

# Modulated crystal structure of Pr<sub>2</sub>SbO<sub>2</sub>

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## Supplementary Materials

$\text{Pr}_2\text{SbO}_2$   
idealized structure

$I4/mmm$   $I4/m$   $2/m$   $2/m$  (no. 139)

$$\begin{array}{l} | \\ a = 13.7017 \text{ \AA} \\ b = c = 3.9957 \text{ \AA} \\ | \\ t2 \end{array}$$

$Immm$   $I2/m$   $2/m$   $2/m$  (no. 71)

$$| \\ t2 \\ |$$

$Pmmm$   $P2/m$   $2/m$   $2/m$  (no. 47)

$$| \\ i2 \\ |$$

$$\begin{array}{l} a, 2b, c \\ | \\ a = 13.7017 \text{ \AA} \\ b = 7.9914 \text{ \AA} \\ c = 3.9957 \text{ \AA} \end{array}$$

$Pmmm$   $P2/m$   $2/m$   $2/m$  (no. 47)

$\text{Pr}_2\text{SbO}_2$   
Motif 1

| Sb: 2a<br>$4/mmm$ | Pr: 4e<br>$4mm$ | O: 4d<br>$\bar{4}m2$ |
|-------------------|-----------------|----------------------|
| 0                 | 0.3362          | $\frac{1}{4}$        |
| 0                 | 0               | $\frac{1}{2}$        |
| 0                 | 0               | 0                    |

| 2a<br>$mmm$ | 4i<br>$mm2$ | 4j<br>$mm2$   |
|-------------|-------------|---------------|
| 0           | 0.3362      | 0.25          |
| 0           | 0           | $\frac{1}{2}$ |
| 0           | 0           | 0             |

| 1a<br>$mmm$ | 1h<br>$mmm$   | 2q<br>$mm2$ | 2t<br>$mm2$   | 2s<br>$mm2$   | 2r<br>$mm2$   |
|-------------|---------------|-------------|---------------|---------------|---------------|
| 0           | $\frac{1}{2}$ | 0.3362      | 0.3362        | 0.25          | 0.25          |
| 0           | $\frac{1}{2}$ | 0           | $\frac{1}{2}$ | $\frac{1}{2}$ | 0             |
| 0           | $\frac{1}{2}$ | 0           | $\frac{1}{2}$ | 0             | $\frac{1}{2}$ |

| 2i<br>$2mm$ | 2j<br>$2mm$   | 2q<br>$mm2$ | 2s<br>$mm2$   | 4x<br>.m.     | 4w<br>.m. | 2t<br>$mm2$   | 2r<br>$mm2$   |
|-------------|---------------|-------------|---------------|---------------|-----------|---------------|---------------|
| 0           | $\frac{1}{2}$ | 0.3362      | 0.3362        | 0.3362        | 0.25      | 0.25          | 0.25          |
| 0.18        | 0.18          | 0           | $\frac{1}{2}$ | 0.25          | 0.25      | $\frac{1}{2}$ | 0             |
| 0           | 0             | 0           | 0             | $\frac{1}{2}$ | 0         | $\frac{1}{2}$ | $\frac{1}{2}$ |

Fig. 1. Group-subgroup relations between idealized Structure of  $\text{Pr}_2\text{SbO}_2$  (which is identical to  $\text{Pr}_2\text{BiO}_2$ ) and structure with ordered Sb-dumbbells (motif 1, Fig. 12b).

$\text{Pr}_2\text{SbO}_2$   
idealized structure

$I4/mmm$   $I4/m$   $2/m$   $2/m$  (no. 139)

$$a = 13.7017 \text{ \AA}$$

$$b = c = 3.9957 \text{ \AA}$$

$t_2$

$P\bar{4}$   $P\bar{4}11$  (no. 81)

$t_2$

$\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$

$P4_2/n$   $P4_2/n11$  (no. 86)

Origin choice 2

$i5$

$a-2b, 2a+b, c$

$\downarrow$

$P4_2/n$   $P4_2/n11$  (no. 86)

Origin choice 2

$t_2$

$\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$

$\downarrow$

$I4/m$   $I4/m11$  (no. 87)

$\text{Pr}_2\text{SbO}_2$   
Motif 3

| Sb: $2a$<br>$4/mmm$ | Pr: $4e$<br>$4mm$ | O: $4d$<br>$\bar{4}m2$ |
|---------------------|-------------------|------------------------|
| 0                   | 0.3362            | $\frac{1}{4}$          |
| 0                   | 0                 | $\frac{1}{2}$          |
| 0                   | 0                 | 0                      |

| $2a$<br>$4/m$ | $4e$<br>4.. | $4d$<br>$\bar{4}..$ |
|---------------|-------------|---------------------|
| 0             | 0.3362      | $\frac{1}{4}$       |
| 0             | 0           | $\frac{1}{2}$       |
| 0             | 0           | 0                   |

| $2a$<br>$\bar{4}..$ | $4f$<br>2..   | $4e$<br>2..   |
|---------------------|---------------|---------------|
| $\frac{3}{4}$       | 0.0862        | 0.0           |
| $\frac{3}{4}$       | $\frac{3}{4}$ | $\frac{3}{4}$ |
| $\frac{3}{4}$       | $\frac{3}{4}$ | $\frac{1}{4}$ |

| $2b$<br>$\bar{4}..$ | $8g$<br>1 | $8g$<br>1 | $8g$<br>1 | $4f$<br>2..   | $8g$<br>1 | $8g$<br>1 | $4e$<br>2..   |
|---------------------|-----------|-----------|-----------|---------------|-----------|-----------|---------------|
| $\frac{1}{4}$       | 0.75      | 0.0862    | 0.0862    | 0.9138        | 0         | 0.5       | 0             |
| $\frac{3}{4}$       | 0.85      | 0.85      | 0.05      | $\frac{3}{4}$ | 0.15      | 0.35      | $\frac{3}{4}$ |
| $\frac{3}{4}$       | 0.45      | 0.45      | 0.85      | $\frac{3}{4}$ | 0.05      | 0.45      | $\frac{1}{4}$ |
| $1a$<br>$\bar{4}..$ | $4h$<br>1 | $4h$<br>1 | $4h$<br>1 | $2e$<br>2..   | $4h$<br>1 | $4h$<br>1 | $2g$<br>2..   |
| $\frac{1}{2}$       | 0.0       | 0.8362    | 0.8362    | 0.1638        | 0.25      | 0.25      | 0.25          |
| 0                   | 0.07      | 0.6       | 0.8       | 0             | 0.3       | 0.1       | $\frac{1}{2}$ |
| 0                   | 0.645     | 0.2       | 0.6       | 0             | 0.6       | 0.2       | 0             |
| $1b$<br>$\bar{4}..$ | $4h$<br>1 | $4h$<br>1 | $4h$<br>1 | $2f$<br>2..   | $4h$<br>1 | $4h$<br>1 | $2g$<br>2..   |
| 0                   | 0.5       | 0.3362    | 0.3362    | 0.6638        | 0.75      | 0.75      | 0.75          |
| $\frac{1}{2}$       | 0.57      | 0.7       | 0.1       | $\frac{1}{2}$ | 0.9       | 0.7       | $\frac{1}{2}$ |
| $\frac{1}{2}$       | 0.145     | 0.9       | 0.7       | $\frac{1}{2}$ | 0.8       | 0.4       | 0             |

Fig. 2. Group-subgroup relations between idealized Structure of  $\text{Pr}_2\text{SbO}_2$  (which is identical to  $\text{Pr}_2\text{BiO}_2$ ) and structure with ordered Sb-dumbbells and isolate Sb-atoms (motif 3, Fig. 12d).

$\text{Pr}_2\text{SbO}_2$   
idealized structure

$I4/mmm$   $I$   $4/m$   $2/m$   $2/m$  (no. 139)

$$a = 13.7017 \text{ \AA}$$

$$b = c = 3.9957 \text{ \AA}$$

$t_2$

$Immm$   $I$   $2/m$   $2/m$   $2/m$  (no. 71)

$t_2$

$Pmmm$   $P$   $2/m$   $2/m$   $2/m$  (no. 47)

$t_2$

$P2/m$   $P$   $1$   $2/m$   $1$  (no. 10)

$t_2$

$P\bar{1}$   $P\bar{1}$  (no. 2)

$t_2$

|                     |                   |                        |
|---------------------|-------------------|------------------------|
| Sb: $2a$<br>$4/mmm$ | Pr: $4e$<br>$4mm$ | O: $4d$<br>$\bar{4}m2$ |
| 0                   | 0.3362            | $\frac{1}{4}$          |
| 0                   | 0                 | $\frac{1}{2}$          |
| 0                   | 0                 | 0                      |

|               |               |               |
|---------------|---------------|---------------|
| $2a$<br>$mmm$ | $4i$<br>$mm2$ | $4j$<br>$mm2$ |
| 0             | 0.3362        | 0.25          |
| 0             | 0             | $\frac{1}{2}$ |
| 0             | 0             | 0             |

|               |               |               |               |               |               |
|---------------|---------------|---------------|---------------|---------------|---------------|
| $1a$<br>$mmm$ | $1h$<br>$mmm$ | $2q$<br>$mm2$ | $2t$<br>$mm2$ | $2s$<br>$mm2$ | $2r$<br>$mm2$ |
| 0             | $\frac{1}{2}$ | 0.3362        | 0.3362        | 0.25          | 0.25          |
| 0             | $\frac{1}{2}$ | 0             | $\frac{1}{2}$ | $\frac{1}{2}$ | 0             |
| 0             | $\frac{1}{2}$ | 0             | $\frac{1}{2}$ | 0             | $\frac{1}{2}$ |

|               |               |             |               |               |               |
|---------------|---------------|-------------|---------------|---------------|---------------|
| $1a$<br>$2/m$ | $1h$<br>$2/m$ | $2m$<br>$m$ | $2n$<br>$m$   | $2n$<br>$m$   | $2m$<br>$m$   |
| 0             | $\frac{1}{2}$ | 0.3362      | 0.3362        | 0.25          | 0.25          |
| 0             | $\frac{1}{2}$ | 0           | $\frac{1}{2}$ | $\frac{1}{2}$ | 0             |
| 0             | $\frac{1}{2}$ | 0           | $\frac{1}{2}$ | 0             | $\frac{1}{2}$ |

|                   |                   |           |               |               |               |
|-------------------|-------------------|-----------|---------------|---------------|---------------|
| $1a$<br>$\bar{1}$ | $1h$<br>$\bar{1}$ | $2i$<br>1 | $2i$<br>1     | $2i$<br>1     | $2i$<br>1     |
| 0                 | $\frac{1}{2}$     | 0.3362    | 0.3362        | 0.25          | 0.25          |
| 0                 | $\frac{1}{2}$     | 0         | $\frac{1}{2}$ | $\frac{1}{2}$ | 0             |
| 0                 | $\frac{1}{2}$     | 0         | $\frac{1}{2}$ | 0             | $\frac{1}{2}$ |

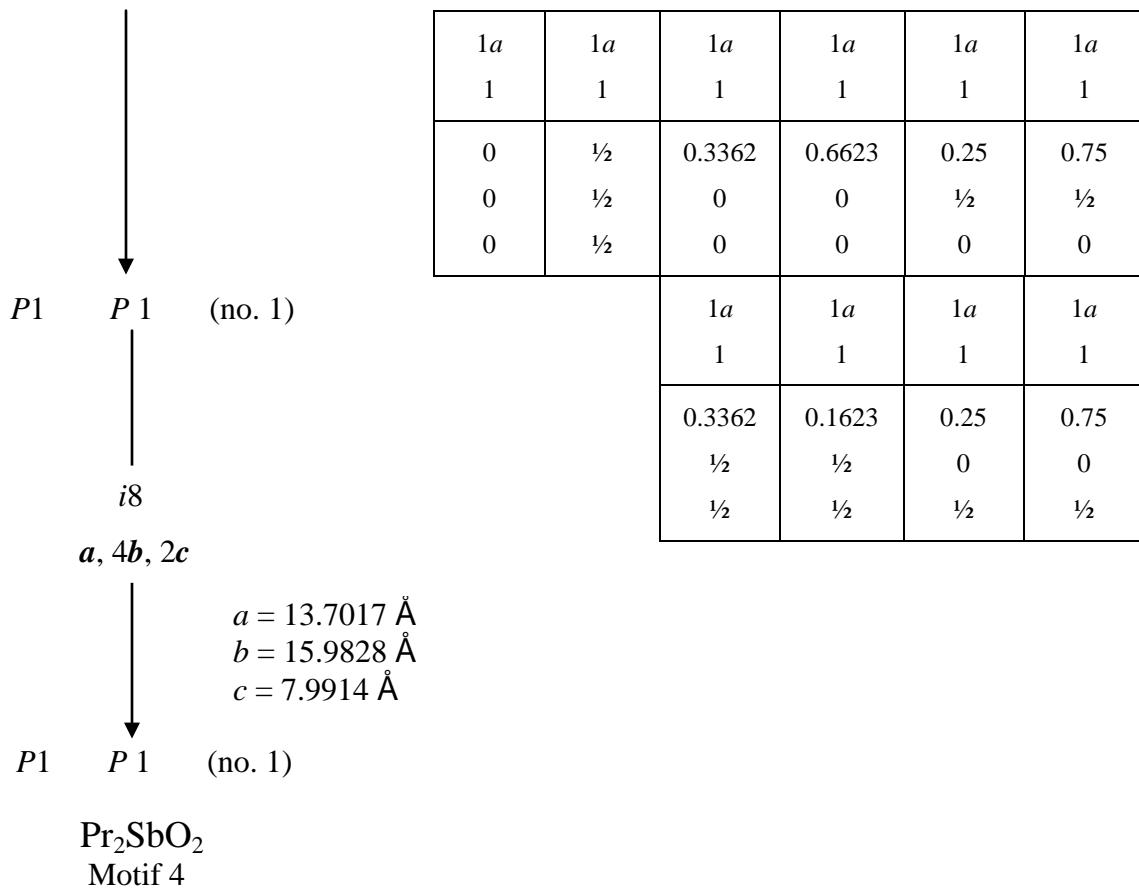


Fig. 3. Group-subgroup relations between idealized Structure of Pr<sub>2</sub>SbO<sub>2</sub> (which is identical to Pr<sub>2</sub>BiO<sub>2</sub>) and structure with ordered Sb-dumbbells and isolate Sb-atoms (motif 4, Fig. 12e).