

## STRUCTURAL SCIENCE CRYSTAL ENGINEERING MATERIALS

Volume 73 (2017)
Supporting information for article:

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## Electronic Supplementary Information

# Nature of $E_{2} X_{2} \sigma(4 c-6 e)$ of the $X--E-E--X$ type at naphthalene 1,8-positions and model, elucidated by X-ray crystallographic analysis and QC calculations with QTAIM approach 

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## QTAIM Dual Functional Analysis (QTAIM-DFA)

The bond critical point (BCP; *) is an important concept in QTAIM. The BCP of $(\omega, \sigma)=(3,-1)$ (Bader, 1990; Matta, 2007) is a point along the bond path (BP) at the interatomic surface, where charge density $\rho(\boldsymbol{r})$ reaches a minimum. It is donated by $\rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$. While the chemical bonds or interactions between A and B are denoted by A-B, which correspond to BPs between A and B in QTAIM, A-*-B emphasizes the presence of $\mathrm{BCP}(*)$ in $\mathrm{A}-\mathrm{B}$.

The sign of the Laplacian $\rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\left(\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\right)$ indicates that $\rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ is depleted or concentrated with respect to its surrounding, since $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ is the second derivative of $\rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) . \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ is locally depleted relative to the average distribution around $\boldsymbol{r}_{\mathrm{c}}$ if $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)>0$, but it is concentrated when $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)<0$. Total electron energy densities at BCPs $\left(H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\right)$ must be a more appropriate measure for weak interactions on the energy basis (Bader, 1990; Matta, 2007; Bader, 1985, 1990, 1991, 1998; Bader et al., 1983; Matta, \& Boyd, 2007; Biegler-König \& Schönbohm, 2002; Biegler-König et al., 1982, 2001; Tang et al., 1985; Nakanishi et al., 2007, 2008b, 2009, 2012; Nakanishi \& Hayashi, 2010a, 2010b). $H_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ are the sum of kinetic energy densities $\left(G_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)\right)$ and potential energy densities $\left(V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\right)$ at BCPs, as shown in Equation (S1). Electrons at BCPs are stabilized when $H_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)<0$, therefore, interactions exhibit the covalent nature in this region, whereas they exhibit no covalency if $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)>0$, due to the destabilization of electrons at BCPs under the conditions (Bader, 1990; Matta, 2007). Equation (S2) represents the relation between $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ and $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$, together with $G_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ and $V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$, which is closely related to the virial theorem.

$$
\begin{align*}
& H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)=G_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)  \tag{S1}\\
& \begin{aligned}
\left(\hbar^{2} / 8 m\right) V^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) & =H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2 \\
& =G_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)+V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2
\end{aligned} \tag{S2}
\end{align*}
$$

Interactions are classified by the signs of $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ and $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$. Interactions in the region of $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)<0$ are called shared-shell (SS) interactions and they are closed-shell (CS) interactions for $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)>0 . H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ must be negative when $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)<0$, since $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ are larger than $\left(\hbar^{2} / 8 m\right) \nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ by $V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$ with negative $V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ at all BCPs (Equation (S2)). Consequently, $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)<0$ and $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)<0$ for the SS interactions. The CS interactions are especially called pure CS interactions for $H_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)>0$ and $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)>0$, since electrons at BCPs are depleted and destabilized under the conditions (Bader, 1990). Electrons in the intermediate
region between SS and pure CS , which belong to CS , are locally depleted but stabilized at BCPs, since $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)>0$ but $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)<0$ (Bader, 1990). We call the interactions in this region regular CS (Nakanishi et al., 2008b, 2009; Nakanishi \& Hayashi, 2010a), when it is necessary to distinguish from pure CS. The role of $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ in the classification can be replaced by $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$, since $\left(\hbar^{2} / 8 m\right) \nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)=H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-$ $V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$ (Equation (S2)).

We proposed QTAIM-DFA by plotting $H_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ versus $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2\left(=\left(\hbar^{2} / 8 m\right) \nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\right)$ (Nakanishi et al., 2009), after the proposal of $H_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ versus $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ (Nakanishi et al., 2008b). Both axes in the plot of the former are given in energy unit, therefore, distances on the $(x, y)\left(=\left(H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2, H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\right)\right.$ plane can be expressed in the energy unit, which provides an analytical development. QTAIM-DFA can incorporate the classification of interactions by the signs of $\nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ and $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$. Scheme S1 summarizes the QTAIM-DFA treatment. Interactions of pure CS appear in the first quadrant, those of regular CS in the forth quadrant and SS interactions do in the third quadrant. No interactions appear in the second one.


Scheme S1. QTAIM-DFA: Plot of $H_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ versus $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$ for Weak to Strong Interactions

In our treatment, data for perturbed structures around fully optimized structures are also employed for the plots, together with the fully optimized ones (see Fig. S1) (Nakanishi et al., 2008b, 2009, 2012; Nakanishi \& Hayashi, 2010a, 2010b). We proposed the concept of the "dynamic nature of interaction" originated from the perturbed structures. The behavior of interactions at the fully optimized structures corresponds to "the static nature of interactions", whereas that containing perturbed structures exhibit the "dynamic nature of interaction" as explained below. The method to generate the perturbed structures is discussed later. Plots of $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ versus $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$ are analyzed employing the polar coordinate $(R, \theta)$ representation with $\left(\theta_{\mathrm{p}}, \kappa_{\mathrm{p}}\right)$ parameters (Nakanishi et al., 2009, 2012; Nakanishi \& Hayashi, 2010a, 2010b). Fig. S1 explains the treatment. $R$ in ( $R, \theta$ ) is defined by Equation (S3) and given in the energy unit. $R$ corresponds to the energy for an interaction at BCP. The plots show a spiral stream, as a whole. $\theta$ in $(R, \theta)$ defined by Equation (S4), measured from the $y$-axis, controls the spiral stream of the plot. Each plot for an interaction shows a specific curve, which provides important information of the interaction (see Fig. S1). The curve is expressed by $\theta_{\mathrm{p}}$ and $\kappa_{\mathrm{p}}$. While $\theta_{\mathrm{p}}$, defined by Equation (S5) and measured from the $y$-direction, corresponds to the tangent line of a plot, where $\theta_{\mathrm{p}}$ is calculated employing data of the perturbed structures with a fully-optimized structure and $\kappa_{\mathrm{p}}$ is the curvature of the plot (Equation (S6)). While $(R, \theta)$ correspond to the static nature, $\left(\theta_{\mathrm{p}}, \kappa_{\mathrm{p}}\right)$ represent the dynamic nature of interactions. We call $(R, \theta)$ and $\left(\theta_{\mathrm{p}}, \kappa_{\mathrm{p}}\right)$ QTAIM-DFA parameters, whereas $\rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right), \nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right), G_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right), V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right), H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ and $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ -
$V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$ belong to QTAIM functions. $k_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$, defined by Equation (S7), is an QTAIM function but it will be treated as if it were an QTAIM-DFA parameter, if suitable.


Figure S1. Polar $(R, \theta)$ coordinate representation of $H_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ versus $H_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{b}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$, with $\left(\theta_{\mathrm{p}}, \boldsymbol{\kappa}_{\mathrm{p}}\right)$ parameters.

$$
\begin{align*}
& R=\left(x^{2}+y^{2}\right)^{1 / 2}  \tag{S3}\\
& \theta=90^{\circ}-\tan ^{-1}(y / x)  \tag{S4}\\
& \theta_{\mathrm{p}}=90^{\circ}-\tan ^{-1}(\mathrm{~d} y / \mathrm{d} x)  \tag{S5}\\
& \kappa_{\mathrm{p}}=\left|\mathrm{d}^{2} y / \mathrm{d} x^{2}\right| /\left[1+(\mathrm{d} y / \mathrm{d} x)^{2}\right]^{3 / 2}  \tag{S6}\\
& k_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)=V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / G_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)  \tag{S7}\\
& \text { where }(x, y)=\left(H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2, H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\right)
\end{align*}
$$

## Criteria for Classification of Interactions: Behavior of Typical Interactions Elucidated by QTAIM-DFA

$H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ are plotted versus $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$ for typical interactions in vdW (van der Waals interactions), HB (hydrogen bonds), CT-MC (molecular complexes through charge transfer), $\mathrm{X}_{3}{ }^{-}$(trihalide ions), CT-TBP (trigonal bipyramidal adducts through charge-transfer), Cov-w (weak covalent bonds) and Cov-s (strong covalent bonds) (Nakanishi et al., 2008b, 2009, 2012; Nakanishi \& Hayashi, 2010a, 2010b). Rough criteria are obtained, after the analysis of the plots for the typical interactions according to Equations (S3)-(S7), by applying QTAIM-DFA. Scheme S2 shows the rough criteria, which are accomplished by the $\theta$ and $\theta_{\mathrm{p}}$ values, together with the values of $k_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$. The criteria will be employed to discuss the nature of interactions in question, as a reference.


Scheme S2. Rough classification of interactions by $\theta$ and $\theta_{\mathrm{p}}$, together with $k_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\left(=V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / G_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)\right)$.
(a)



$$
\left.C_{2 n}: r^{( }{ }^{1} \mathrm{H}-{ }^{8} \mathrm{H}\right)=2.484 \mathrm{~A}
$$

$$
\phi\left({ }^{1} \mathrm{H}^{1} \mathrm{C}^{8} \mathrm{C}^{8} \mathrm{H}\right)=0.0^{\circ}
$$

${ }^{1} \mathrm{H}--{ }^{8} \mathrm{H}$ : no interaction detected
(b)

(c)



$$
\left.C_{1}: r^{1} \mathrm{Br}-\mathrm{B}^{8} \mathrm{Br}\right)=3.275 \mathrm{~A}
$$

$$
\phi\left({ }^{1} \mathrm{Br}^{1} \mathrm{C}^{8} \mathrm{C}^{8} \mathrm{Br}\right)=19.8^{\circ}
$$

${ }^{1} \mathrm{Br}-{ }^{-}{ }^{8} \mathrm{Br}$ : typical-HB nature without covalency




$$
\left.C_{1}: r^{1} \mathrm{Br}-{ }^{8} \mathrm{Se}\right)=3.136 \mathrm{~A}
$$


$\phi\left({ }^{1} \mathrm{Br}^{1} \mathrm{C}^{8} \mathrm{C}^{8} \mathrm{Se}\right)=24.8^{\circ}\left(\angle \mathrm{BrSeC} \mathrm{Me}=172.6^{\circ}\right)$
${ }^{1} \mathrm{Br}-{ }^{8} \mathrm{Se}$ : typical-HB nature without covalency
Figure S2. Molecular graphs and contour plots of $\rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ on the optimized structures of $\mathrm{C}_{10} \mathrm{H}_{8}$ and $1-\mathrm{Br}-8-\mathrm{YC}_{10} \mathrm{H}_{6}(\mathrm{Y}=\mathrm{H}, \mathrm{Br}$, and SeMe$)$ with MP2/BSS-A. Colors and marks are the same as those in Fig. 4 in the text.

Table S1. QTAIM functions and parameters for ${ }^{1} \mathrm{H}-*-{ }_{-}^{8} \mathrm{Y},{ }^{1} \mathrm{X}-*-{ }^{8} \mathrm{Y}$, and ${ }^{1} \mathrm{X}-*-{ }^{8}$ Se at BCPs of $1-\mathrm{Br}-8-\mathrm{YC}_{10} \mathrm{H}_{6}(\mathrm{Y}=\mathrm{H}$, Br , and SeMe$)$ and $1-\mathrm{Cl}-8-\mathrm{YC}_{10} \mathrm{H}_{6}(\mathrm{Y}=\mathrm{SeMe})$, optimized with MP2/BSS-A..$^{(\mathrm{a})}$

| $\operatorname{Compd}\left({ }^{1} \mathrm{X}-{ }^{8} \mathrm{Y}\right)^{(\mathrm{b})}$ | $\rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ <br> $\left(e a_{0}{ }^{-3}\right)$ | $c \nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)^{(\mathrm{c})}$ <br> $(\mathrm{au})$ | $H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ <br> $(\mathrm{au})$ | $k_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)^{(\mathrm{d})}$ | $R$ <br> $(\mathrm{au})$ | $\theta$ <br> $\left({ }^{\circ}\right)$ | $\mathrm{Freq}^{(\mathrm{e})}$ <br> $\left(\mathrm{cm}^{-1}\right)$ | $k_{\mathrm{f}}^{(\mathrm{f})}$ <br> $(\mathrm{g})$ | $\theta_{\mathrm{p}}$ <br> $\left({ }^{\circ}\right)$ | $\kappa_{\mathrm{p}}$ <br> $\left(\mathrm{au}^{-1}\right)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{HBr}(\mathrm{H}-*-\mathrm{Br})$ | 0.0129 | 0.0061 | 0.0019 | -0.811 | 0.0064 | 72.4 | 176.8 | 0.160 | - | - |
| $\mathrm{Br}(\mathrm{Br}-*-\mathrm{Br})$ | 0.0168 | 0.0066 | 0.0011 | -0.907 | 0.0067 | 80.4 | 143.4 | 0.763 | 100.4 | 95.4 |
| $\mathrm{ClSeMe}(\mathrm{Se}-*-\mathrm{Cl})$ | 0.0279 | 0.0081 | -0.0017 | -1.095 | 0.0083 | 101.9 | 130.2 | 0.126 | 151.4 | 107 |
| $\mathrm{ClSeMe}(\mathrm{Se}-*-\mathrm{C})$ | 0.1165 | 0.0013 | -0.0612 | -1.960 | 0.0612 | 178.8 | 400.6 | 3.189 | 182.6 | 0.7 |
| $\mathrm{BrSeMe}(\mathrm{Se}-*-\mathrm{Br})$ | 0.0198 | 0.0070 | 0.0004 | -0.971 | 0.0070 | 86.8 | 134.3 | 0.161 | 121.0 | 170 |
| $\mathrm{BrSeMe}(\mathrm{Se}-*-\mathrm{C})$ | 0.1490 | -0.0186 | -0.0918 | -2.681 | 0.0937 | 191.5 | 620.4 | 1.121 | 191.3 | 1.1 |

(a) The $6-311+\mathrm{G}(3 \mathrm{df})$ basis set being employed for S and Se with the $6-311 \mathrm{G}(\mathrm{d})$ basis set for C and H ; (b)
$C_{1}$ symmetry; (c) $c \nabla^{2} \rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)=H_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)-V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / 2$, where $c=\hbar^{2} / 8 m$; (d) $k_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)=V_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) / G_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right) ;$ (e) Corresponding to the interaction in question. Symmetric and anti-symmetric modes being employed for ${ }^{\mathrm{A}} \mathrm{E}-*_{-}{ }^{\mathrm{A}} \mathrm{E}$ and ${ }^{\mathrm{A}} \mathrm{E}-*-{ }_{-}^{\mathrm{B}} \mathrm{E}$, respectively; (f) Force constant for v ; (g) mdyn $\AA^{-1}$.
(a)

(b)


Figure S3. Structure of 1, determined by the X-ray crystallographic analysis. Thermal ellipsoids are drawn at $50 \%$ probability.
(a)

(b)


Figure S4. Structure of 3, determined by the X-ray crystallographic analysis. Thermal ellipsoids are drawn at $50 \%$ probability.

Table S2. Crystallographic data for 1, 3, and 4

|  | $\mathbf{1}$ | $\mathbf{3}$ | $\mathbf{4}$ |
| :--- | :---: | :---: | :---: |
| Empirical formula | $\mathrm{C}_{20} \mathrm{H}_{12} \mathrm{Cl}_{2} \mathrm{~S}_{2}$ | $\mathrm{C}_{20} \mathrm{H}_{12} \mathrm{Cl}_{2} \mathrm{Se}_{2}$ | $\mathrm{C}_{20} \mathrm{H}_{12} \mathrm{Br}_{2} \mathrm{Se}_{2}$ |
| Formula weight | 387.32 | 481.12 | 570.04 |
| Temperature $(\mathrm{K})$ | $103(2)$ | $103(2)$ | $103(2)$ |
| Crystal system | orthorhombic | orthorhombic | Triclinic |
| Space group | $\mathrm{Pca} 2_{1}(\# 29)$ | $\mathrm{Pca} 2_{1}(\# 29)$ | $\mathrm{P}-1(\# 2)$ |
| Unit cell dimensions |  |  |  |
| $a(\AA)$ | $7.824(2)$ | $7.89330(10)$ | $7.83940(10)$ |
| $b(\AA)$ | $28.782(8)$ | $29.1713(4)$ | $8.0986(2)$ |
| $c(\AA)$ | $14.350(4)$ | $14.4594(2)$ | $15.0650(4)$ |
| $\alpha($ deg $)$ | 90.00 | 90.00 | $90.9410(10)$ |
| $\beta($ deg $)$ | 90.00 | 90.00 | $101.8880(10)$ |
| $\gamma($ deg $)$ | 90.00 | 90.00 | $111.0930(10)$ |
| Volume $\left(\AA^{3}\right)$ | $3231.7(15)$ | $3329.39(8)$ | $868.92(3)$ |
| $Z$ | 8 | 8 | 2 |
| Dcalcd $(\mathrm{g}$ cm |  | 1.920 | 2.179 |
| $\mathrm{~F}(000)$ | 1.592 | 1872 | 540 |
| Reflections observed $[\mathrm{I}>2 \sigma(\mathrm{I})]$ | 1584 | 6129 | 3813 |
| Parameters | 5988 | 433 | 217 |
| $R_{1}[\mathrm{I}>2 \sigma(\mathrm{I})]$ | 529 | 0.024 | 0.0391 |
| $R_{1}[$ all data $]$ | 0.020 | 0.026 | 0.0432 |
| $\omega R_{2}[\mathrm{I}>2 \sigma(\mathrm{I})]$ | 0.020 | 0.059 | 0.0788 |
| $\omega R_{2}$ [all data] | 0.052 | 0.060 | 0.0805 |
| Goodness-of-fit on $F^{2}$ | 0.052 | 1.058 | 1.198 |

Table S3. Structural parameters evaluated for model $\mathbf{A}[(\mathrm{S}, \mathrm{Cl}),(\mathrm{S}, \mathrm{Br}),(\mathrm{Se}, \mathrm{Cl}),(\mathrm{Se}, \mathrm{Br})]\left(C_{2}\right)$ with MP2/BSS-C. ${ }^{(\text {a })}$

| Species | $r_{0}(\mathrm{E}, \mathrm{E})$ <br> $(\AA)$ | $r_{0}(\mathrm{E}, \mathrm{X})$ <br> $(\AA)$ | $\Delta r_{0}(\mathrm{E}, \mathrm{X})^{(\mathrm{b})}$ <br> $(\AA)$ | $\angle \mathrm{H}^{\mathrm{A}} \mathrm{E}^{\mathrm{A}^{\top} \mathrm{E}}$ <br> $\left({ }^{\circ}\right)$ | $\angle^{\mathrm{B}} \mathrm{X}^{\mathrm{A}} \mathrm{E}^{\Lambda} \mathrm{E}$ <br> $\left({ }^{\circ}\right)$ | $\phi_{1}^{(\mathrm{c})}$ <br> $\left({ }^{( }\right)$ | $\phi_{2^{(\mathrm{d})}}$ <br> $\left({ }^{\circ}\right)$ | $\Delta E_{\mathrm{ES}}$ <br> $\left(\mathrm{kJ} \mathrm{mol}^{-1}\right)$ | $\Delta E_{\mathrm{ZP}}$ <br> $\left(\mathrm{kJ} \mathrm{mol}^{-1}\right)$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $(\mathrm{S}, \mathrm{Cl})$ | 2.0559 | 3.3838 | -0.1662 | 98.9 | 170.4 | -101.8 | -113.2 | -26.5 | -22.2 |
| $(\mathrm{~S}, \mathrm{Br})$ | 2.0572 | 3.4947 | -0.1533 | 98.8 | 171.3 | -106.1 | -121.7 | -26.7 | -22.6 |
| $(\mathrm{Se}, \mathrm{Cl})$ | 2.3220 | 3.4617 | -0.1883 | 96.7 | 161.4 | -130.2 | -169.6 | -26.9 | -23.6 |
| $(\mathrm{Se}, \mathrm{Br})$ | 2.3242 | 3.5805 | -0.1695 | 96.6 | 160.9 | -135.6 | 179.6 | -27.6 | -24.3 |

(a) BSS-C: the $6-311+\mathrm{G}(3 \mathrm{df})$ basis sets being employed for S and Se with the $6-311 \mathrm{G}(\mathrm{d}, \mathrm{p})$ basis sets for C and H ; (b) $\left.\Delta r_{0}\left({ }^{\mathrm{A}} \mathrm{E},{ }^{\mathrm{B}} \mathrm{X}\right)=r_{\mathrm{o}}{ }^{\mathrm{A}} \mathrm{E},{ }^{\mathrm{B}} \mathrm{X}\right)-\Sigma r_{\mathrm{vdW}}\left({ }^{\mathrm{A}} \mathrm{E},{ }^{\mathrm{B}} \mathrm{X}\right)$, where $r_{\mathrm{vdw}}(\mathrm{S})=1.80 \AA, r_{\mathrm{vdW}}(\mathrm{Se})=1.90 \AA, r_{\mathrm{vdw}}(\mathrm{Cl})$ $=1.75 \AA$, and $r_{\mathrm{vdW}}(\mathrm{Br})=1.85 \AA$, (Bondi, 1964); (c) $\phi_{1}=\phi\left(\mathrm{H}^{\mathrm{A}} \mathrm{E}^{A} \mathrm{EH}\right)$; (d) $\phi_{2}=\phi\left(\mathrm{H}^{\mathrm{A}} \mathrm{E}^{\mathrm{B}} \mathrm{XMe}\right)$.


Figure S5. Molecular graphs for models $\mathbf{A}[(\mathrm{E}, \mathrm{X})=(\mathrm{S}, \mathrm{Cl}),(\mathrm{S}, \mathrm{Br}),(\mathrm{Se}, \mathrm{Cl}),(\mathrm{Se}, \mathrm{Br})]$. BCPs (bond critical points) are denoted by red dots, RCPs (ring critical points) by yellow dots, CCPs (cage critical points) by green dots, and BPs (bond paths) by pink lines. Carbon atoms are in black, hydrogen atoms are in gray, and selenium atoms in pink.


Figure S6. Contour plots of $\rho_{\mathrm{b}}\left(\boldsymbol{r}_{\mathrm{c}}\right)$ for models $\mathbf{A}[(\mathrm{E}, \mathrm{X})=(\mathrm{S}, \mathrm{Cl}),(\mathrm{S}, \mathrm{Br}),(\mathrm{Se}, \mathrm{Cl}),(\mathrm{Se}, \mathrm{Br})]$. BCPs on the plane are shown by red dots, those outside of the plane in dark pink dots, RCPs on and outside the plane by blue squares and light blue ones, respectively. CCPs by green squares, and BPs on the plane by black lines and those outside of the plane are by gray lines. Atoms on and outside the plane are by black dots and gray ones, respectively. The contours $\left(e \mathrm{a}_{0}{ }^{-3}\right)$ are at $2^{l}(l= \pm 8, \pm 7, \ldots, 0)$ with 0.0047 (heavy line).


Figure S7. Negative Laplacians for $\mathbf{1 - 4}$ drawn with M06-2X/BSS-A//MP2/BSS-A and model A (S, Cl)( $\mathrm{Se}, \mathrm{Br}$ ) drawn with MP2/BSS-C//MP2/BSS-C, similarly to the case of Fig. 4 in the text. Blue and red lines correspond to the positive and negative values, respectively.


Figure S8. Trajectory plots for $\mathbf{1 - 4}$ drawn with M06-2X/BSS-A//MP2/BSS-A and model A (S, Cl)-(Se, Br ) drawn with MP2/BSS-C//MP2/BSS-C, similarly to the case of Fig. 4 in the text. Colors and marks are the same as those in Fig. 4.

Table S4. Results of NBO analysis for the ${ }^{1} \mathrm{E}-\mathrm{-}^{8} \mathrm{X}$ interactions in $\mathbf{1 - 4}$ with M06-2X/BSS-A//MP2/BSS-A and models $\mathbf{A}[(\mathrm{S}, \mathrm{Cl}),(\mathrm{S}, \mathrm{Br}),(\mathrm{Se}, \mathrm{Cl})$, and $(\mathrm{Se}, \mathrm{Br})]$ with MP2/BSS-C//MP2/BSS-C.

| Compound$\left({ }^{1} \mathrm{E},{ }^{8} \mathrm{X}\right)$ | $\begin{gathered} E(2)^{(\mathrm{a}, \mathrm{~b})} \\ ([\mathrm{e}]) \end{gathered}$ | $\begin{gathered} E(2)^{(\mathrm{a}, \mathrm{~b})} \\ ([\mathrm{f}]) \end{gathered}$ | $[E(i)-E(j)]^{(c)} F(i, j){ }^{(d)}$ |  | Compound$\left({ }^{1} \mathrm{E},{ }^{8} \mathrm{X}\right)$ | $\left.E(2)^{(\mathrm{a}, \mathrm{b})} E(2)^{(\mathrm{a}, \mathrm{b})}[E(i)-E(j)]^{(\mathrm{c})} F(i, j)\right)^{(\mathrm{d})}$ |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | (au) | (au) |  | ([e]) | ([f]) | (au) | (au) |
| calculated |  |  |  |  |  |  |  |  |  |
| $1(\mathrm{~S}, \mathrm{Cl})\left(C_{2}\right)$ | 4.61 | 19.3 | 0.51 | 0.043 | $2(\mathrm{~S}, \mathrm{Br})\left(C_{2}\right)$ | 4.42 | 18.5 | 0.48 | 0.041 |
| $\mathbf{3}(\mathrm{Se}, \mathrm{Cl})\left(C_{2}\right.$ observed |  | 28.1 | 0.47 | 0.050 | $4(\mathrm{Se}, \mathrm{Br})\left(C_{2}\right)$ | 6.66 | 27.9 | 0.42 | 0.047 |
| $1(\mathrm{~S}, \mathrm{Cl})^{(\mathrm{g})}$ | $4.88{ }^{(\mathrm{h})}$ | $20.4{ }^{(\mathrm{h})}$ | $0.51{ }^{\text {(h) }}$ | $0.044^{(\mathrm{h})}$ |  |  |  |  |  |
| $3(\mathrm{Se}, \mathrm{Cl})^{(\mathrm{g})}$ | $7.04{ }^{(\mathrm{h})}$ | $29.4{ }^{(\mathrm{h})}$ | $0.46{ }^{[\mathrm{h}]}$ | $0.051{ }^{(\mathrm{h})}$ | $4(\mathrm{Se}, \mathrm{Br})$ | $8.59^{(\mathrm{h})}$ | $35.9{ }^{\text {(h) }}$ | $0.42{ }^{\text {(h) }}$ | $0.054^{(\mathrm{h})}$ |
| model A |  |  |  |  |  |  |  |  |  |
| $(\mathrm{S}, \mathrm{Cl})\left(C_{2}\right)$ | 1.64 | 6.9 | 0.49 | 0.025 | $(\mathrm{S}, \mathrm{Br})\left(C_{2}\right)$ | 1.88 | 7.9 | 0.46 | 0.026 |
| $(\mathrm{Se}, \mathrm{Cl})\left(C_{2}\right)$ | 2.22 | 9.3 | 0.43 | 0.028 | $(\mathrm{Se}, \mathrm{Br})\left(C_{2}\right)$ | 2.67 | 11.2 | 0.40 | 0.029 |

(a) Second-order perturbation energy; (b) Only one side of energy is shown; (c) Donor orbital of NBO(i) is $n_{p}\left({ }^{8} \mathrm{X}\right.$ or $\left.{ }^{\mathrm{B}} \mathrm{X}\right)$ and acceptor orbital of NBO (j) corresponds to $\sigma^{*}\left({ }^{1} \mathrm{E}-{ }^{1}{ }^{\mathrm{E}}\right.$ or ${ }^{\mathrm{A}} \mathrm{E}-{ }^{{ }^{\prime}} \mathrm{E}$ ); (d) Fock matrix; (e) In kcal $\mathrm{mol}^{-1}$; (f) In $\mathrm{kJ} \mathrm{mol}{ }^{-1}$; (g) The crystals contain two independent molecules in a unit cell; (h) Averaged value.


Figure S9. Plot of $\Delta E_{\mathrm{ES}}$ and $\Delta E_{\mathrm{ZP}}$ for model $\mathbf{A}$.


Figure S10. Plot of $2 E(2)$ versus $\Delta E_{\mathrm{ES}}$ for model $\mathbf{A}$.

Table S5. $r_{\mathrm{BP}}$ and $R_{\mathrm{SL}}$ values for the ${ }^{\mathrm{B}} \mathrm{X}---{ }^{\mathrm{A}} \mathrm{E}-{ }^{\mathrm{A}} \mathrm{E}--{ }^{\mathrm{B}} \mathrm{X}$ interactions in compounds $\mathbf{1 - 4}$ with MP2/BSS-A and model A with MP2/BSS-C. ${ }^{(\text {a) }}$

| $\begin{aligned} & \text { Species } \\ & { }^{\mathrm{B}} \mathrm{X}--\mathrm{A}^{\mathrm{E}} \mathrm{E}-{ }^{\mathrm{A}} \mathrm{E}--\mathrm{B}^{\mathrm{B}} \mathrm{X} \end{aligned}$ | $\begin{gathered} R_{\mathrm{SL}}\left({ }^{8} \mathrm{X},{ }^{1}{ }^{1} \mathrm{E}\right) \\ \hline \end{gathered}$ | $\begin{gathered} R_{\mathrm{SL}}\left({ }^{\left.\mathrm{I} \mathrm{E},{ }^{\prime}{ }^{\prime} \mathrm{E}\right)}\right. \\ \hline \end{gathered}$ | $\begin{gathered} r_{\mathrm{BP}}\left({ }^{8} \mathrm{X},{ }^{\mathrm{I}} \mathrm{E}\right) \\ \hline \end{gathered}$ | $r_{\mathrm{BP}}\left({ }^{1} \mathrm{E},{ }^{1}{ }^{\top} \mathrm{E}\right)$ <br> (Å) | $\begin{array}{r} r_{\mathrm{BP}}\left(\begin{array}{l} 8 \\ (\mathrm{X} \\ (\mathrm{A} \end{array}\right) \end{array}$ | $\begin{array}{r} r_{\mathrm{BP}}\left({ }^{(1 \mathrm{E},},\right. \\ (\AA) \\ \hline \end{array}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Compounds 1-4 |  |  |  |  |  |  |
| ${ }^{8} \mathrm{Cl}-*-{ }^{1} \mathrm{~S}-*-{ }^{1} \mathrm{~S}-*-{ }^{8} \mathrm{Cl}$ in $\mathbf{1}$ | 2.9340 | 2.0311 | 2.9481 | 2.0324 | 0.0142 | 0.0013 |
| ${ }^{8} \mathrm{Br}-*_{-}{ }^{1} \mathrm{~S}-*-{ }^{1} \mathrm{~S}-*-{ }^{8} \mathrm{Br}$ in 2 | 3.0392 | 2.0330 | 3.0526 | 2.0344 | 0.0134 | 0.0015 |
| ${ }^{8} \mathrm{Cl}-*-{ }^{1} \mathrm{Se}-*-{ }^{1} \mathrm{Se}-*-{ }^{8} \mathrm{Cl}$ in 3 | 32.9774 | 2.3010 | 2.9824 | 2.3024 | 0.0050 | 0.0014 |
| ${ }^{8} \mathrm{Br}-*-{ }^{1} \mathrm{Se}-\mathrm{F}^{1}{ }^{\prime} \mathrm{Se}-*-{ }^{8} \mathrm{Br}$ in 4 | 43.0837 | 2.3072 | 3.0887 | 2.3085 | 0.0050 | 0.0013 |
| Observed |  |  |  |  |  |  |
| ${ }^{8} \mathrm{Cl}-*-{ }^{1} \mathrm{~S}-*-{ }^{1} \mathrm{~S}-*_{-}{ }^{\prime} \mathrm{Cl}$ in 1 | 2.9493 | 2.0461 | 2.9630 | 2.0474 | 0.0138 | 0.0013 |
| ${ }^{8} \mathrm{Cl}-*-{ }^{1} \mathrm{Se}-*-{ }^{1} \mathrm{Se}-*-{ }^{8} \mathrm{Cl}$ in $\mathbf{3}$ | 32.9708 | 2.3249 | 2.9754 | 2.3264 | 0.0046 | 0.0015 |
| ${ }^{8} \mathrm{Br}-*-{ }^{1} \mathrm{Se}-{ }^{1}{ }^{1} \mathrm{Se}-*_{-}{ }^{\prime} \mathrm{Br}$ in 4 | 43.0740 | 2.3354 | 3.0791 | 2.3369 | 0.0051 | 0.0015 |
| model A |  |  |  |  |  |  |
| ${ }^{\mathrm{B}} \mathrm{Cl}-*-{ }^{\text {A }}$ S-*- ${ }^{\text {A }} \mathrm{S}-*-{ }^{\text {B }}$ ' Cl | 3.3838 | 2.0559 | 3.3943 | 2.0576 | 0.0105 | 0.0017 |
| ${ }^{\mathrm{B}} \mathrm{Br}-*_{-}{ }^{\mathrm{A}} \mathrm{S}-*_{-}{ }^{\mathrm{A}} \mathrm{S}-{ }^{\text {- }}{ }^{\mathrm{B}}{ }^{\text {' }} \mathrm{Br}$ | 3.4947 | 2.0572 | 3.5052 | 2.0589 | 0.0105 | 0.0017 |
|  | 3.4617 | 2.3220 | 3.4682 | 2.3226 | 0.0065 | 0.0006 |
|  | 3.5805 | 2.3242 | 3.5871 | 2.3248 | 0.0066 | 0.0006 |

(a) BSS-A: the $6-311+\mathrm{G}(3 \mathrm{dff})$ basis sets being employed for S and Se with the $6-311 \mathrm{G}(\mathrm{d})$ basis sets for C and H. BSS-C: the $6-311+\mathrm{G}(3 \mathrm{df})$ basis sets being employed for S and Se with the $6-311 \mathrm{G}(\mathrm{d}, \mathrm{p})$ basis sets for C and H ; (b) $\Delta r_{\mathrm{BP}}\left({ }^{8} \mathrm{X},{ }^{1} \mathrm{E}\right)=r_{\mathrm{BP}}\left({ }^{8} \mathrm{X},{ }^{1} \mathrm{E}\right)-R_{\mathrm{SL}}\left({ }^{8} \mathrm{X},{ }^{\mathrm{C}} \mathrm{E}\right) ;(\mathrm{c}) \Delta r_{\mathrm{BP}}\left({ }^{1} \mathrm{E},{ }^{1} \mathrm{E}\right)=r_{\mathrm{BP}}\left({ }^{1} \mathrm{E},{ }^{1} \mathrm{E}\right)-R_{\mathrm{SL}}\left({ }^{1} \mathrm{E},{ }^{1} \mathrm{E}\right)$.


Figure S11. Plots of $r_{\mathrm{BP}}$ versus $R_{\mathrm{SL}}$ for the interactions in Compounds $\mathbf{1 - 4}$ and models $\mathbf{A}$. Correlation is very good, which are shown in the figure.

