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**Supporting information for article:**

**Size effect of the guest cation on the  $\text{AlO}_4$  framework in aluminato sodalite-type oxides  $M_8[\text{Al}_{12}\text{O}_{24}](\text{SO}_4)_2$  ( $M = \text{Sr}$  and  $\text{Ca}$ ) in the  $I43m$  phase**

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**Table S1** Volumetric thermal expansion coefficient  $\alpha_V$  of (a) SAS and (b) CAS in each phase.

(a) SAS		(b) CAS	
Phase (temperature range)	$\alpha_V$ [ $10^{-5} \text{ K}^{-1}$ ]	Phase (temperature range)	$\alpha_V$ [ $10^{-5} \text{ K}^{-1}$ ]
Tetragonal ( $300 < T < 520 \text{ K}$ )	1.8	Orthorhombic ( $300 < T < 740 \text{ K}$ )	1.2
Cubic ( $I\bar{4}3m$ ) ( $520 < T < 960 \text{ K}$ )	3.0	Cubic ( $I\bar{4}3m$ ) ( $740 < T < 1100 \text{ K}$ )	2.9
Cubic ( $Im\bar{3}m$ ) ( $960 < T < 1100 \text{ K}$ )	5.0	-	-

**Table S2** Structural parameters of SAS in the  $Im\bar{3}m$  phase (1100 K)  $a = 9.483220(6)$  Å;  $wRp = 3.33\%$ ;  $R_F = 3.21\%$ ;  $R_B = 3.36\%$ ; goodness-of-fit = 1.54.

Atom	Site	Symmetry	$g$	$x$	$y$	$z$
Sr	8c	$\bar{3}m$	1	1/4	$= x$	$= x$
S	2a	$m\bar{3}m$	1	0	0	0
Al	12d	$\bar{4}2m$	1	1/4	1/2	0
O1	24h	$mm2$	1	0.15813(13)	$= x$	1/2
O2	16f	$3m$	1	0.0815(3)	$= x$	$= x$

Atom	$U_{11}$ [Å <sup>2</sup> ]	$U_{22}$ [Å <sup>2</sup> ]	$U_{33}$ [Å <sup>2</sup> ]	$U_{12}$ [Å <sup>2</sup> ]	$U_{13}$ [Å <sup>2</sup> ]	$U_{23}$ [Å <sup>2</sup> ]
Sr	0.1019(7)	$= U_{11}$	$= U_{11}$	0.0735(7)	$= U_{12}$	$= U_{12}$
S	0.1062(16)	$= U_{11}$	$= U_{11}$	0	0	0
Al	0.0236(10)	0.0208(5)	$= U_{22}$	0	0	0
O1	0.0293(8)	$= U_{11}$	0.0525(13)	0.0229(10)	0	$= U_{12}$
O2	0.401(6)	$= U_{11}$	$= U_{11}$	0.008(3)	$= U_{12}$	$= U_{12}$

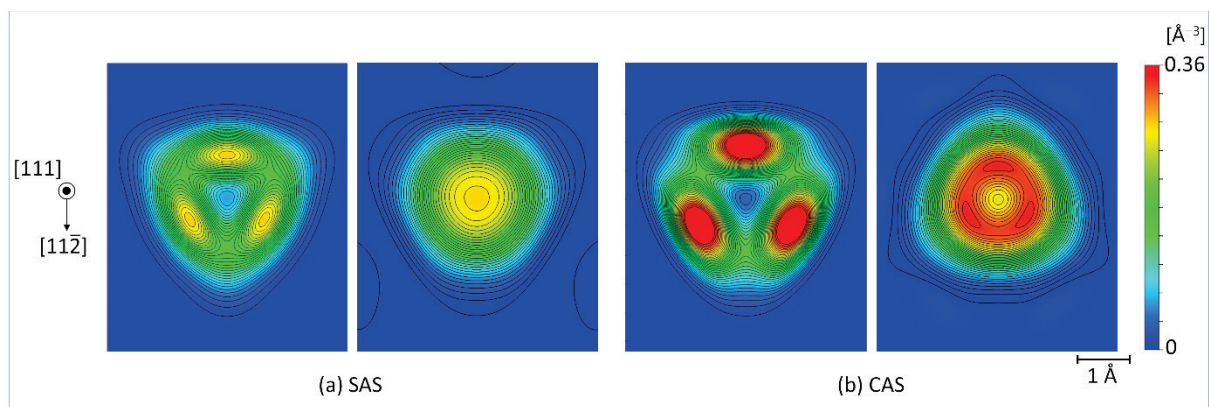
Atom	$C_{111}$ [10 <sup>-3</sup> ]	$C_{112}$ [10 <sup>-3</sup> ]	$C_{123}$ [10 <sup>-3</sup> ]	$D_{1111}$ [10 <sup>-4</sup> ]	$D_{1112}$ [10 <sup>-4</sup> ]	$D_{1122}$ [10 <sup>-4</sup> ]	$D_{1123}$ [10 <sup>-4</sup> ]
Sr	0	0	0	-0.0025(7)	-0.0039(4)	-0.0034(4)	-0.0047(5)
O2	0.032(11)	0.026(13)	-0.121(19)	0.35(5)	0.211(7)	0.23(5)	0.29(2)

restriction of 8c site ( $\bar{3}m$ ):  $C_{ijk} = 0$  ( $i, j, k = 1, 2, 3$ ),  $D_{1111} = D_{2222} = D_{3333}$ ,  $D_{1112} = D_{1113} = D_{1222} = D_{1333} = D_{2223} = D_{2333}$ ,  $D_{1122} = D_{1133} = D_{2233}$ ,  $D_{1123} = D_{1223} = D_{1233}$

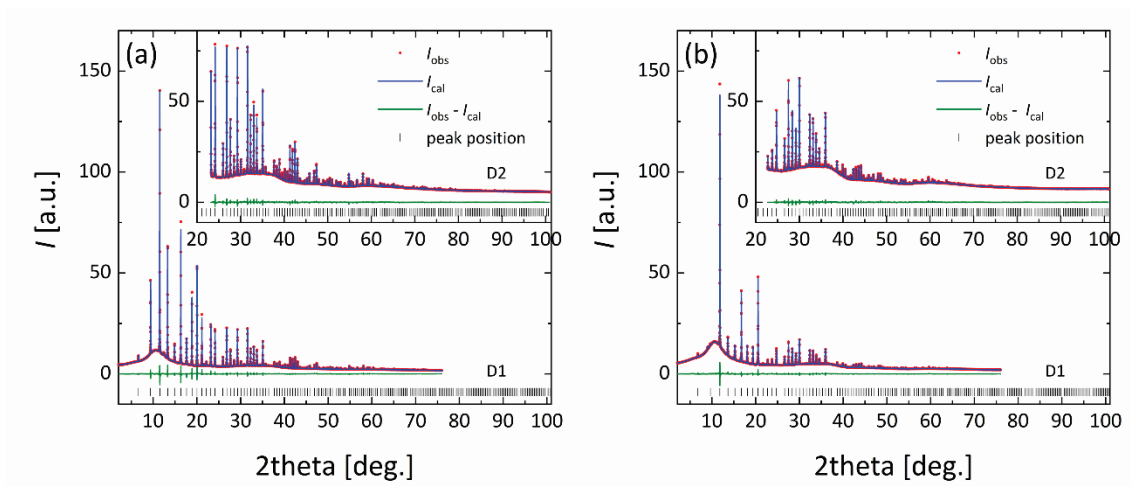
restriction of 16f site ( $3m$ ):  $C_{111} = C_{222} = C_{333}$ ,  $C_{112} = C_{113} = C_{122} = C_{133} = C_{223} = C_{233}$ ,  $D_{1111} = D_{2222} = D_{3333}$ ,  $D_{1112} = D_{1113} = D_{1222} = D_{1333} = D_{2223} = D_{2333}$ ,  $D_{1122} = D_{1133} = D_{2233}$ ,  $D_{1123} = D_{1223} = D_{1233}$

**Table S3** Positions of maxima in the PDFs of the guest cations, O1 and O2 in the  $\bar{I}43m$  phase (850 K) of SAS and CAS. The maxima of O1 are the same as those listed in Table 2.

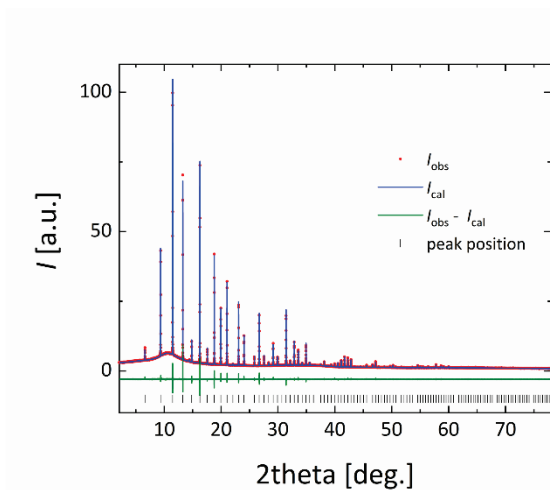
Material	Atom	Symmetry	$x$	$y$	$z$
SAS	Sr	$3m$	0.220(1)	$= x$	0.235(1)
	O1	$m$	0.15715(10)	$= x$	0.48364(18)
	O2	$3m$	0.078(1)	$= x$	$= x$
CAS	Ca	$3m$	0.212(1)	$= x$	$= x$
	O1	$m$	0.15379(11)	$= x$	0.44811(11)
	O2	$3m$	0.130(1)	0.046(1)	$= y$



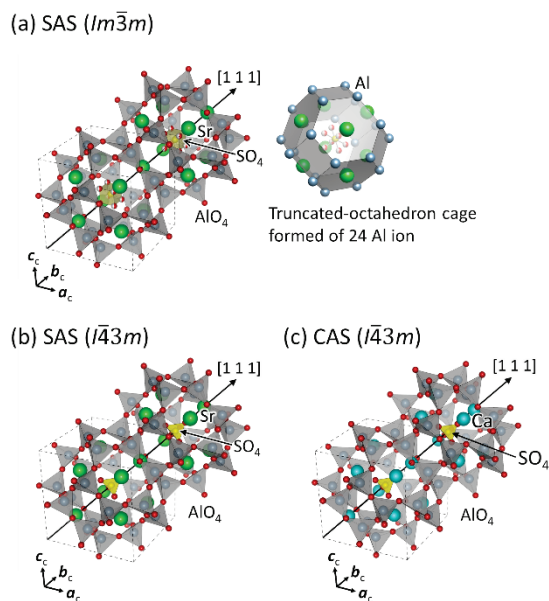
**Figure S1** Two-dimensional maps of PDF of O2 atom in the  $I\bar{4}3m$  phase (850 K). Datasets D1 and D2 were used. (a) SAS. (b) CAS. The left- and right-hand figures show the maps derived from the 3-site model and the Gram-Charlier method, respectively.



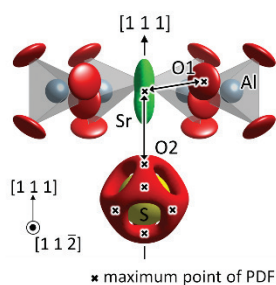
**Figure S2** Rietveld profile fitting results of (a) SAS and (b) CAS in the  $I\bar{4}3m$  phase (850 K). Insets represent fitting results of high-angular D2 data ( $d > 0.5$  Å).



**Figure S3** Rietveld profile fitting results of SAS in the  $Im\bar{3}m$  phase (1100 K). The structural parameters and  $R$ -factors are summarized in Table S2.



**Figure S4** Crystal structure models of SAS and CAS. (a) SAS in the  $Im\bar{3}m$ . A truncated octahedron-shaped cage comprising Al atoms is shown. Eight Sr atoms were located at the centers of the eight hexagonal surfaces.  $SO_4$  ions were present in the cages. The four O atoms of  $SO_4$  occupy the eight sites by symmetry restriction. (b) SAS in the  $I\bar{4}3m$  phase (c) CAS in the  $I\bar{4}3m$  phase.



**Figure S5** ORTEP-like view of PDF (isosurface of  $0.17 \text{ \AA}^{-3}$ ) of SAS in the  $Im\bar{3}m$  phase (1100 K). The cross mark represents the maximum point in the PDF of each atom. O2 had eight maximum points in the PDF in the  $\langle 1\ 1\ 1 \rangle$  direction.