NOTE

SMALLEST REGULAR GRAPHS OF GIVEN DEGREE AND DIAMETER

MARTIN KNOR¹

*Slovak University of Technology in Bratislava
Faculty of Civil Engineering, Department of Mathematics
Radlinského 11, 813 68 Bratislava*

e-mail: knor@math.sk

Abstract

In this note we present a sharp lower bound on the number of vertices in a regular graph of given degree and diameter.

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