A NOTE ON THE INTERVAL FUNCTION OF A DISCONNECTED GRAPH

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Abstract

In this note we extend the Mulder-Nebesky characterization of the interval function of a connected graph to the disconnected case. One axiom needs to be adapted, but also a new axiom is needed in addition.

Keywords: interval function, transit function, axiomatic characterization, disconnected graph.

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