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Supporting information for article:

Incommensurate structures and radiation damage in Rb₂V₃O₈ and K₂V₃O₈ mixed-valence vanadate fresnoites

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Table S1 Experimental data for the measurement on the (3+1)-*d* structure of $K_2V_3O_8$ at 100 K ($\bullet = 0.69127 \text{ \AA}$).

Superspace group	<i>Cmm</i> 2(0 β 1/2) <i>s</i> 00
<i>a</i> (Å)	12.6452(9)
<i>b</i> (Å)	12.6452(9)
<i>c</i> (Å)	5.2235(5)
<i>V</i> (Å ³)	835.2
<i>Z</i>	4
<i>D_c</i> (g cm ⁻³)	2.855
Twin volume (1,2)	0.469(2),
0.531(2)	
<i>G_{iso}</i>	0.214(6)
Modulation vector q	0, 0.626, 0.5
<i>Data collection</i>	
No. measured refl.	8351
No. main refl.	1575
No. satellite refl. $\pm (1,0)$	6776
Range of <i>hkl</i>	-16 < <i>h</i> < 15
	-16 < <i>k</i> < 16
	-6 < <i>l</i> < 6
	-1 < <i>m</i> < 1
No. observed refl. (all, main, satellites) ^a	1929, 762, 1167
<i>R_{int}</i> (obs/all)	1.58/1.61
<i>Refinement</i> ^b	
<i>R_{obs/all}</i> (all refl.)	1.58/2.40
<i>wR_{obs/all}</i> (all refl.)	1.98/2.09
<i>R_{obs/all}</i> (main refl.)	1.34/1.39
<i>wR_{obs/all}</i> (main refl.)	1.80/1.83
<i>R_{obs/all}</i> (satellite refl. $\pm (1,0)$)	4.09/8.48
<i>wR_{obs/all}</i> (satellite refl. $\pm (1,0)$)	4.49/5.31
No. parameters	144

^a Criterion for observed reflections is $|F_{\text{obs}}| > 3\sigma$

^b All agreement factors are given in %, weighing scheme $1/[\sigma^2(F_{\text{obs}}) + (0.01 F_{\text{obs}})^2]$

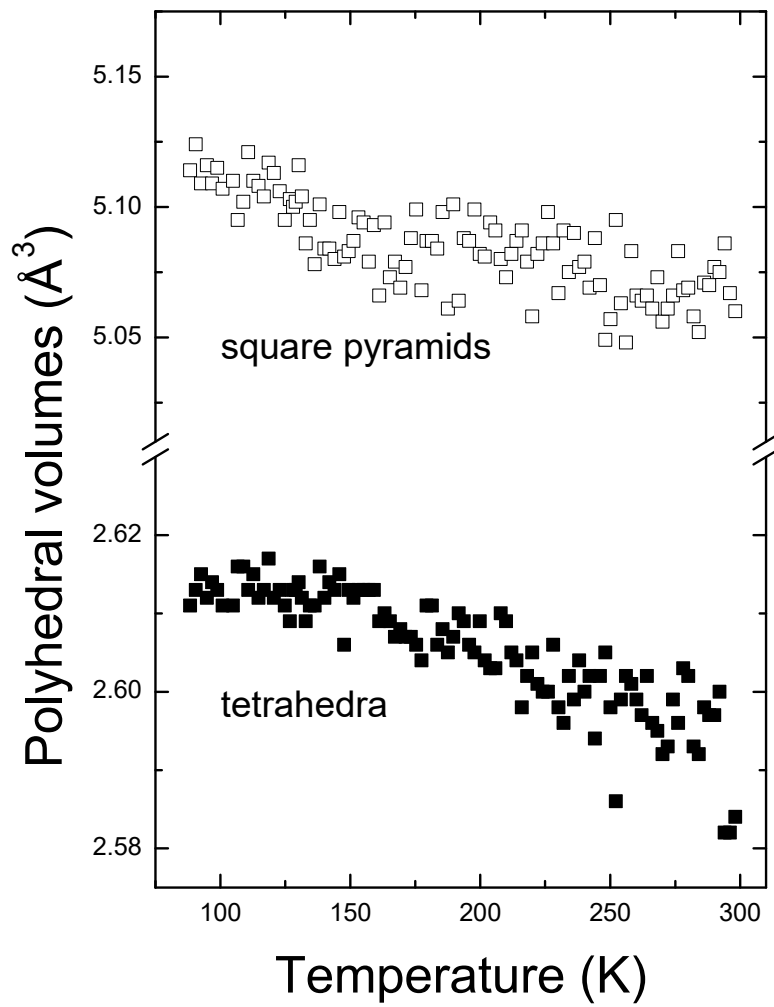


Figure S1 Volume of the tetrahedra and square pyramids as a function of temperature in $\text{K}_2\text{V}_3\text{O}_8$.

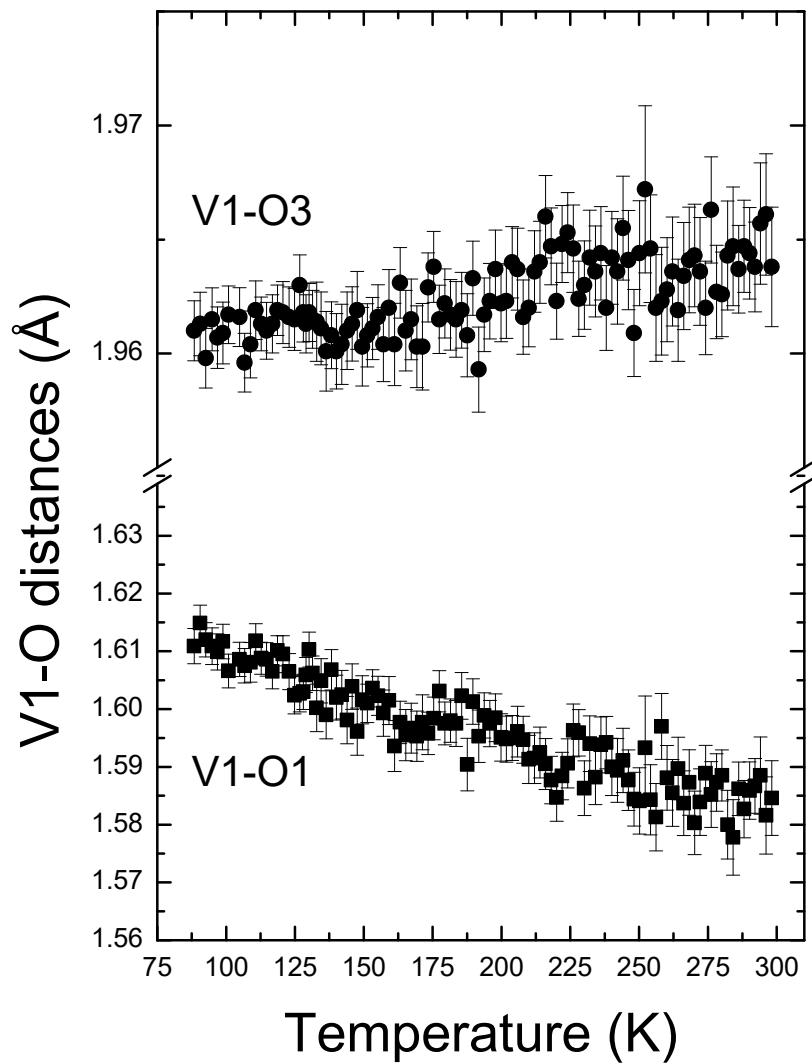
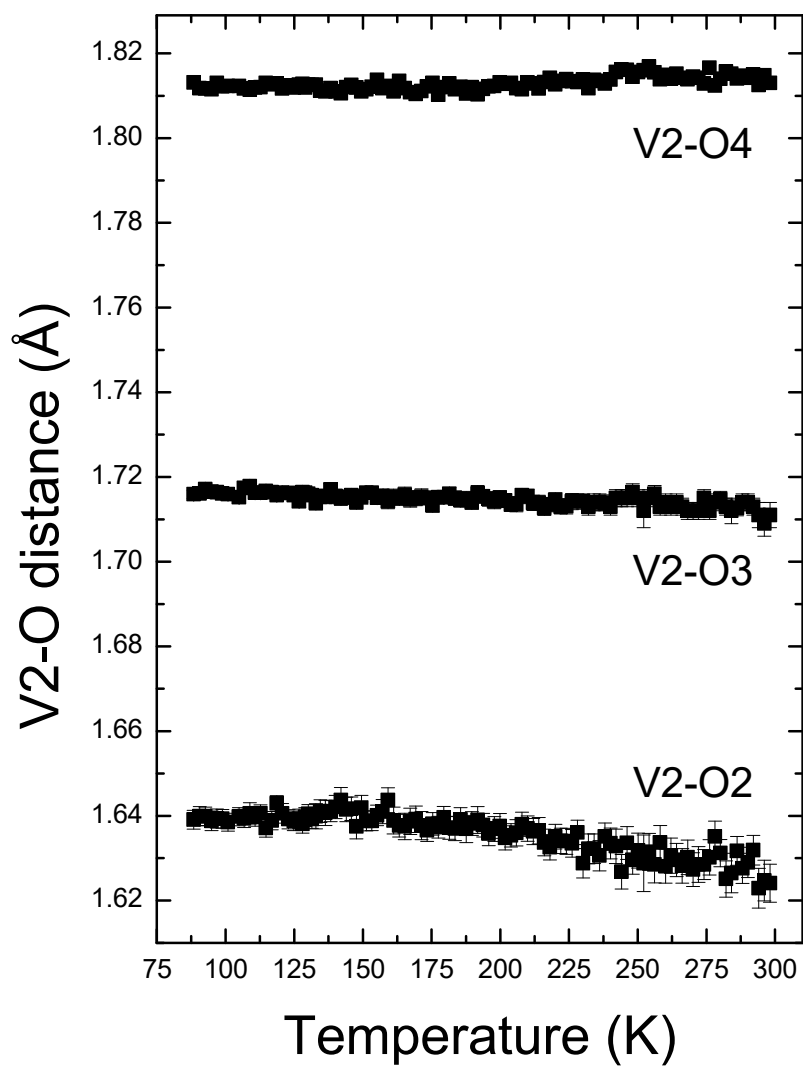
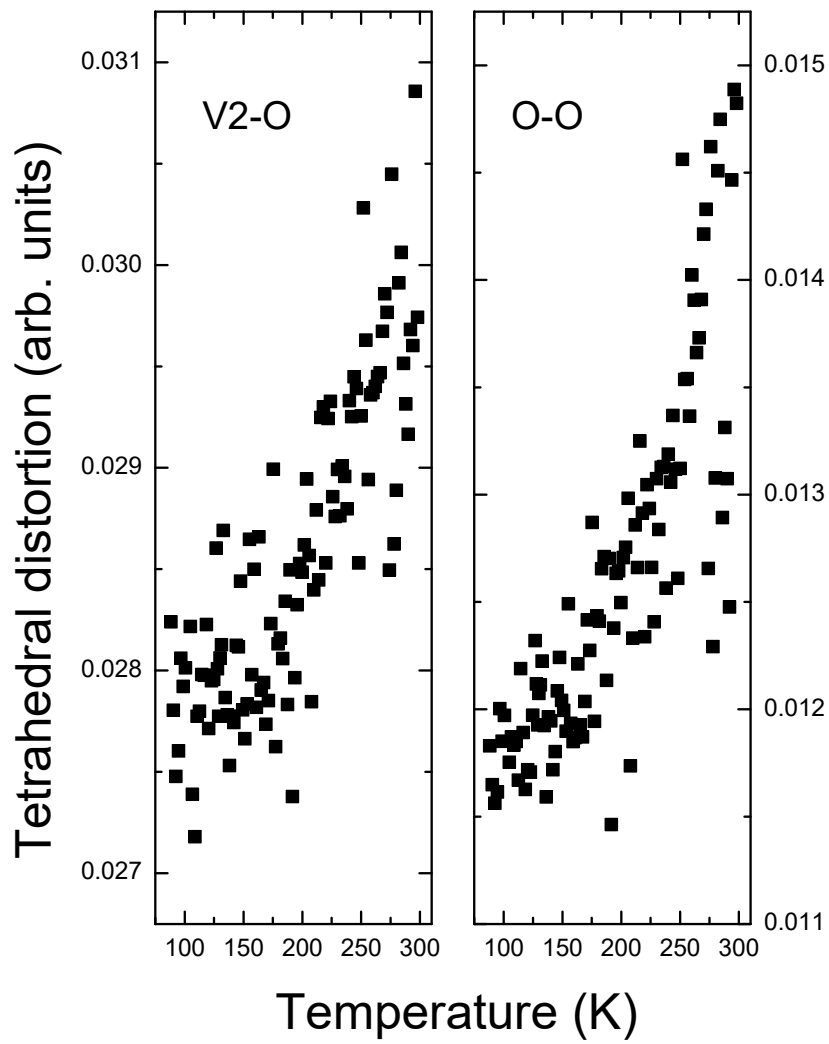


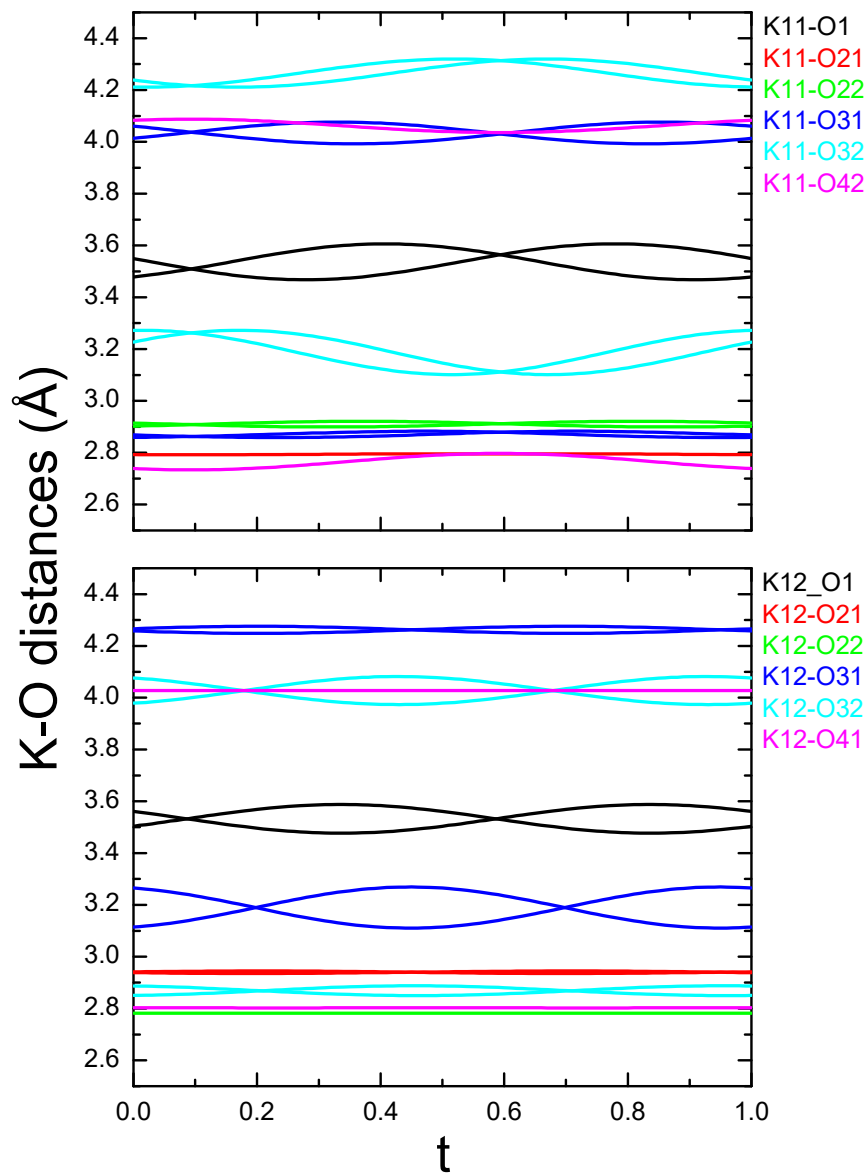
Figure S2

V1-O interatomic distances in the VO₅ square pyramid as a function of temperature inK₂V₃O₈.

**Figure S3**

V2-O interatomic distances in the VO_4 tetrahedra as a function of temperature in $K_2V_3O_8$. The standard deviations are drawn when larger than the size of the symbols.

**Figure S4**V2-O bond-length and O-O distance tetrahedral distortions in $K_2V_3O_8$.

**Figure S5**

K-O distances in the (3+1)-*d* structure of $K_2V_3O_8$ at 100 K as a function of the internal coordinate *t*.

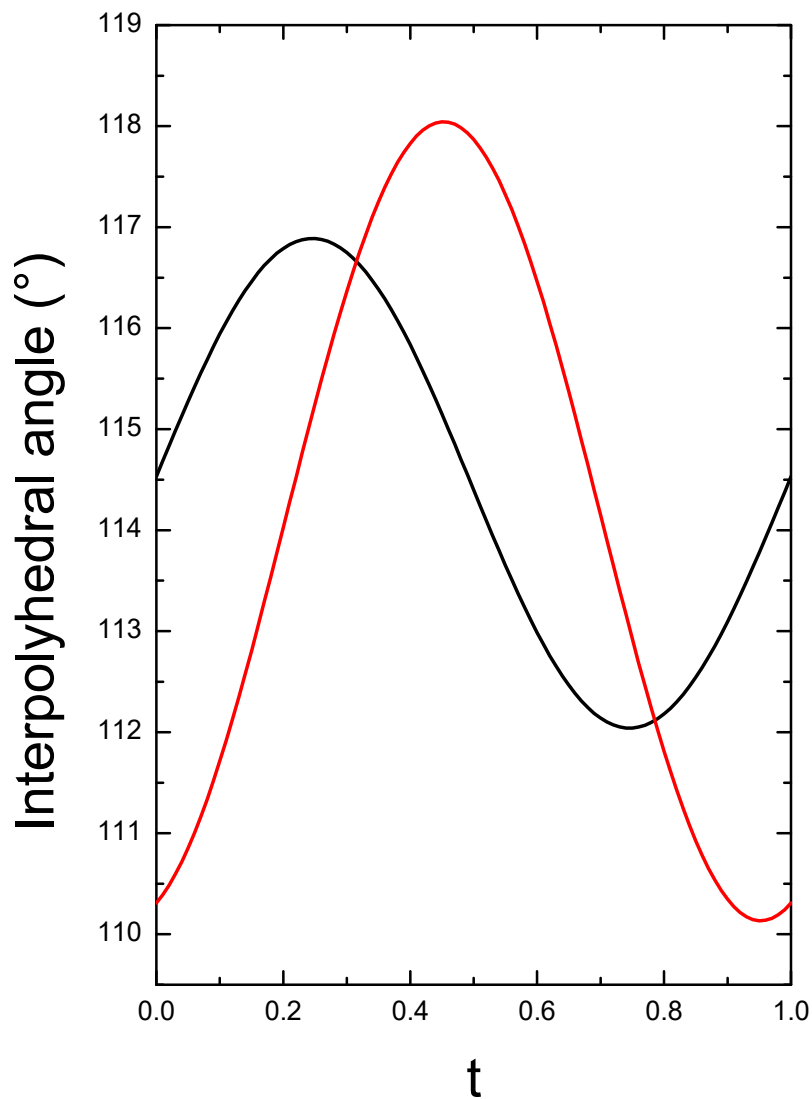
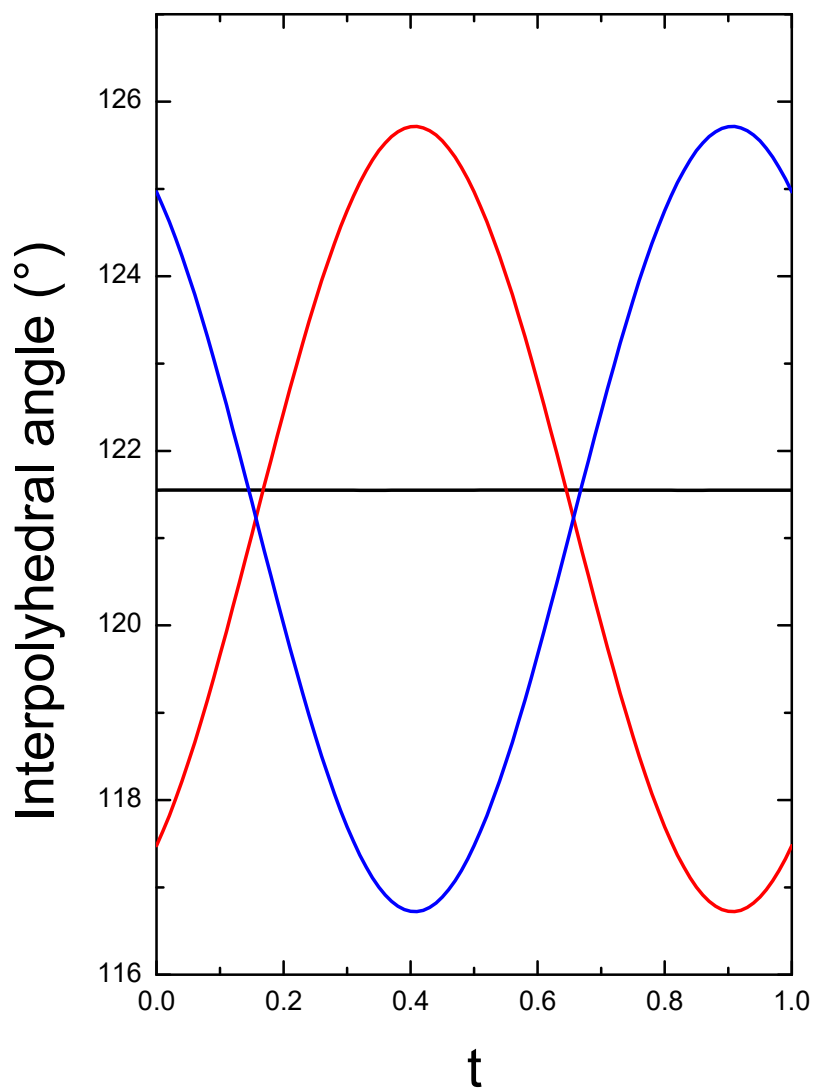


Figure S6 O31-O31-O32 (black line) and O31-O32-O32 (red line) interpolyhedral angles in the (3+1)- d model as a function of the internal coordinate t .

**Figure S7**

O31-O41-O31 (black line), O32-O42-O32 (red line), and O32-O42-O32 (blue line)

interpolyhedral angles in the (3+1)- d model as a function of the internal coordinate t .