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**Supporting information for article:**

**X-Ray Calc 3: improved software for simulation and inverse problem solving for X-ray reflectivity**

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Stack / Layer	H (Å)	$\sigma$ (Å)	$\rho$ (g/cm³)	N
Top				1
Si	40.00	3.00	2.10	
Main (top)				7
MoSiz	7.70	4.00	6.10	
Mo	16.00	4.00	10.00	
MoSiz	11.00	4.00	6.10	
Si	42.00	4.00	2.33	
Main (bottom)				7
MoSiz	5.40	3.00	6.10	
Mo	22.00	3.00	10.00	
MoSiz	10.20	3.00	6.10	
Si	32.00	3.00	2.10	
Bottom				1
MoSiz	9.00	4.00	6.40	
Mo	100.00	4.00	10.20	
Substrate				
SiO2	5.00	2.20		

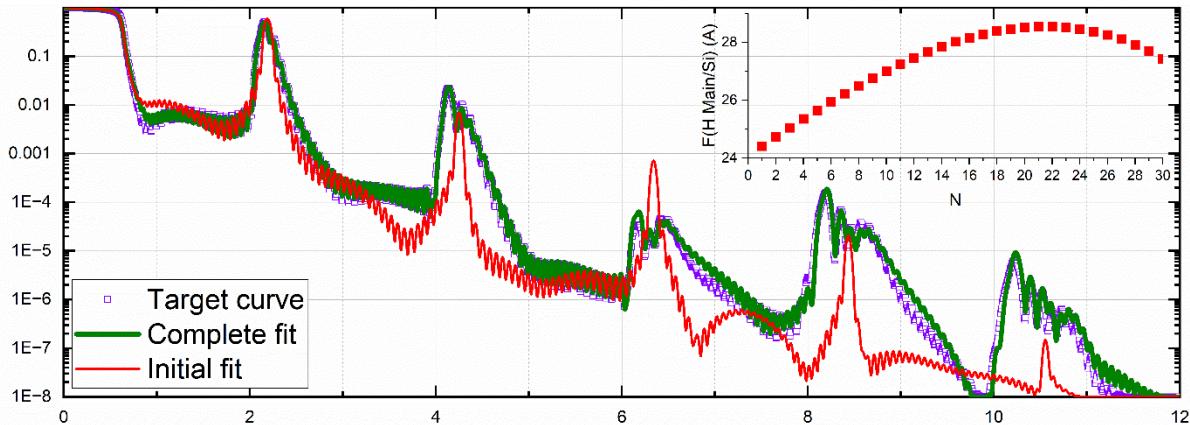
  

Stack / Layer	H (Å)	$\sigma$ (Å)	$\rho$ (g/cm³)	N
Top				1
Si	47.56	3.11	2.23	
Main (top)				1
MoSiz	7.00	4.00	6.10	
Mo	16.00	4.00	10.00	
MoSiz	11.00	4.00	6.10	
Si	42.00	4.00	2.33	
Main (bottom)				1
MoSiz	5.40	3.00	6.10	
Mo	22.00	3.00	10.00	
MoSiz	10.20	3.00	6.10	
Si	32.00	3.00	2.10	
Bottom				1
MoSiz	7.00	4.00	6.40	
Mo	100.00	4.00	10.20	
Substrate				
SiO2	5.00	2.20		

Stack / Layer	H (Å)	$\sigma$ (Å)	$\rho$ (g/cm³)	N
Top				1
Si	60.00	2.00	2.00	
Main				30
Si	24.00	4.00	2.00	
Mo	18.00	4.00	9.50	
Substrate				
Si	5.00	2.20		

**Figure S1** Examples of fitted structures. a) Multilayer coating with two periodical stacks (N = 2x7). b) non-periodical structure, 12 layers in total. c) Simple periodical structure (N=30) with a top layer.



**Figure S2** XRR fitting for test structure ML30x2 (P3). Inset shows reconstructed distribution of thickness of Si layer.

**Table S1** Computation time of XRR curves ( $\theta$ - $2\theta$  mode, 2000 points) on various CPUs.

CPU	Cores/Threads	Computing time (sec)			
		4 Layers	12 Layers	Multilayer 30x2 (P3)	Multilayer (300x4)
Intel Core i7-12700H	14/20	0.006	0.007	0.011	0.090
Intel Core i9-10900K	10/20	0.003	0.003	0.007	0.057
Intel Core i9-13900KF	24/32	0.002	0.002	0.014	0.065
AMD Ryzen 9 3950X	16/32	0.005	0.006	0.018	0.065

**Table S2** Solving of optimization problem on various CPUs. Default settings. Size: 200, Population: 200.

CPU	Cores/Threads	Structure Model			
		4 Layers	12 Layers	Multilayer 30x2 (P3)	Multilayer (300x4)
Intel Core i7-12700H	14/20	1 min 57 sec	2 min 13 sec	5 min 32 sec	75 min
Intel Core i9-10900K	10/20	1 min 18 sec	2 min 00 sec	3 min 35 sec	41 min
Intel Core i9-13900KF	24/32	1 min 32 sec	1 min 37 sec	3 min 59 sec	44 min
Intel Core i9-13900KF	8/16*	1 min 07 sec	1 min 18 sec	3 min 4 sec	40 min
AMD Ryzen 9 3950X	16/32	4 min 23 sec	4 min 23 sec	7 min 06 sec	52 min