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Supporting information for article:

On the stacking disorder of dl-norleucine
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## S1. Validation of the force field and DFT-D calculations

The molecular structure of a single molecule from the single crystals of the $\alpha$-and $\beta$-phases from DL-norleucine were compared with a single molecule of the crystal structures optimised by Dreiding force field and DFT-D (Table S1).

Table S1 Comparison of the experimental molecular structure of DL-norleucine with force field and DFT-D optimised molecular structure.

|  | $\alpha$-phase |  |  | $\beta$-phase |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bond length / Å | observed ${ }^{\text {a }}$ | DFT-D | Force field | observed $^{\text {b }}$ | DFT-D | Force field |
| O1-C1 | 1.249(2) | 1.266 | 1.245 | 1.248(1) | 1.266 | 1.245 |
| O2-C1 | 1.256(2) | 1.278 | 1.243 | 1.262(1) | 1.277 | 1.243 |
| N1-C2 | 1.488(2) | 1.488 | 1.461 | 1.487(1) | 1.489 | 1.461 |
| C1-C2 | 1.521(3) | 1.529 | 1.465 | 1.528(1) | 1.529 | 1.465 |
| C2-C3 | 1.528(3) | 1.532 | 1.546 | 1.529(1) | 1.532 | 1.546 |
| C3-C4 | 1.513(3) | 1.526 | 1.545 | 1.526(2) | 1.526 | 1.545 |
| C4-C5 | 1.502(4) | 1.524 | 1.543 | 1.517(2) | 1.524 | 1.543 |
| C5-C6 | 1.509(5) | 1.525 | 1.538 | 1.521(2) | 1.525 | 1.538 |
| Angle / ${ }^{\circ}$ |  |  |  |  |  |  |
| O1-C1-02 | 125.8(2) | 125.31 | 114.70 | 126.1(1) | 125.25 | 114.70 |
| O1-C1-C2 | 117.1(2) | 117.31 | 123.27 | 117.0(1) | 117.04 | 123.27 |
| O2-C1-C2 | 117.0(2) | 117.29 | 122.02 | 116.8(1) | 117.63 | 122.02 |
| N1-C2-C1 | 109.3(2) | 108.94 | 108.56 | 108.8(1) | 108.71 | 108.59 |
| N1-C2-C3 | 110.9(2) | 110.65 | 112.94 | 110.7(1) | 110.43 | 112.92 |
| C1-C2-C3 | 109.3(2) | 109.41 | 110.55 | 109.0(1) | 109.56 | 110.56 |
| C4-C3-C2 | 116.4(2) | 114.09 | 114.05 | 115.4(1) | 114.03 | 114.02 |
| C5-C4-C3 | 113.7(2) | 112.50 | 111.44 | 112.7(1) | 112.65 | 111.46 |


| C4-C5-C6 | $114.3(3)$ | 112.52 | 112.21 | $113.1(1)$ | 112.34 | 112.17 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Torsion angle ${ }^{\circ}$ |  |  |  |  |  |  |
| O1-C1-C2-N1 | -30.59 | -31.34 | -47.94 | $-31.1(1)$ | -33.48 | -48.10 |
| O2-C1-C2-N1 | 153.22 | 151.92 | 133.47 | $152.7(1)$ | 149.59 | 133.29 |
| N1-C2-C3-C4 | -53.51 | -51.67 | -55.06 | $-52.7(1)$ | -52.05 | -55.23 |
| C1-C2-C3-C4 | -174.07 | -171.70 | -176.95 | $-172.3(1)$ | -171.76 | -177.11 |
| C2-C3-C4-C5 | -177.76 | -179.79 | -174.72 | $-177.9(1)$ | -178.35 | -174.86 |
| C3-C4-C5-C6 | -174.30 | -173.60 | -174.85 | $-174.6(1)$ | -176.11 | -175.08 |

${ }^{\text {a }}$ Harding et al. (1995)
b Dalhus \& Görbitz (1996)

The Dreiding force field describes the molecular structure of both phases of DL-norleucine in a reliable way. The force field is sufficiently adapted to norleucine. The DFT-D geometry of the molecule is in similarly good agreement with the experimental molecular structure.
R.m.s. cartesian displacement (r.m.s.c.d.) values of non-hydrogen atoms were additionally calculated after the method of van de Streek and Neumann (2010) (van de Streek, Neumann, 2010). An r.m.s.c.d. value above $0.25 \AA$ "either indicates an incorrect experimental crystal structure or reveal interesting structural features". The calculated r.m.s.c.d. values are given in Table S2.

Table S2 R.m.s. cartesian displacement values of force field and DFT-D optimised crystal structures of DL-norleucine.

|  |  |  | R.m.s.c.d. value / $\AA$ |
| :--- | :--- | :--- | :--- |
| Crystal structure | Stacking sequence | Force field | DFT-D |
| $\alpha$-phase | L | 0.206 | 0.147 |
| $\beta$-phase | LM | 0.200 | 0.081 |

The calculated r.m.s.c.d. values of the force field as well as the DFT-D calculations are far below $0.25 \AA$. Therefore both methods can be used for the geometry optimisation of ordered models of DL-norleucine.

## S2. Lattice-energy minimisations using force fields

Results of the lattice energy minimisations using force fields with models containing four double layers ( $\boldsymbol{c}^{\prime}=4 \boldsymbol{c}_{0}$ ) are shown in Table S3. Models including a mixture of $L, M, A$ and $B$ layers are less favourable by nearly $1 \mathrm{~kJ} \cdot \mathrm{~mol}^{-1}$. The stacking sequences LAMB, LBMA and LAMA increase the energy by about $2 \mathrm{~kJ} \cdot \mathrm{~mol}^{-1}$.

Table S3 Results of the lattice-energy minimisations using force field on models containing four double layers $\left(c^{\prime}=4 \boldsymbol{c}_{0}, Z=16\right)$.

| Stacking sequence | Space group model $^{h}$ | Force field methods <br> Relative energy / <br> $\mathrm{kJ} \cdot \mathrm{mol}^{-1}$ | Remarks |
| :---: | :---: | :---: | :---: |
| LLLL | $P 2_{1} / a, \mathrm{Z}=4$ | 0.00 | $\alpha$-phase |
| LLLM | $P 2_{1} / a, Z=16$ | 0.02 |  |
| LMLM | $C 2 / c, Z=8$ | 0.05 | $\beta$-phase |
| LLMM | $A 2 / a, \mathrm{Z}=16$ | 0.02 |  |
| LLLA | $P 2{ }_{1} / a, Z=16$ | 1.03 |  |
| LALA | $P 2_{1} / c, Z=4$ | 2.01 |  |
| LLAA | $P 2_{1} / a, \mathrm{Z}=8$ | 1.03 |  |
| LLLB | $P 2_{1} / a, Z=16$ | 0.99 |  |
| LBLB | $A 2 / n, Z=8$ | 1.92 |  |
| LLBB | $A 2 / a, \mathrm{Z}=16$ | 0.99 |  |
| LMAM | $P 2{ }_{1} / a, Z=16$ | 1.01 |  |
| LMBM | $P 2_{1} / a, Z=16$ | 1.05 |  |
| LMAB | $P 2 / a, \mathrm{Z}=8$ | 1.01 |  |
| LAMB | $A 2 / a, \mathrm{Z}=16$ | 1.97 |  |
| LBAM | $P 2 / a, \mathrm{Z}=8$ | 1.01 |  |
| LBMA | $A 2 / a, \mathrm{Z}=16$ | 1.97 |  |


| LMAB | $P 2 / a, Z=8$ | 1.01 |
| :--- | :--- | :--- |
| LMBA | $A 2 / a, Z=16$ | 1.05 |
| LAAB | $P a, Z=16$ | 1.02 |
| LABA | $P 2_{1} / a, Z=16$ | 1.05 |
| LBAA | $P a, Z=16$ | 1.02 |
| LAAM | $P a, Z=16$ | 1.02 |
| LAMA | $P a, Z=16$ | $1.07, Z=16$ |
| LMAA | $P a, Z=16$ | 1.02 |
| LBBA | $P 2_{1} / a, Z=16$ | 1.01 |
| LBAB | $P a, Z=16$ | 1.02 |
| LABB |  |  |

## S3. Local stacking probabilities

Assuming that the energy of a double layer is given by the neighbouring double layers in a finite distance, this double layer is considered to be the centre of a layer triple. Therefore the latticeenergy is calculated by the sum of the energies of the layer triples within a given model size.

For the stacking sequences, an additive combination of energies is assumed, i.e. the energy of a given double layer depends almost exclusively only on the arrangement of the neighbouring layers, whereas interactions with more distant double layers do not play a major role. For a given length of the local layer triple, we use a combinatorial approach to get the total number of possible local layer triples.

For a statistical examination of the energies of the layer triples, the Boltzmann distribution is used.

$$
\frac{N_{i}}{N_{j}}=\frac{g_{i}}{g_{j}} \mathrm{e}^{\frac{E_{i}-E_{j}}{k T}}
$$

Using the energies of the layer triples, first the relative occupancy values $N_{\mathrm{i}}$ and afterwards stacking probabilities $p_{i}$ for each local layer triple was calculated.

$$
p_{i}=\frac{N_{i}}{\sum_{i=1}^{n} N_{i}}
$$

As the basis we took the DFT-D optimised models LLLL with $Z=4$, LMLM with $Z=8$ and LLMM with $Z=16$. With these models a complete set of layer triples is given to describe all models containing
four double layers with only $L$ and $M$ double layers. On a given double layer the obtained stacking probabilities describe the chance to find a specific neighbouring double layer within a theoretical infinite disordered crystal. The resulting stacking probabilities are given in Table S4.

Table S4 Probabilities for the layer triples.

| Layer triple | $E_{\text {rel }}$ of the local layer triple / <br> $\left(\mathrm{kJ} \cdot \mathrm{mol}^{-1}\right)$ | Probability of the local layer <br> triple |
| :--- | :---: | :---: |
| LLL or MMM | 4.11 | 0.044 each |
| LLM or MML or MLL or LMM | 1.84 | 0.111 each |
| LML or MLM | 0.00 | 0.233 each |

These probabilities were used to construct a large model, containing 100 double layers. The lattice parameters of this model are $a=9.9069 \AA, b=4.7370 \AA, c=1638.2000 \AA, b=104.6810^{\circ}$ with the staking sequence

LMLMMLMMMLMLMMLMLLMLMLLMLMLMMLMLMMLMLLMLMLMMLLMLMLLLLMLMLLMLMLMM LMMLLMMLMLMLMLMLLMLMLMMLMMLMMMMLMMML

The simulated single-crystal diffraction pattern is shown in. The pattern shows sharp intensity maxima for reflexions with $h+k=2 n$ and strong diffuse streaks parallel to the $\boldsymbol{c}^{*}$ axis, through all reflexions with $h+k=2 n+1$, which is consistent with experimental observations.


Figure S1 Simulated single-crystal diffraction pattern of a model containing 100 double layers with a stacking sequence of $L$ and $M$ layers according to the stacking probabilities calculated of the DFT-D energies. Zone axis [100].

## References

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