

## SUPPLEMENTARY DOCUMENT

Electronically driven structural transitions in  $A_{10}(\text{PO}_4)_6\text{F}_2$  apatites (A=Ca, Sr, Pb, Cd, and Hg)

Prasanna V. Balachandran<sup>1,\*</sup>, Krishna Rajan<sup>2</sup>, and James M. Rondinelli<sup>1</sup>

<sup>1</sup>Department of Materials Science and Engineering, Drexel University, Philadelphia, PA 19104, USA.

<sup>2</sup>Department of Materials Science and Engineering, Iowa State University, Ames, IA 50011, USA.

\*Corresponding author email address: [prasven@coe.drexel.edu](mailto:prasven@coe.drexel.edu)

### S1.0 DENSITY FUNCTIONAL THEORY

In Table S1, the electronic configurations of the pseudopotentials are given. The input files for the scalar relativistic pseudopotentials were taken from the PSLIBRARY project [1] and the pseudopotentials were generated using the `ld1.x` routine in the Quantum ESPRESSO package. In our frozen phonon calculations, the atomic displacement amplitudes were set at 0.01Å.

**Table S1.** Valence electron configurations used in our pseudopotentials.

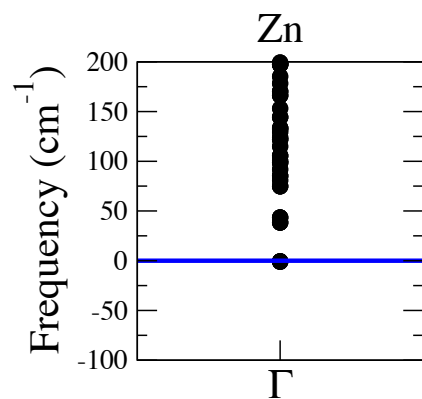
Element	Valence electron configuration
Ca	$3s^2 3p^6 4s^2$
Sr	$4s^2 4p^6 5s^2 5p^0$
Pb	$5d^{10} 6s^2 6p^2$
Cd	$4d^{9.5} 5s^2 5p^{0.5}$
Hg	$5d^{10} 6s^2 6p^0$
Zn	$3d^{10} 4s^2 4p^0$
P	$3s^2 3p^3$
O	$2s^2 2p^4$
F	$2s^2 2p^5$

### S2.0 LATTICE DYNAMICAL CALCULATIONS FOR $\text{Zn}_{10}(\text{PO}_4)_6\text{F}_2$

In Figure S1, we show the low-energy zone center phonons for  $\text{Zn}_{10}(\text{PO}_4)_6\text{F}_2$  in the aristotype  $P6_3/m$  structure. Absence of phonons with negative or imaginary frequencies indicates that the aristotype structure is dynamically stable.

### S3.0 CRYSTAL STRUCTURES

The ground state and high symmetry structures are attached separately in \*.CIF format.



**Figure S1** Frequencies ( $\omega$ ) of the low energy zone-center phonons for  $\text{Zn}_{10}(\text{PO}_4)_6\text{F}_2$  in the aristotype  $P6_3/m$  structure.

## REFERENCE

S1. <http://qe-forge.org/gf/project/pslibrary/> (v. 0.2.5)