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Supporting information for article:

Exploring the impact of incoherent Compton scattering on X-ray pair distribution function analysis of disordered materials

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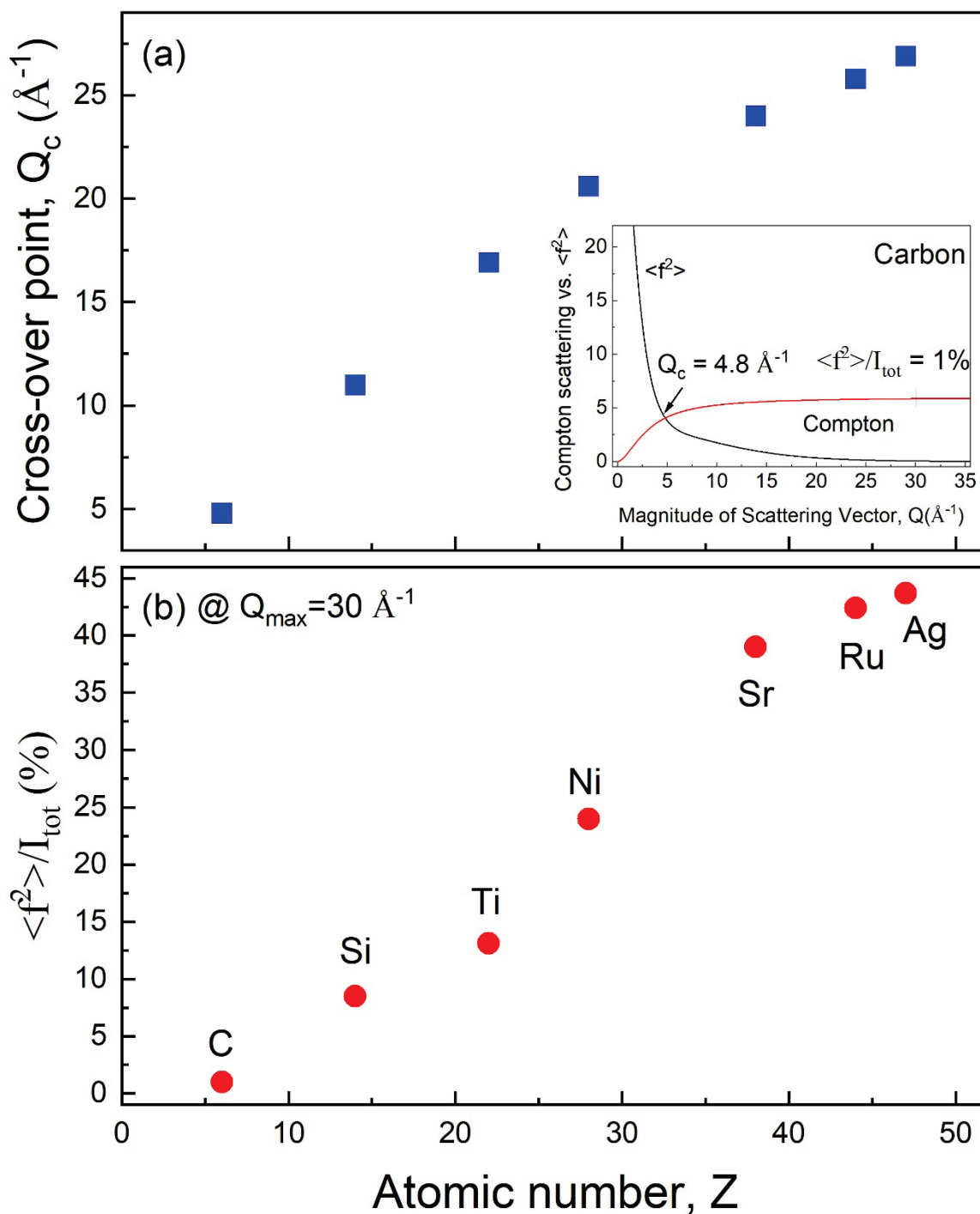


Fig. S1. (a) Cross-over point, Q_c between Compton intensity and $\langle f^2 \rangle$ as a function of atomic number, Z . The inset shows a comparison of Compton and atomic form factor of Carbon. The cross-over point Q_c and $\langle f^2 \rangle / I_{\text{tot}}$ at $Q = 30 \text{\AA}^{-1}$ are marked. (b) The ratio of $\langle f^2 \rangle$ to the total intensity I_{tot} at $Q_{\text{max}} = 30 \text{\AA}^{-1}$. For light elements such as carbon and silicon, elastic scattering estimated by $\langle f^2 \rangle$ is less than 10% of the total intensity.

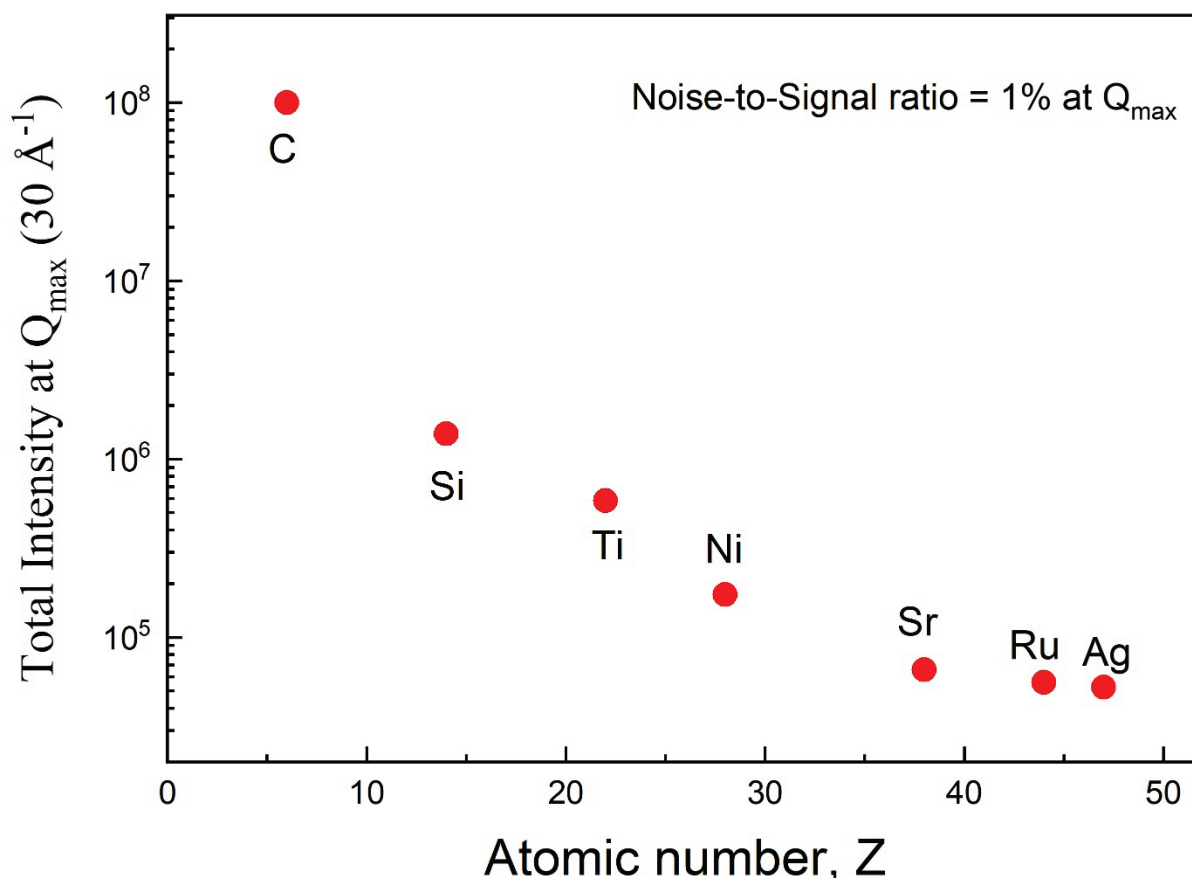


Fig. S2. Total intensity I_{tot} required to achieve a noise-to-signal ratio of 1% at $Q_{\max} = 30 \text{ \AA}^{-1}$ based on $\langle f^2 \rangle / I_{\text{tot}}$ shown in Fig. S1(b) as a function of atomic number, Z . For lighter elements, much higher counts are measured. Beyond strontium, the slope of I_{tot} with Z becomes weak.

In the simulation studies we tested three cases with total intensities 7500, 30,000, and 120,000 counts at $Q_{\max} = 35 \text{ \AA}^{-1}$. In the Fig. S3, simulated XRPD intensity (elastic and Compton scattering) shown in (a) is re-scaled with scale factor of 310 to obtain total intensity of $I_{\text{tot}} = 7,500$ at $Q_{\max} = 35 \text{ \AA}^{-1}$ (Fig. S3(b)). For a given ratio $\langle f^2 \rangle / I_{\text{tot}} = 0.33$ at Q_{\max} (35 \AA^{-1}), the corresponding elastic scattering $\langle f^2 \rangle \sim 7500 \times 0.33 \approx 2500$ counts, and the intensity of Compton scattering is about $7500 \times 0.67 \approx 5000$ counts, respectively. And then, random noise is added using Poisson statistics based on rescaled intensities of elastic and Compton scattering. After rescaling, the N/S ratio given by $\sqrt{I_{\text{coh}} + I_{\text{inc}}} / \langle f^2 \rangle$ is $\sqrt{7500} / 2500 = 3.4\%$. Similarly, Fig. S3(c) shows the case with total intensity of 30,000 counts (scale factor 1240). Here, $\langle f^2 \rangle$ is about 10,000, and the Compton intensity is 20,000 respectively. Thus, the N/S will be about 1.7%.

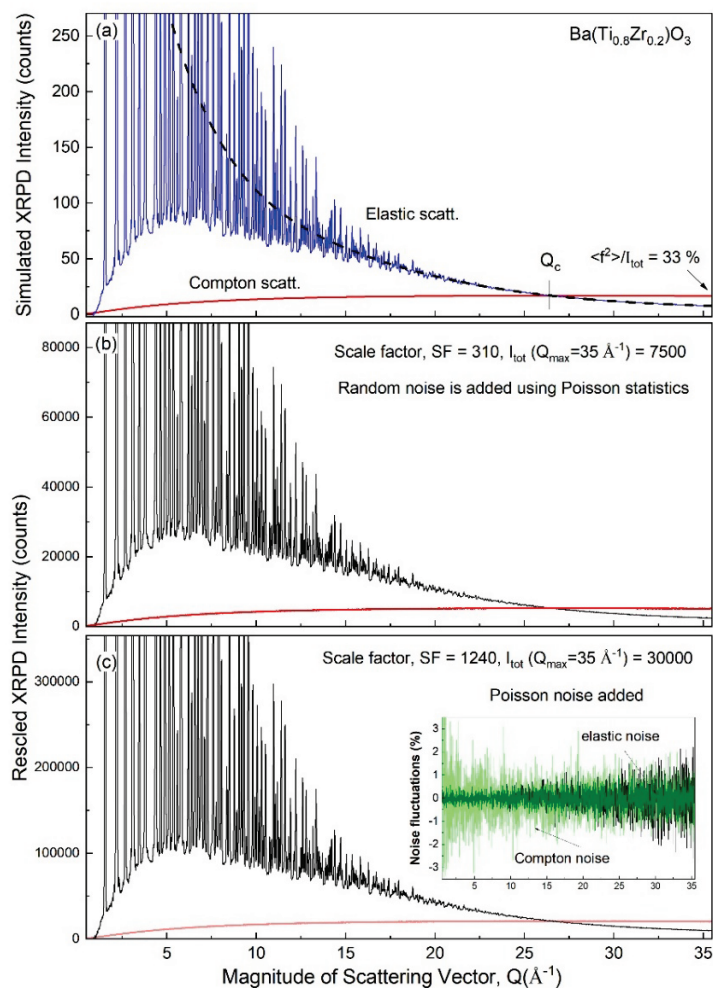


Fig. S3. (a) A simulated x-ray elastic diffraction pattern and Compton scattering of $\text{Ba}(\text{Ti}_{0.8}\text{Zr}_{0.2})\text{O}_3$. The ratio of $\langle f^2 \rangle$ to I_{tot} is 0.33 at $Q_{\text{max}} = 35 \text{ \AA}^{-1}$. (b) Re-scaled intensities of elastic and Compton scattering with scale factor of 310. Total intensity at $Q_{\text{max}} = 35 \text{ \AA}^{-1}$ is 7,500. (c) Re-scaled XRPD intensity with $\text{SF} = 1240$ to have total intensity of 30,000 at $Q_{\text{max}} = 35 \text{ \AA}^{-1}$. After re-scaling random noise is added following Poisson statistics. The inset shows noise fluctuations in elastic and Compton scattering.