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**Supporting information for article:**

**When the difference between incommensurate and commensurate structures becomes elusive: the case of  $\text{Bi}_4\text{BO}_7\text{X}$  ( $\text{X} = \text{Cl}, \text{Br}$ ) oxyhalides**

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**Table S1** Atomic coordinates, displacement parameters ( $\text{\AA}^2$ ), site-occupancy factors (SOFs) and bond valence sums (BVS, v.u.) in the structure of  $\text{Bi}_4\text{BO}_7\text{Cl}$ .

| Atom | SOF  | Wyckoff site | $x$       | $y$        | $z$ | $U_{\text{eq}}$ | BVS               |
|------|------|--------------|-----------|------------|-----|-----------------|-------------------|
| Bi   | 1    | 4g           | 0.5       | 0.15371(3) | 0.5 | 0.02037(19)     | 2.643(1)–3.453(1) |
| Cl   | 0.5  | 2a           | 0         | 0          | 0   | 0.044(2)        | 0.556(1)–0.664(1) |
| B    | 0.5  | 2a           | 0         | 0          | 0   | 0.044(2)        | 2.873(1)–3.487(1) |
|      |      |              |           | 0.2475(7)  |     | 0.019(2)        | 2.135(1)–2.315(1) |
| O1   | 1    | 8l           | 0         |            | 0.5 |                 |                   |
| O2   | 0.5  | 8l           | 0         | –0.078(4)  | 0   | 0.019(5)        | 1.701(1)–2.292(1) |
| O3   | 0.25 | 8m           | –0.184(8) | –0.090(3)  | 0   | 0.037995        | 1.806(1)–1.982(1) |
| O4   | 0.5  | 8n           | –0.363    | 0          | 0   | 0.130968        | 1.374(1)–1.496(1) |

**Table S2** Anisotropic parameters of atomic displacements in the structure of  $\text{Bi}_4\text{BO}_7\text{Cl}$ .

| Atom | $U_{11}$  | $U_{22}$  | $U_{33}$  | $U_{12}$ | $U_{13}$ | $U_{23}$ |
|------|-----------|-----------|-----------|----------|----------|----------|
| Bi   | 0.0254(4) | 0.0179(3) | 0.0178(3) | 0        | 0        | 0        |
| Cl   | 0.063(5)  | 0.028(4)  | 0.041(4)  | 0        | 0        | 0        |
| B    | 0.063(5)  | 0.028(4)  | 0.041(4)  | 0        | 0        | 0        |
| O1   | 0.018(4)  | 0.025(5)  | 0.014(3)  | 0        | 0        | 0        |
| O2   | 0.019(8)  | 0.011(9)  | 0.026(8)  | 0        | 0        | 0        |
| O3   | 0.037995  | 0.037995  | 0.037995  | 0        | 0        | 0        |
| O4   | 0.130968  | 0.130968  | 0.130968  | 0        | 0        | 0        |

**Table S3** Selected distances ( $\text{\AA}$ ) in the crystal structure of  $\text{Bi}_4\text{BO}_7\text{Cl}$ .

|                  | Ave.       | Min.       | Max.       |
|------------------|------------|------------|------------|
| Bi–O1 $\times$ 2 | 2.326(10)  | 2.209(17)  | 2.371(17)  |
| Bi–O1 $\times$ 2 | 2.335(14)  | 2.105(18)  | 2.609(18)  |
| Bi–O3 $\times$ 4 | 3.394(19)  | 3.33(2)    | 3.48(2)    |
| Bi–O4 $\times$ 4 | 2.7959(9)  | 2.7525(14) | 2.8608(14) |
| Bi–O2 $\times$ 4 | 2.851(10)  | 2.48(2)    | 3.34(2)    |
| Bi–Cl $\times$ 4 | 3.461(4)   | 3.408(6)   | 3.495(6)   |
| B–O2 $\times$ 2  | 1.306(19)  | 1.24(2)    | 1.37(2)    |
| B–O3 $\times$ 4  | 1.40(3)    | 1.40(3)    | 1.40(3)    |
| B–O4 $\times$ 4  | 1.4258(12) | 1.4258(12) | 1.4258(12) |

**Table S4** Atomic coordinates, displacement parameters ( $\text{\AA}^2$ ), site-occupancy factors (SOFs) and bond valence sums (BVS, v.u.) in the structure of  $\text{Bi}_4\text{BO}_7\text{Br}$ .

| Atom | SOF  | Wyckoff site | $x$        | $y$        | $z$       | $U_{\text{eq}/\text{iso}}$ | BVS               |
|------|------|--------------|------------|------------|-----------|----------------------------|-------------------|
| Bi   | 1    | 4g           | 0.5        | 0.15510(3) | 0.5       | 0.02038(19)                | 2.74(13)–3.26(13) |
| Br   | 0.5  | 2a           | 0          | 0          | 0         | 0.0221(7)                  | 0.60(13)–0.76(13) |
| B    | 0.5  | 2a           | 0          | 0          | 0.1192    | 0.0221(7)                  | 2.40(13)–3.36(13) |
| O1   | 1    | 8l           | 0          | 0.2440(11) | 0.5       | 0.014(3)                   | 2.15(13)–2.29(13) |
| O2   | 0.25 | 8l           | 0          | 0.1042(2)  | 0.0631(9) | 0.057(8)*                  | 1.57(13)–1.90(13) |
| O3   | 0.25 | 8m           | 0.2516(14) | –0.0609(3) | 0         | 0.057(8)*                  | 1.94(13)–2.21(13) |
| O4   | 0.5  | 4e           | 0          | 0          | 0.4268(8) | 0.1158(8)                  | 1.80(13)–2.14(13) |

\*Isotropic ADP

**Table S5** Anisotropic parameters of atomic displacements in the structure of Bi<sub>4</sub>BO<sub>7</sub>Br.

| Atom | $U_{11}$   | $U_{22}$   | $U_{33}$   | $U_{12}$ | $U_{13}$ | $U_{23}$ |
|------|------------|------------|------------|----------|----------|----------|
| Bi   | 0.0291(4)  | 0.0172(2)  | 0.0148(3)  | 0        | 0        | 0        |
| Br   | 0.0125(12) | 0.0214(10) | 0.0323(15) | 0        | 0        | 0        |
| B    | 0.0125(12) | 0.0214(10) | 0.0323(15) | 0        | 0        | 0        |
| O1   | 0.012(5)   | 0.019(4)   | 0.013(5)   | 0        | 0        | 0        |

**Table S6** Selected distances (Å) in the crystal structure of Bi<sub>4</sub>BO<sub>7</sub>Br.

|           | Ave.       | Min.       | Max.       |
|-----------|------------|------------|------------|
| Bi–O1 × 2 | 2.306(10)  | 2.187(14)  | 2.365(14)  |
| Bi–O1 × 2 | 2.376(15)  | 2.064(17)  | 2.655(17)  |
| Bi–O3 × 4 | 2.4470(14) | 2.3578(18) | 2.6377(18) |
| Bi–O2 × 4 | 2.6393(16) | 2.5704(19) | 2.7945(19) |
| Bi–Br × 4 | 3.4542(3)  | 3.4178(18) | 3.5557(18) |
| B–O2 × 2  | 1.3987     | 1.3987     | 1.3987     |
| B–O3 × 2  | 1.3596(6)  | 1.3596(6)  | 1.3596(6)  |
| B–O4 × 4  | 1.2055     | 1.2055     | 1.2055     |

**Table S7** Assignment of the vibrational bands observed in the infrared and Raman spectra for Bi<sub>4</sub>BO<sub>7</sub>Br.

| Raman band, cm <sup>-1</sup> | IR, cm <sup>-1</sup> | Assignment   |
|------------------------------|----------------------|--|
| 88                           |                      | Bi–O lattice vibrations  |
| 115                          |                      | stretching frequencies of the BiO units with Bi–O bonds <2.4 Å   |
| 157                          |                      |  |
| 226                          |                      |  |
| 296                          |                      |  |
| 450–608                      | 705                  | stretching frequencies of the BiO units with Bi–O bonds >2.4 Å<br>Bending vibrations of BO <sub>3</sub> groups |
|                              |                      | Stretching vibrations of BO <sub>3</sub> groups  |
| 915                          |                      |  |
| 1155                         |                      |  |
|                              | 1210                 |  |
|                              | 1314                 |  |
|                              | 1415                 | Asymmetric stretching vibration of the Bi–Cl band  |
|                              | 1525                 |  |

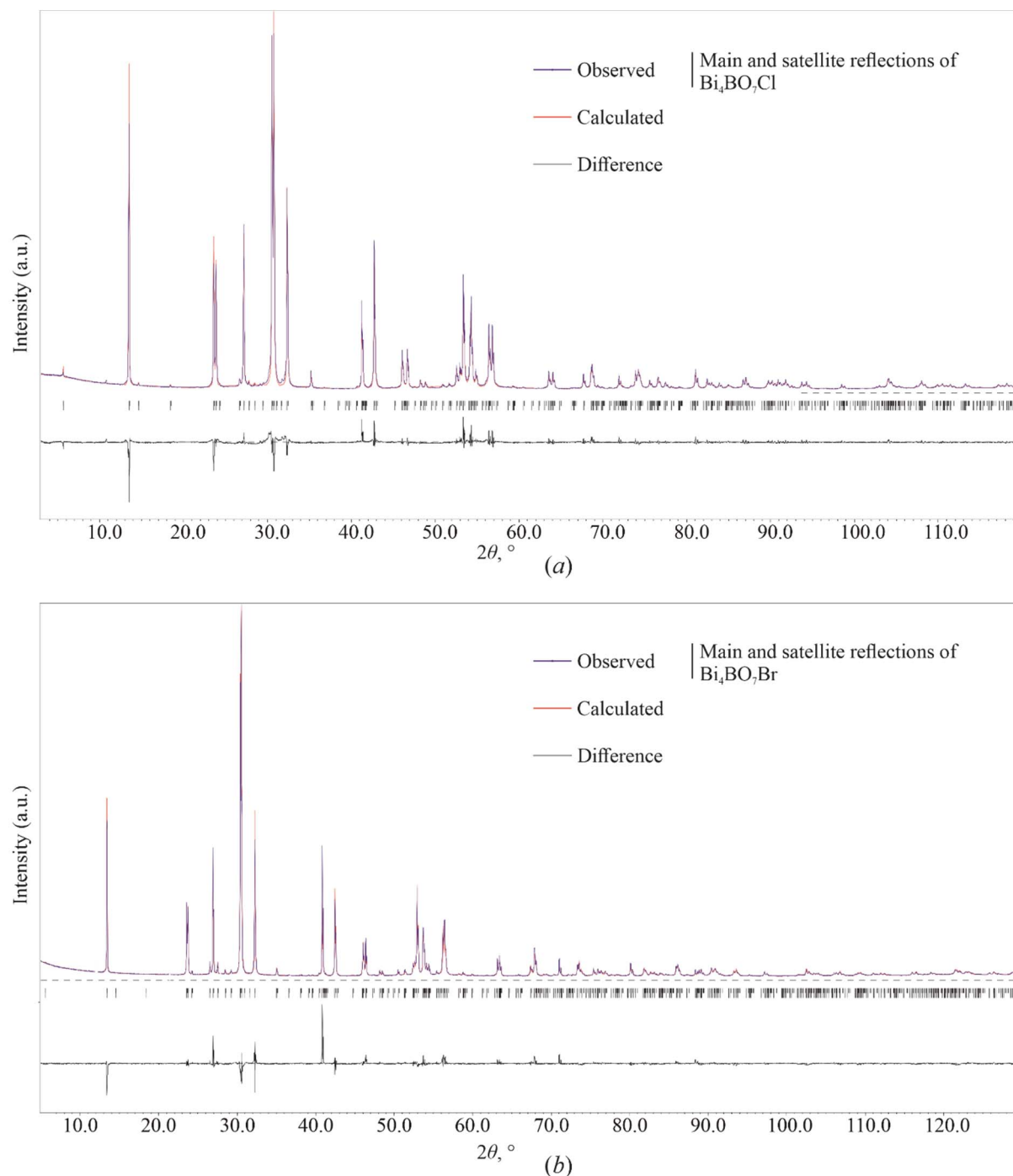
**Table S8** Optimized lattice parameters (Å) for Bi<sub>4</sub>BO<sub>7</sub>Br.

|              | Optimized | Initial model |
|--------------|-----------|---------------|
| <i>a</i> (Å) | 4.157     | 3.935         |
| <i>b</i> (Å) | 13.451    | 13.250        |
| <i>c</i> (Å) | 16.194    | 15.673        |

**Table S9** The decomposition products of  $\text{Bi}_4\text{BO}_7\text{Br}$  compound, as obtained from the Materials Project database.

| Compound                           | ICSD # | MP ID # <sup>a</sup> | Space group |
|------------------------------------|--------|----------------------|-------------|
| $\text{Bi}_4\text{Br}_2\text{O}_5$ | 412591 | mp-23544             | $P2_1$      |
| $\text{Bi}_4\text{B}_2\text{O}_9$  | 250426 | mp-23356             | $P2_1/c$    |

<sup>a</sup>The unique ID # from the Materials Project database.



**Figure S1** Intensity profiles for the powder X-ray Rietveld refinement of (a)  $\text{Bi}_4\text{BO}_7\text{Cl}$  and (b)  $\text{Bi}_4\text{BO}_7\text{Br}$ . The observed and calculated profiles are represented in blue and red lines, respectively. The difference profile is plotted at the bottom.

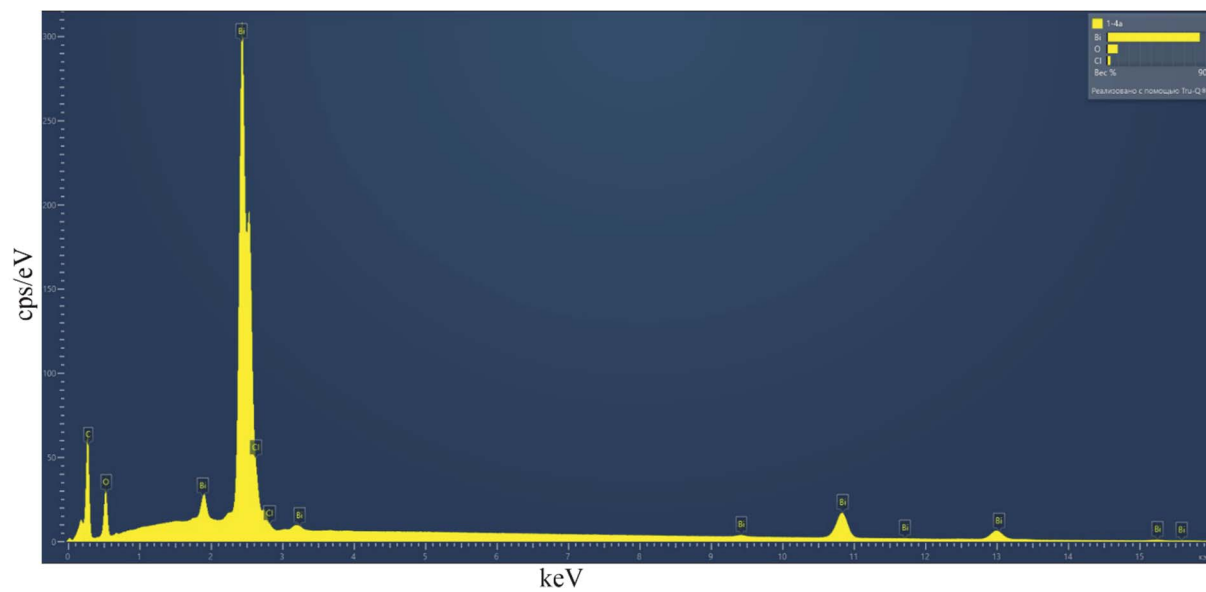


Figure S2 EDX spectrum of  $\text{Bi}_4\text{BO}_7\text{Cl}$ .