the continental U.S. within the training dataset for field capacity, permanent wilting point, and available water capacity pedotransfer functions. Soil samples from NAPESHM study sites within the U.S. were used as the validation dataset to test models.

Analysis of physical properties

Soil texture was measured using a rapid and quantitative texture method that uses 3% sodium hexametaphosphate and shaking to disperse soil particles. Then, samples are sieved through 53 μm and allowed to sediment for two hours to determine the percentage of sand, silt, and clay (Kettler, Doran, and Gilbert 2001). WAS was measured by shaking soil samples for 10 s on a mechanical shaker with stacked sieves of 2.0 and 0.25 mm to collect macroaggregates between 0.25-to-2.0 mm. A single layer of macroaggregates was spread on a 0.25 mm mesh sieve and received 1.25 cm of water and 2.5 J of energy over a 5-min period. WAS was determined as the fraction of stable soil that remains above the sieve, correcting for particles >0.25 mm. θ_{FC} and θ_{PWP} were measured by placing approximately 15 g of air dried-2 mm-sieved soil into rubber rings on 1 and 15 bar porous ceramic pressure plates, respectively, and allowing soils to completely saturate (Soil Moisture Equipment Corp., Goleta, CA). Then pressure plates were placed in pressure chambers and equilibrated to −10 kPA (θ_{FC}) and −1500 kPA (θ_{PWP}). Field capacity water content was chosen to be at −10 kPa instead of the more commonly used −33 kPa because (i) most soils under consideration have limited depth to restricting layers or water tables (Fan, Li, and Miguez-Macho 2013; Reynolds and Topp 2008a), and (ii) plant water availability is most critical during growing seasons when water uptake is immediate after soil recharge (rather than after a 2–3 day drainage period). Field capacity is also defined as −10 kPa in Australia, New Zealand, Sweden, and by Ward Labs in the US (Nemes, Pachepsky, and Timlin 2011; Robertson et al. 2021; Ward 2021). AWC was calculated as the difference in gravimetric water content between θ_{FC} and θ_{PWP} (Reynolds and Topp 2008b).

Analysis of biological properties

SOM was analyzed by mass loss on ignition (LOI) in a muffle furnace at 500°C for two hours. Then % LOI was converted to % SOM using Equation 1 from Storer (1984), which is the standard method for calculating % SOM in New York State.

$$\%SOM = (\%LOI \times 0.7) - 0.23 \tag{1}$$

POXC was measured in duplicate, by reacting 2.5 g of soil with 20 mL 0.02 M potassium permanganate ($KMnO_4$) x 0.1 M calcium chloride ($CaCl_2$) solution (pH 7.2). Extracts were shaken for 2 minutes at 120 rpm and then allowed to settle for exactly 8 minutes. An aliquot of solution was diluted 100-fold and absorbance readings were taken at 550 nm using a handheld spectrophotometer (Hach, Loveland, CO). Absorbance was converted to mg POXC per kg soil using the equation of Weil et al. (2003) and a standard curve. Resp was analyzed by measuring cumulative CO_2 production over a four-day incubation with an alkali trap on 20.0 g air dried-8 mm sieved soil sample. The amount of CO_2 produced and absorbed by the KOH trap over the course of incubation was determined by measuring the change in electrical conductivity of the solution with an OrionTM DuraProbeTM 4-Electrode Conductivity Cell (ThermoFisher Scientific, Inc., Waltham, MA). Blanks without soil were also incubated to subtract CO_2 from the air that reacted with the alkali trap (Nunes et al. 2018).

Analysis of chemical properties

Nutrients were measured by extracting soil with a Modified Morgan solution (ammonium acetate plus acetic acid, pH 4.8) and then extracts were analyzed using inductively coupled plasma optical emission spectrometry (SPECTRO Analytical Instruments Inc., Mahwah, NJ) (Wolf and Beegle 1995). All nutrient contents are reported in units of mg kg^{-1} soil (ppm).

Validation dataset

The North American Project to Evaluate Soil Health Measurements (NAPESHM; Norris et al. 2020) data were used as an independent validation dataset to test the accuracy of developed pedotransfer functions for θ_{FC}, θ_{PWP}, and AWC. The NAPESHM validation dataset contained 1,406 composite soil samples that were collected within the US, from 0 to 15 cm depth, in 2019 (Figure 1; Table S2). The project, conducted by the Soil Health Institute (Cary, NC), sampled 90 long-term (>10 years) experiments that were testing treatments from various agronomic management practices, including tillage, nutrient management, cover crops, crop diversity, water management, or multiple stacked practices (Norris et al. 2020; Figure 1). Samples were submitted to the Cornell Soil Health Laboratory for the analysis of all soil properties using the same methods in the training dataset: sand, silt, clay, θ_{FC}, θ_{PWP}, AWC, WAS, SOM, POXC, Resp, and Modified Morgan K, Mg, Fe, and Mn (Norris et al. 2020). The Training and NAPESHM datasets had similar distributions of sand, silt, and clay. However, the Training dataset had a slightly higher mean SOM value and a larger proportion of samples with SOM values between 4 and 8% than the NAPESHM dataset (Figure S2). The NAPESHM Validation Dataset provides a completely independent dataset to validate pedotransfer functions developed with the Training Dataset.

The NAPESHM dataset was also used to determine if model predictions could be equally sensitive to management as the measured values. We selected 57 experiments with at least 12 experimental plots, which included 1,178 observations, and assessed the sensitivity of measured gravimetric AWC to management. Treatments depended on the experiment but included at least one of the following treatment factors: tillage, cover crop, nutrient type, nutrient rate, cropping category (i.e., row crop, perennial, etc.), residue removal, crop rotation, and landscape position. In experiments where treatments had a significant effect on gravimetric AWC, we investigated whether modeled predictions could replicate those results. Gravimetric AWC model predictions included direct RF model predictions of AWC or calculation of AWC through separate RF prediction of θ_{FC} and θ_{PWP}.

Modeling approaches

Multiple linear regression

Multiple linear regression (MLR) models for θ_{FC}, θ_{PWP}, and AWC were fit to the Training dataset using sand, clay, and SOM, which are the most widely used to develop MLR pedotransfer functions for θ_{FC} and θ_{PWP} (Bagnall et al. 2022; Saxton and Rawls 2006). For θ_{FC} and AWC, MLR models included

coefficients for sand, clay, SOM, sandxclay, sandxSOM, and clayxSOM. Whereas θ_{PWP} MLR models only included coefficients for sand, clay, and SOM. MLR models were fit using the lm function in R (R Core Team 2022), and nonsignificant coefficients were underlined in MLR Equations.

Random forest machine learning algorithm

Random forest is a robust non-linear machine learning algorithm that combines predictions of many decision trees (a forest) to model variables. Each decision tree is made with a bootstrap sample (random sampling with replacement) of approximately 63.2% of the Training Dataset. In each tree, a random subsample of all predictor variables, p, is tested as the splitting variable that will minimize error at various nodes in the tree (Breiman 2001; Liaw and Wiener 2002). The out-of-bag (OOB) samples, or the 36.8% that are omitted from building the decision tree, are predicted on that decision tree. RF predictions take the average of predictions of each decision tree in the forest. Aggregated OOB predictions are used to test and validate the predictions from the RF model (Liaw and Wiener 2002). Unlike MLR, RF allows for many predictor variables to be used without the effects of less important predictor variables being masked by more important predictor variables. Additionally, RF can capture non-linear or local importance of predictor variables. RF models were run using the randomForest package in R, which implements Breiman's random forest algorithm (Breiman 2001; Liaw and Weiner 2022). Seed was arbitrarily set at 500 using the set.seed function in R to make the RF models reproducible. Previous work determined that changing the set.seed parameter leads to insignificant changes to the RF models. An exercise with one Full RF model in this study showed that changing the set.seed parameter led to insignificant increases of only 0.26%, 0.29%, and 0.80% from the min to max values of percent variance explained, OOB RMSE, and RMSE, respectively. The parameters for each RF model were: 500 trees, randomForest defaults (mtry = p/3, rounded down; target node size = 5), proximity = TRUE, localImp = TRUE.

Full and Reduced RF models were developed for θ_{FC}, θ_{PWP}, and AWC. The Full RF models used all available predictor variables, which included sand, silt, clay, WAS, SOM, POXC, Resp, and Modified Morgan K, Mg, Fe, and Mn. Whereas the Reduced RF models used sand, silt, clay, and SOM. Full and Reduced RF models were compared to determine how novel variables contribute to the prediction of θ_{FC}, θ_{PWP}, and AWC.

Pedotransfer function validation

Initial validation of pedotransfer functions was done with the Training Dataset by plotting predictions against measured values. For the RF models, percent of variance (%Var) explained and OOB root mean square error (RMSE) and OOB normalized RMSE (NRMSE) were calculated. %Var explained is a metric provided with RF models in R and can be described as how well the OOB predictions match the observed values (Equation 2). Therefore, it is a pseudo-R-squared metric defined by:

$$\%Var\,Explained = \left(1 - \frac{MSE\ of\ OOB\ predictions\colon \frac{1}{n}\sum_{i=1}^{n}\left(Y_i - \hat{Y}_i\right)^2}{Variance\ of\ observed\ values\colon \frac{\sum (x_i - \bar{x})^2}{n-1}}\right) \times 100 \qquad (2)$$

Out of bag (OOB) RMSE was calculated by comparing OOB model predictions to measured values:

$$RMSE = \sqrt{\frac{1}{n}\sum_{i=1}^{n}\left(Y_i - \hat{Y}_i\right)^2} \qquad (3)$$

The OOB NRMSE was calculated by dividing the OOB RMSE by the average of the measured values:

$$NRMSE = \frac{\sqrt{\frac{1}{n}\sum_{i=1}^{n}\left(Y_i - \hat{Y}_i\right)^2}}{\overline{Y}_i} \qquad (4)$$

For MLR models, adjusted R^2, RMSE (Equation 3), and NRMSE (Equation 4) were calculated.

A secondary validation step was carried out with the NAPESHM data. Regression equations, mean absolute error (MAE; Equation 5), RMSE, and NRMSE were all used as validation metrics in the secondary validation step:

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |Y_i - \hat{Y}_i| \tag{5}$$

Variable importance and partial dependence of RF models

RF models containing 100s of decision trees are more difficult to interpret (black-box) than a single decision tree, which can be easily visualized, or a MLR model with explicit coefficients. Several powerful tools have been developed to interpret RF models and variable importance. The randomForestExplainer package in R enables the calculation and visualization of the mean minimal depth (min_depth_distribution function), or the average location of predictor variables across all decision trees, where 0 is the root node of the tree, 1 is the 2nd layer, etc (Palusynska, Biecek, and Jiang 2022). It also extracts variable importance metrics from the RF model, including MSE increase, which ranks variables by their ability to reduce mean square error of the prediction (i.e., higher MSE increase values are associated with more predictive variables), and node purity increase, how much each variable improves the purity of different parts of the tree (Palusynska, Biecek, and Jiang 2022). Additionally, Shapley Additive exPlanations (SHAP) values were calculated and visualized using the kernalshap and shapviz packages in R, respectively (Mayer and Stando 2023; Mayer, Watson, and Prezemyslaw 2023). SHAP is a popular technique for interpreting machine learning models due to its flexibility (i.e., can be used on any machine learning model, which is useful for model comparison) and ability to predict individual predictions (Molnar 2023). SHAP values calculate variable importance by comparing model predictions with and without the variable of interest (Tseng 2018). SHAP values were calculated using the kernalshap function with 1,085 random samples from the training dataset to explain (number picked within the recommended range) and 362 random samples from the training dataset as background (number picked within the recommended range) (Mayer, Watson, and Prezemyslaw 2023). Then, two types of sv importance plots were constructed: a simple one that showed the mean absolute SHAP value, which can be interpreted as the magnitude of the effect of each variable on the predicted value; and a "beeswarm" plot, which plots each of the SHAP values of those 1,085 points and maps each predictor variable value from high to low.

Partial dependence analysis with the pdp package was used to determine the influence of single predictor variables on θ_{FC}, θ_{PWP}, and AWC in the full RF models, while other variables are held constant. The four most important predictor variables for θ_{FC}, θ_{PWP}, and AWC as indicated by the MSE increase metric were run as individual partial dependence plots. The next three most important variables (i.e., 5th – 7th) were included in the supplemental materials for θ_{FC} and AWC. The pdp package also provides functionality to plot multi-predictor partial dependence plots (Greenwell 2017) which were constructed with SOM and sand or clay to visualize interaction among those variables. Variable importance and partial dependence plots were only made for the full RF models for θ_{FC}, θ_{PWP}, and AWC.

Results and discussion

Field capacity (θ_{FC})

Model comparison and validation

Three pedotransfer functions were developed for gravimetric θ_{FC}, including a Full RF model, a Reduced RF model, and MLR (Equation 6). Units of predictor variables and θ_{FC} in Equation 6 are in g g^{-1} (i.e., g H$_2$O g^{-1} oven dry soil and g sand g^{-1} oven dry soil).

Field Capacity (θ_FC) Training Dataset

Field Capacity (θ_FC) NAPESHM Validation Dataset

Figure 2. (a-c) measured vs. predicted field capacity water content (θ_{FC}) for full random forest (RF), reduced RF, and multiple linear regression (MLR) models on the training dataset. (a-b) full and reduced RF models show out of bag predictions. Validation metrics within plots include percent variance explained, out of bag (OOB) root mean square error (RMSE), and OOB normalized RMSE (NRMSE). (d-f) measured vs. predicted field capacity for full RF, reduced RF, and MLR models for the NAPESHM validation dataset. Text within plots includes the regression equation, adjusted R^2, mean absolute error (MAE), RMSE, and NRMSE.

$$\theta_{FC} = 0.3477 - 0.313sand + 0.040clay + 1.855SOM + 0.222\,(sand \times clay) + 1.405\,(sand \times SOM) - 0.202\,(clay \times SOM)$$

$$(6)$$

The first validation step with the Training dataset revealed that the Full RF model had the highest percent variance explained (86.0%) and lowest RMSE (0.036) compared to the Reduced RF (%Var explained = 80.9%; RMSE = 0.042) and MLR models (R^2_{adj} = 0.79; RMSE = 0.043; Figure 2a–c). Furthermore, the Reduced RF model had a similar percent variance explained and RMSE to the MLR model (Figure 2b,c). The second validation step with the independent NAPESHM dataset reinforced trends among models found using the Training dataset (Figure 2d–f). It also demonstrated that each model had NRMSEs that were on average 13.9% higher (Reduced RF: 12.2%, MLR: 12.4%, and Full RF: 17.0%) than the same model calculated for the Training dataset (Figure 2). Therefore, although RF is robust against overfitting (Breiman 2001), the RF models displayed a similar amount of overfitting to the Training dataset as the MLR model. Another explanation for the deviation in performance between Training and NAPESHM Validation datasets is that the Training Dataset had proportionally fewer samples from the Southern Plain States and Northwest than the NAPESHM dataset (Tables S1 and S2). The Full RF model had a 16.3% lower RMSE than the MLR model, which indicates inclusion of additional variables beyond sand, silt, clay, and SOM can provide meaningful improvements to prediction of θ_{FC} (Figure 2d–f). In contrast, we found that the Reduced RF model performed similarly to the MLR model that contained similar predictor variables: sand, silt, clay, and SOM, indicating that

simple modeling approaches like MLR can be adequate in situations where only 3–4 predictor variables are being used. If the goal is prediction and access is available to many potential predictors of θ_{FC}, machine learning algorithms, like RF, can utilize all those variables to improve the prediction of θ_{FC}.

Variable importance

Variable importance approaches for the Full RF θ_{FC} model showed that sand was the most influential predictor variable, followed by SOM and silt, and then clay (Figures 3 and S3). By the nature of its particle diameter (53–2,000 µm), sand content is the primary determinant of the percentage of total porosity with a pore diameter equal to or smaller than 30 µm, which is the theoretical pore size that is drained at −10 kPa or θ_{FC} (Amer, Logsdon, and Davis 2009; Moebius et al. 2007). Therefore, there was a strong negative relationship between sand content and θ_{FC} (Figure 3a). Both silt and SOM were of secondary importance as predictor variables of θ_{FC}. Silt was slightly more important than SOM for improving the prediction of θ_{FC} as indicated by a larger MSE increase value (Figure S3b), but both had similar magnitude effects on θ_{FC} (Figure S3c). Clay content was the least important of the four variables as indicated by MSE increase and mean SHAP values (Figure S3). Interestingly, there was an interaction between sand content and SOM, where increases in SOM led to larger increases in θ_{FC} between 50 to 100% sand (coarser-textured) than between 0 to 25% sand (finer-textured). This corroborates similar findings that AWC responds to SOM to a larger extent in sandier soils than in silty or clayey soils (Bauer and Black 1992; Libohova et al. 2018; Minasny and Mcbratney 2018).

After sand, silt, SOM, and clay, POXC, Mg, and K were the next three most important variables for improving the prediction of θ_{FC} as indicated by MSE increase and mean SHAP metrics (Figure S3). Higher values for POXC, Mg, and to a lesser extent K were associated with higher values for θ_{FC} (Figure S4). POXC provides redundancy in the model and likely helps to capture the effects of increasing SOM content on θ_{FC}. Extractable Mg could potentially indicate soils that have calcareous mineralogy, which can influence soil water retention

Figure 3. (a-d) partial dependence plots for individual field capacity water content (θ_{FC}) predictor variables: sand, silt, clay, and soil organic matter. (e) Multi-predictor partial dependence plot with the interaction between sand and soil organic matter. These partial dependence plots show the influence of individual predictor variables on θ_{FC} within the full RF model while all other predictor variables are held constant.

(Bagnall et al. 2022). Extractable Mg and to a lesser extent K show negative correlations with sand content and positive correlations with SOM content (Amsili, Van Es, and Schindelbeck 2021), which indicates that they may also provide some redundancy for sand and SOM effects on θ_{FC}.

Permanent wilting point (θ_{PWP})

Model comparison and validation

Three pedotransfer functions were developed for gravimetric θ_{PWP}, including a Full RF model, a Reduced RF model, and MLR (Equation 7). Units of predictor variables and θ_{PWP} in Equation 7 are in g g^{-1}.

$$\theta_{PWP} = 0.0132 - 0.014sand + 0.244clay + 1.158SOM \tag{7}$$

There were fewer differences among models for θ_{PWP} then among models for θ_{FC} when they were compared using the Training (Figure 4a–c) and Validation Datasets (Figures 2 and 4d–f). The Full RF model had a higher percent variance explained (92.3%) and lower RMSE (0.011) compared to the MLR model ($R^2_{adj} = 0.88$; RMSE = 0.013) but was only marginally better than the Reduced RF model (%Var explained = 89.7%; RMSE = 0.012; Figure 4a–c). The second validation step with the independent NAPESHM dataset illustrated once again that each model had NRMSEs that were on average 36.3% higher (MLR: 28.9%, Reduced RF: 33.1%, and Full RF: 46.9%) than the same model

Figure 4. (a-c) measured vs. predicted permanent wilting point water content (θ_{PWP}) for full random forest (RF), reduced RF, and multiple linear regression (MLR) models on the training dataset. (a-b) full and reduced RF models show RF model out of bag predictions. Validation metrics within plots include percent variance explained, out of bag (OOB) root mean square error (RMSE), and OOB normalized RMSE (NRMSE). (d-f) measured vs. predicted permanent wilting point for full RF, reduced RF, and MLR models for the NAPESHM validation dataset. Text within plots includes the regression equation, adjusted R^2, mean absolute error (MAE), RMSE, and NRMSE.

Figure 5. (a-d) partial dependence plots for individual permanent wilting point water content (θ_{PWP}) predictor variables: clay, sand, magnesium, and soil organic matter. (e) Multi-predictor partial dependence plot with the interaction between clay and soil organic matter. These partial dependence plots show the influence of individual predictor variables on θ_{PWP} within the full RF model while all other predictor variables are held constant.

calculated for the Training dataset (Figure 4). As before, this demonstrates that RF models can be just as susceptible to overfitting to the Training dataset as an MLR model. The Full RF model had a 13.3% lower RMSE than the MLR model, which indicates that RF models can provide slight improvements to the prediction of θ_{PWP} (Figure 4d–f). In contrast to the prediction of θ_{FC}, the Full RF model was only marginally better than the Reduced RF model, which indicates that additional predictor variables provide less benefit for predicting θ_{PWP} than θ_{FC}, i.e., it is mostly defined by texture and SOM.

Variable importance

Clay was the most important variable for the prediction of θ_{PWP}, followed by SOM, and then Mg and sand (Figure 5, Equation 7, Figure S5). Clay content's importance in predicting PWP is sensible because clay is the primary determinant of the proportion of total porosity with a pore diameter equal to less than 0.20 µm, which is the theoretical pore size that can hold water at −1500 kPA (Amer, Logsdon, and Davis 2009). As follows, there was a strong positive relationship between clay content and θ_{PWP} from 0 to approximately 40% clay (Figure 5a). SOM also had a positive influence on θ_{PWP} from between 0 to approximately 7%, which may be due to an increase in total porosity or an increase in the proportion of total porosity with a diameter less than 0.20 µm (Libohova et al. 2018). SOM had a smaller effect on θ_{PWP} (Figure 5d) than it does on θ_{FC} (Figure 3d) by approximately a magnitude of 2. Both sand and exchangeable Mg led to similar reductions in MSE of θ_{PWP} and had similar size effects on θ_{PWP}. Sand had a negative effect on θ_{PWP} (Figure 5b) because increases result in a smaller proportion of total porosity with a diameter less than 0.20 µm. Whereas, Mg had a slight positive effect on θ_{PWP}, which could potentially be helping to separate soils that have clay mineralogy with more surface area like smectites (Figure 5c; Chu and Johnson 1985). This is a novel finding that extractable Mg was equally important to sand for the prediction of θ_{PWP}. Unlike θ_{FC}, there was no clear interaction between clay content and SOM, which was counter to previous research that found that SOM had a smaller impact on θ_{PWP} in soils with higher clay content (Minasny and Mcbratney 2018; Saxton and Rawls 2006).

Further variables were not explored due to the similarity between full and reduced RF models (i.e., texture components and SOM were sufficient for predicting θ_{PWP}).

Available water capacity (AWC)

Model comparison and validation

Three pedotransfer functions were developed for gravimetric AWC, including a Full RF model, a Reduced RF model, and MLR (Equation 8). Units of predictor variables and AWC in Equation 8 are in g g^{-1}.

$$AWC = 0.340 - 0.304 sand - 0.212 clay + 0.526 SOM + 0.184(sand \times clay) + 1.708(sand \times SOM) - 0.153(clay \times SOM)$$

(8)

Similar to θ_{FC}, the Full RF model performed better for AWC (%Var explained = 75.4%; RMSE = 0.035) than the Reduced RF and MLR models with the Training Dataset (Figure 6a–c). Whereas the Reduced RF model only had a marginally higher percent variance explained (66.4%) and marginally lower RMSE (RMSE = 0.041) than the MLR model (R^2_{adj} = 0.64; RMSE = 0.043; Figure 6b,c). The secondary independent validation with the NAPESHM dataset revealed that the Reduced RF and MLR models performed similarly (Figure 6e,f). It also demonstrated that each model had NRMSEs that were on average 3.8% higher (MLR: −0.6%, Reduced RF: 3.6%, and Full RF: 8.5%) than the same model

Figure 6. (a-c) measured vs. predicted available water capacity (AWC) for full random forest (RF), reduced random forest, and multiple linear regression models on the training dataset. (a-b) full and reduced random forest models show OOB RF model predictions on the training dataset. Validation metrics within plots include percent variance explained, out of bag (OOB) root mean square error (RMSE), and OOB normalized RMSE (NRMSE). (d-f) measured vs. predicted available water capacity for full random forest, reduced random forest, and multiple linear regression models for the NAPESHM validation dataset. Text within plots includes the regression equation, adjusted R^2, mean absolute error (MAE), RMSE, and NRMSE.

calculated for the Training dataset (Figure 6). In contrast to the models for θ_{FC} and θ_{PWP}, the models for AWC performed similarly when compared between the Training and Validation datasets. The Full RF model had a 12.8% lower RMSE than the MLR model, which indicates inclusion of additional variables beyond sand, silt, clay, and SOM can provide meaningful improvements to prediction of AWC (Figure 6d–f). In contrast, we found that the Reduced RF model performed similarly to the MLR model that contained similar predictor variables: sand, silt, clay, and SOM, indicating that simple modeling approaches like MLR can be adequate in situations where only 3–4 predictor variables are being used. If the goal is prediction and many potential predictors are available from a standard test, machine learning algorithms like RF can utilize all those variables to improve the prediction of AWC.

Variable importance

Silt and sand were the most important variables for predicting AWC, followed by SOM, clay, and POXC (Figures 7 and S6b). Silt was slightly more useful for reducing the MSE and had a slightly larger impact on AWC values than sand (Figures 6b,c and S6b,c). Silt content's importance for predicting AWC may be related to its particle size diameter range, 2–53 µm, corresponding most closely to the theoretical pore size range that stores plant available water, 0.20–30 µm (Amer, Logsdon, and Davis 2009; Libohova et al. 2018). Previous studies have documented that silt content has the highest correlation with AWC, followed by sand content (Amsili, Van Es, and Schindelbeck 2021; Libohova et al. 2018). Silt has a positive relationship with AWC while sand has a negative relationship with AWC. As described above, as sand content increases, the proportion of total porosity with a pore diameter greater than 30 µm, which is drained at −10kPa or θ_{FC}, increases. SOM, clay, and POXC were the third, fourth, and fifth most important variables for reducing MSE in the RF model. Both SOM and POXC had positive impacts on AWC values, with SOM having a slightly stronger influence on AWC than POXC as indicated by its mean SHAP value (Figures 7d, S6c and S7a). There was a clear interaction between sand content and SOM, where SOM has a larger effect on AWC in soils with higher sand content (Figure 7e). This interaction is visible in partial dependence plots for individual soil texture classes, where changes in SOM from 0 to 6% caused increases in AWC of 0.054, 0.051,

Figure 7. (a-d) partial dependence plots for individual available water capacity (AWC) predictor variables: sand, silt, clay, and soil organic matter. (e) Multi-predictor partial dependence plot with the interaction between sand and soil organic matter. These partial dependence plots show the influence of individual predictor variables on AWC within the full RF model while all other predictor variables are held constant.

0.032, and 0.029 g H_2O g^{-1} soil for sandy loam, loam, silt loam, and clay loam, respectively (Figure S8). Previous research has documented similar interactions between sand and SOM content (Libohova et al. 2018; Minasny and Mcbratney 2018; Rawls et al. 2003). The importance of POXC in the model indicates that POXC provides some additional value to SOM in prediction of AWC. POXC represents a small fraction of the total SOC by mass (i.e. 1–6% of total SOC; Amsili et al. 2023, unpublished data) and has been determined to most closely represents phenolic and polyphenolic compounds (Christy et al. 2023). Therefore, POXC likely provides some redundancy for SOM and may help to capture SOM quality effects on AWC. Although clay helped reduce MSE in the model, it had a negligible effect on AWC values as indicated by its partial dependence plot (Figure 7c) and mean SHAP value (Figure S6c). Interestingly, WAS and extractable Fe had a greater impact on AWC values in the RF model than clay content (Figure S7b,c). Higher WAS values were associated with lower AWC values (Figures S6c and S7b) which is likely an artifact of the WAS method used that tends to result in slightly higher mean values for coarse-textured soils compared to loam and fine-textured soils (Amsili et al. 2023). Extractable Fe also had a positive impact on AWC, which could help to parameterize pastures and hayfields, which tend to have lower pHs and as a result higher extractable Fe (Amsili, Van Es, and Schindelbeck 2021).

Sensitivity of AWC and RF models to agronomic management

Laboratory-measured gravimetric AWC was sensitive to treatment effects ($p < .05$) at 23/57 sites that were analyzed but was not consistently sensitive to specific agronomic management practices. Three of those significant results were not easily explainable by the associated SOM or texture data. Crop rotation, nutrient type, residue return level, tillage, cropping system, and cover crops significantly affected gravimetric AWC at 30.0, 28.6, 28.6, 26.8, 20.0, and 14.3% of sites that tested those management practices. Additionally, soil texture class did not appear to influence whether gravimetric AWC was sensitive to management. Gravimetric AWC was sensitive to management in 50, 30, 36, 40, 43, and 67% of loamy sand, sandy loam, loam, silt loam, clay loam, and silty clay loam sites, respectively. This potentially does not support the result that management is more likely to have a positive effect on AWC in coarser-textured soils, as is indicated in the model and previous research (Libohova et al. 2018; Minasny and Mcbratney 2018; Rawls et al. 2003). However, the duration of the experiment influenced the likelihood that agronomic management had a significant effect on gravimetric AWC. For example, only 18% of the experiments running for 0–15 years showed significant results. Whereas 75% of the experiments running for >45 years had significant results. This relatively short-term insensitivity to agronomic management may be an inherent limitation with gravimetric AWC as a dynamic soil health indicator. Using intact soil cores to measure θ_{FC} shows greater response to agronomic management but involves a significantly more expensive measurement that is not practical for routine laboratory analysis (Bagnall et al. 2022).

Prediction of AWC directly or calculation of AWC with predicted θ_{FC} and θ_{PW} using full RF models was able to replicate significant ($p < .05$) results at 5/20 sites when excluding apparent nonsensical results. However, at $p < .10$ AWC from predicted θ_{FC} and θ_{PWP} was able to accurately predict more experiments (9/20) than direct prediction of AWC (6/20). This suggests a slight advantage of predicting AWC by calculating it from predicted θ_{FC} and θ_{PWP} rather than direct prediction of AWC. In contrast, the direct prediction of AWC had a similar RMSE to the calculation of AWC with predicted θ_{FC} and θ_{PWP} (0.0389 vs 0.0395; Figure S9), indicating that a single Full RF model of AWC can enable direct prediction for use by a high throughput lab. Therefore, both methods of prediction of AWC are valid and up to the discretion of the user.

Comparison of predicted and measured AWC in long-term experiments demonstrated that using an RF model loses some statistical power to detect treatment effects compared to laboratory measured AWC. This is in part explained by the fact that sustainable agronomic management practices generally result in increased SOM, but this is associated with higher values for both θ_{FC} (Figure 3d) and θ_{PWP} (Figure 5d), thereby resulting in only modest effects on AWC = θ_{FC}-θ_{PWP}

(Figure 7d; Libohova et al. 2018). In all, AWC is best regarded as a relevant inherent soil property with limited ability to measure dynamic change, or soil health effects, from agronomic management.

Model availability and use

Full and reduced RF model files for θ_{FC}, θ_{PWP}, and AWC (i.e., six models) are available for download at the Harvard Dataverse (Amsili, Van Es, and Schindelbeck 2022). The Training dataset used to calibrate the models developed in this study is available for download. The Full RF model for AWC is most precise (lowest RMSE) in the Southwest, Southeast, and Northeast & Lake States, and least precise (highest RMSE) in the southern Plain States and Northwest (Figure S10). This is in part explained by less representation of these regions in the Training dataset, although the Southwest and Southeast also had low sample numbers but had high model performance (Table S1; Figure S10). New pedotransfer functions for gravimetric AWC fit into existing interpretive frameworks and cumulative normal distribution functions for scoring AWC, which would enable their rapid implementation by a commercial soil health laboratory (Moebius-Clune et al. 2017).

Conclusions

Growing interest in comprehensive soil health assessment requires the development of pedotransfer functions to predict some of the costly soil health indicators instead of directly measuring them. Gravimetric AWC is widely considered a key physical soil health measurement and the only indicator to directly assess a soil's water supply capacity. However, of the commonly measured soil health indicators, it is the most time-intensive, expensive to measure, and least sensitive to management. Our research utilizing large training and validation datasets demonstrated that full random forest models improved prediction of θ_{FC}, θ_{PWP}, and AWC compared to MLR models. This indicates that if the goal is prediction, variables beyond sand, silt, clay, and SOM such as POXC, WAS, and extractable Mg, K, and Fe can improve predictions of θ_{FC}, θ_{PWP}, and AWC. NAPESHM experiments confirmed that gravimetric AWC is not consistently sensitive to management practices that have been carried out for <30 years, indicating its short-term insensitivity. Therefore, gravimetric AWC is most useful for capturing a soil's inherent ability to store plant available water and some dynamic effects of large differences in SOM on AWC, but is less useful for capturing the effects of short-term agronomic management on this function.

Abbreviations

θ_{FC}	gravimetric field capacity water content
θ_{PWP}	gravimetric permanent wilting point water content
AWC	available water capacity
WAS	wet aggregate stability
SOM	soil organic matter
SOC	soil organic carbon
Resp	soil respiration from 4-day incubation
POXC	permanganate-oxidizable carbon
CASH	Comprehensive Assessment of Soil Health
NAPESHM	North American Project to Evaluate Soil Health Measurements
RF	random forest
OOB	out-of-bag
MLR	multiple linear regression
RMSE	root mean square error
MAE	mean absolute error.

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1   **Supplemental figures and tables for:**

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3 **Pedotransfer Functions for Field Capacity, Permanent Wilting Point, and**

4 **Available Water Capacity based on Random Forest Models for Routine Soil**

5 **Health Analysis**

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23   Table S1. Number of soil samples in the U.S. Training Dataset by state and soil texture class.

State	n	State	n	Region	n	Texture	n
AK	80	NC	122	Mid-Atlantic/ East Central/	772	Clay	36
AR	54	ND	170	Midwest	2,954	Clay loam	243
AZ	3	NE	177	Northeast	1,702	Loam	1,401
CA	234	NH	242	Northwest	295	Loamy sand	284
CO	105	NJ	44	N. Plain States	652	Sand	183
CT	48	NM	14	S. Plain States	166	Sandy loam	1,266
DC	28	NV	19	Southeast	334	Sandy clay loam	94
DE	8	NY	742	Southwest	277	Silt	11
FL	66	OH	192	Alaska	80	Silt loam	2,903
GA	58	OR	201			Silty clay	168
IA	593	PA	527			Silty clay loam	643
ID	5	RI	38				
IL	710	SC	3				
IN	965	SD	104				
KS	40	TN	2				
MA	38	TX	166				
MD	153	UT	7				
ME	34	VA	25				
MI	346	VT	214				
MN	180	WA	89				
MO	178	WI	136				
MS	4	WV	10				
MT	52	WY	4				

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Figure S1. Eight regions of the U.S. divided by state and grouped to reflect USDA-NRCS Land

Resource Regions as closely as possible.

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42   Table S2. Number of soil samples in the US NAPESHM Validation Dataset by state and soil

43   texture class.

State	n	State	n	Region	n	Texture	n
AL	68	NC	67	Mid-Atlantic/ East Central/	199	Clay	5
AR	9	ND	42	Midwest	305	Clay loam	103
AZ	24	NE	54	Northeast	164	Loam	221
CA	40	NY	60	Northwest	83	Loamy sand	79
CO	88	OH	54	N. Plain States	304	Sand	18
DE	10	OK	9	S. Plain States	72	Sandy loam	233
FL	10	OR	39	Southeast	182	Sandy clay	2
GA	2	PA	57	Southwest	97	Sandy clay loam	26
IA	45	SC	8			Silt	3
ID	14	SD	34			Silt loam	508
IL	24	TN	72			Silty clay	17
IN	27	TX	63			Silty clay loam	191
KS	40	UT	33				
KY	48	VA	12				
LA	6	WA	30				
MI	346	WI	32				
MN	180	WV	12				
MO	178	WY	6				
MT	52						

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Figure S2. Comparison of attribute space of Training and NAPESHM Validation datasets for sand, silt, clay, and soil organic matter (SOM). Kernal density plots with dashed lines indicating mean values were constructed for sand, silt, clay, and SOM in both datasets.

Figure S3. Variable importance plots for the Full RF model for Field Capacity (θ_{FC}) created using the (a-b) randomForestExplainer and (c) shapviz packages in R. (a) Mean depth distribution of predictor variables in the 500 regression trees that make up the random forest model. (b) Mean squared error (MSE) increase vs. Node purity increase for the predictor variables in the RF model. Higher MSE increase is associated with more important variables in the model (i.e., removing that variable would result in a larger increase in MSE). (c) SHAP variable importance plots; (left panel) shows the ranked variable importance and its mean absolute SHAP value; (right panel) The beeswarm plot shows the relationship between the value of the predictor variable and its positive or negative impact on FC.

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76   Figure S4. (a-c) Partial dependence plots for individual field capacity water content (θ_{FC})

77   predictor variables: permanganate oxidizable carbon, magnesium, and potassium, within the Full

78   random forest model for field capacity. These partial dependence plots show the influence of

79   individual predictor variables on field capacity within the Full RF model while all other predictor

80   variables are held constant.

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Figure S5. Variable importance plots for the Full RF model for Permanent Wilting Point (θ_{PWP})

created using the (a-b) randomForestExplainer and (c) shapviz packages in R. (a) Mean depth

distribution of predictor variables in the 500 regression trees that make up the RF model. (b)

Mean squared error (MSE) increase vs. Node purity increase for the predictor variables in the RF

model. Higher MSE increase is associated with more important variables in the model (removing

that variable would result in a larger increase in MSE). (c) SHAP variable importance plots; (left

panel) shows the ranked variable importance and its mean absolute SHAP value; (right panel)

The beeswarm plot shows the relationship between the value of the predictor variable and its

positive or negative impact on PWP.

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Figure S6. Variable importance plots for the Full RF model for Available Water Capacity
(AWC) created using the (a-b) randomForestExplainer and (c) shapviz packages in R. (a) Mean
depth distribution of predictor variables in the 500 regression trees that make up the RF model.
(b) Mean squared error (MSE) increase vs. Node purity increase for the predictor variables in the
RF model. Higher MSE increase is associated with more important variables in the model
(removing that variable would result in a larger increase in MSE). (c) SHAP variable importance
plots; (left panel) shows the ranked variable importance and its mean absolute SHAP value;
(right panel) The beeswarm plot shows the relationship between the value of the predictor
variable and its positive or negative impact on AWC.

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Figure S7. (a-c) Partial dependence plots for individual predictor variables: permanganate oxidizable carbon, wet aggregate stability, and iron, within the Full random forest model for available water capacity (AWC). These partial dependence plots show the influence of individual predictor variables on available water capacity within the Full RF model while all other predictor variables are held constant.

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Figure S8. (a-d) Manual partial dependence plots for soil organic matter within the Full random forest model for available water capacity (AWC) for four different texture classes (sandy loam, loam, silt loam, and clay loam/silty clay loam).

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126 Figure S9. (a-b) Measured available water capacity (AWC) vs (a) directly predicted AWC or vs.

127 (b) calculated AWC with predicted field capacity (θ_{FC}) and permanent wilting point (θ_{PWP}) with

128 the NAPESHM dataset.

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132 Figure S10. Measured vs. Predicted AWC for the NAPESHM dataset in eight different regions

133 of the contiguous US.