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Supporting information for article:

Site dependence of the magnetocaloric effect in $\text{Mn}_{5-x}\text{Fe}_x\text{Si}_3$

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Site dependence of the magneto-caloric effect in $\text{Mn}_{5-x}\text{Fe}_x\text{Si}_3$: Supplementary Material

Table S.1. *Nominal composition of $\text{Mn}_3\text{Fe}_2\text{Si}_3$ as compared to results from chemical analysis (ICP-OES spectroscopy).*

Substance	Nominal Mass (g)	Nominal Mass Ratio (%)	ICP-OES results
Mn	22.85	45.69	45.6±0.3
Fe	15.48	30.96	29.3±0.2
Si	11.68	23.36	23.4±0.1

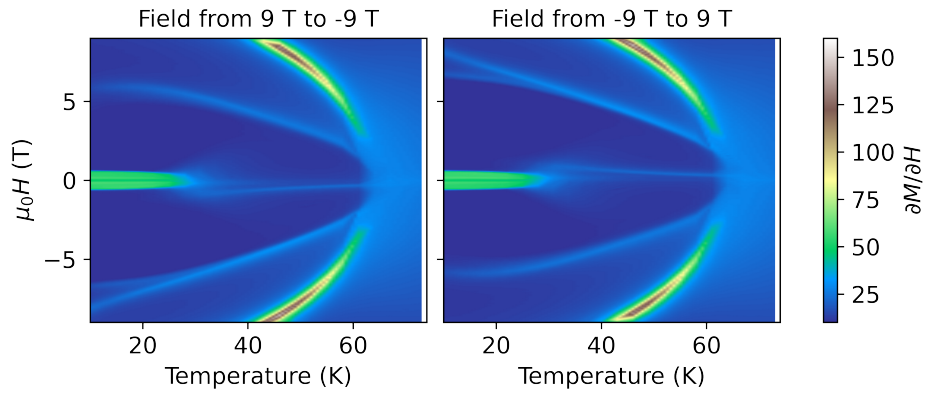


Fig. S.1. False colour plot of $\partial M/\partial H$ for an applied field \parallel [001] interpolated from the isothermal magnetization curves upon field change from 9 T to -9 T (*left*) and from -9 T to 9 T (*right*) for Mn_5Si_3 .

Table S.2. Details of the structure refinements on $Mn_3Fe_2Si_3$ in space group $P6_3/mcm$ based on X-ray diffraction data. Number of variable parameters at all temperatures is 12.

T [K]	No. of measured reflections (obs/all)	$h_{\min} \rightarrow h_{\max}$ $k_{\min} \rightarrow k_{\max}$ $l_{\min} \rightarrow l_{\max}$	No. of indep. reflections (obs/all)	$R(\text{int})$ obs/all	R obs/all	wR obs/all	No. of runs
300	8136/11477	-17 \rightarrow 11; -18 \rightarrow 14; -12 \rightarrow 8	655/787	5.52/5.56	2.45/3.15	2.59/2.74	3
250	8408/11453	-17 \rightarrow 11; -18 \rightarrow 14; -12 \rightarrow 8	668/785	5.42/5.46	2.38/2.94	2.64/2.75	3
200	8603/11415	-17 \rightarrow 11; -18 \rightarrow 14; -12 \rightarrow 8	679/782	4.23/4.27	1.98/2.54	2.32/2.42	3
150	8601/11399	-17 \rightarrow 11; -12 \rightarrow 14; -12 \rightarrow 8	670/779	4.14/4.18	1.98/2.51	2.22/2.32	3
125	8610/11410	-17 \rightarrow 11; -18 \rightarrow 14; -12 \rightarrow 8	665/777	4.22/4.26	2.16/2.64	2.41/2.50	3
100	8565/11357	-17 \rightarrow 11; -14 \rightarrow 12; -12 \rightarrow 8	662/774	4.00/4.04	2.12/2.75	2.37/2.47	3
80	8527/11378	-17 \rightarrow 11; -14 \rightarrow 12; -12 \rightarrow 8	660/774	4.45/4.50	2.36/2.97	2.56/2.66	3
60	8449/11376	-17 \rightarrow 11; -14 \rightarrow 12; -12 \rightarrow 8	654/774	4.40/4.46	2.35/3.01	2.57/2.70	3
40	3291/4572	-16 \rightarrow 9; -18 \rightarrow 14; -12 \rightarrow 5	619/766	3.69/3.80	2.38/3.40	2.78/2.97	1
20	3220/4563	-16 \rightarrow 9; -18 \rightarrow 14; -12 \rightarrow 5	617/765	3.48/3.58	2.54/3.48	2.46/2.63	1

Table S.3. *Lattice parameter and unit cell volume of $Mn_3Fe_2Si_3$ as a function of temperature.*

T (K)	a (Å)	c (Å)	V (Å ³)
300	6.85340(10)	4.75560(10)	193.441(6)
250	6.84910(10)	4.75170(10)	193.040(6)
200	6.84390(10)	4.74740(10)	192.572(6)
150	6.83950(10)	4.74250(10)	192.126(6)
125	6.83760(10)	4.74090(10)	191.955(6)
100	6.83590(10)	4.73890(10)	191.778(6)
80	6.83550(10)	4.73789(10)	191.715(6)
60	6.83490(10)	4.73790(10)	191.682(6)
40	6.8343(2)	4.73690(10)	191.608(9)
20	6.8341(2)	4.73710(10)	191.605(9)

Table S.4. Atomic coordinates and isotropic displacement parameters of $Mn_3Fe_2Si_3$ from the refinements of *x*-ray single crystal diffraction data in $P6_3/mcm$. Mn1/Fe1 occupies WP 4d ($2/3, 1/3, 0$); Mn2/Fe2 and Si occupy WP 6g ($x, 0, 1/4$).

T (K)	$x(Mn2/Fe2)$	$x(Si)$	$U_{iso}(Mn1/Fe1)$	$U_{iso}(Mn2/Fe2)$	$U_{iso}(Si)$
300	0.23281(3)	0.59802(6)	0.00619(4)	0.00788(4)	0.00692(8)
250	0.23271(3)	0.59805(6)	0.00574(4)	0.00719(4)	0.00646(8)
200	0.23259(3)	0.59805(5)	0.00481(3)	0.00596(3)	0.00551(7)
150	0.23249(3)	0.59808(5)	0.00426(3)	0.00515(3)	0.00498(7)
125	0.23247(3)	0.59806(5)	0.00388(3)	0.00465(3)	0.00457(7)
100	0.23250(3)	0.59806(5)	0.00355(3)	0.00419(3)	0.00427(7)
80	0.23246(3)	0.59809(6)	0.00359(3)	0.00417(4)	0.00432(8)
60	0.23247(3)	0.59812(6)	0.00359(4)	0.00410(4)	0.00436(8)
40	0.23246(4)	0.59807(8)	0.00380(4)	0.00416(5)	0.00442(5)
20	0.23247(3)	0.59811(7)	0.00409(4)	0.00450(4)	0.00481(9)

Table S.5. Interatomic distances in Å of $Mn_3Fe_2Si_3$ in space group $P6_3/mcm$ obtained from synchrotron X-ray single crystal diffraction at different temperatures (The assignment of the interatomic distances is illustrated in figure S.2). Symmetry code: $[i]x, y, -z - 1/2$,

$[ii] - x + 1, -y, -z, [iii] - y + 1, x - y, z, [iv] - y + 1, x - y, z, [v]y + 1, -x + y, -z,$
 $[vi] - x + 1, -y, -z, [vii]y, -x + y + 1, -z, [viii] - y, x - y, z.$

T (K)	M1-M1 ^t (Å)	M1-M2 ⁱⁱ /M2 ⁱⁱⁱ (Å)	M2 ⁱⁱ -M2 ⁱⁱⁱ (Å)	M2 ⁱⁱ -M2 ^{iv} (Å)	M2 ⁱⁱ -Si (Å)	M2 ⁱⁱ -Si ^v (Å)	M2 ⁱⁱ -Si ^{vi} (Å)	M1-Si ^{vii} (Å)
300	2.37780(10)	2.94629(15)	2.86352(17)	2.7636(3)	2.3958(4)	2.5029(4)	2.6454(2)	2.4039(4)
250	2.37585(10)	2.94475(17)	2.86099(16)	2.7608(3)	2.3941(4)	2.5022(5)	2.6435(2)	2.4024(4)
200	2.37370(10)	2.94301(19)	2.85803(15)	2.7571(2)	2.3921(3)	2.5012(4)	2.64157(19)	2.4005(3)
150	2.37125(10)	2.94134(18)	2.85504(15)	2.7541(2)	2.3904(3)	2.5005(4)	2.63926(19)	2.3987(4)
125	2.37045(10)	2.94060(19)	2.85405(15)	2.7531(3)	2.3898(3)	2.4998(4)	2.6385(2)	2.3980(4)
100	2.36945(10)	2.93964(17)	2.85312(16)	2.7528(3)	2.3893(3)	2.4989(4)	2.6374(2)	2.3973(4)
80	2.36895(10)	2.93957(17)	2.85250(16)	2.7522(3)	2.3889(4)	2.4993(5)	2.6370(2)	2.3971(4)
60	2.36895(10)	2.93931(17)	2.85246(16)	2.7521(3)	2.3885(4)	2.4992(5)	2.6368(2)	2.3970(4)
40	2.36845(10)	2.9390(3)	2.8519(2)	2.7517(4)	2.3886(5)	2.4986(6)	2.6365(3)	2.3966(5)
20	2.36855(10)	2.9390(3)	2.85202(19)	2.7517(4)	2.3883(5)	2.4988(5)	2.6364(2)	2.39669(19)

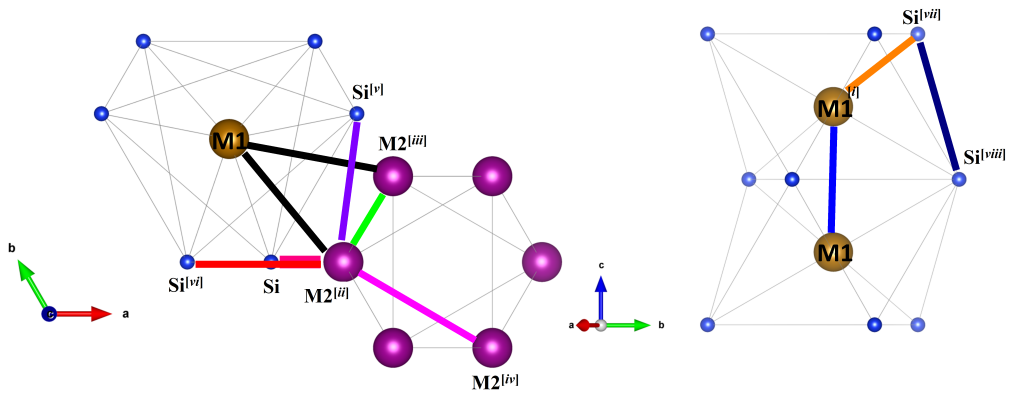


Fig. S.2. Interatomic distances in the crystal structure of $\text{Mn}_3\text{Fe}_2\text{Si}_3$. Symmetry code:
 $[i]x, y, -z - 1/2$, $[ii] - x + 1, -y, -z$, $[iii] - y + 1, x - y, z$, $[iv] - y + 1, x - y, z$,
 $[v]y + 1, -x + y, -z$, $[vi] - x + 1, -y, -z$, $[vii]y, -x + y + 1, -z$, $[viii] - y, x - y, z$.

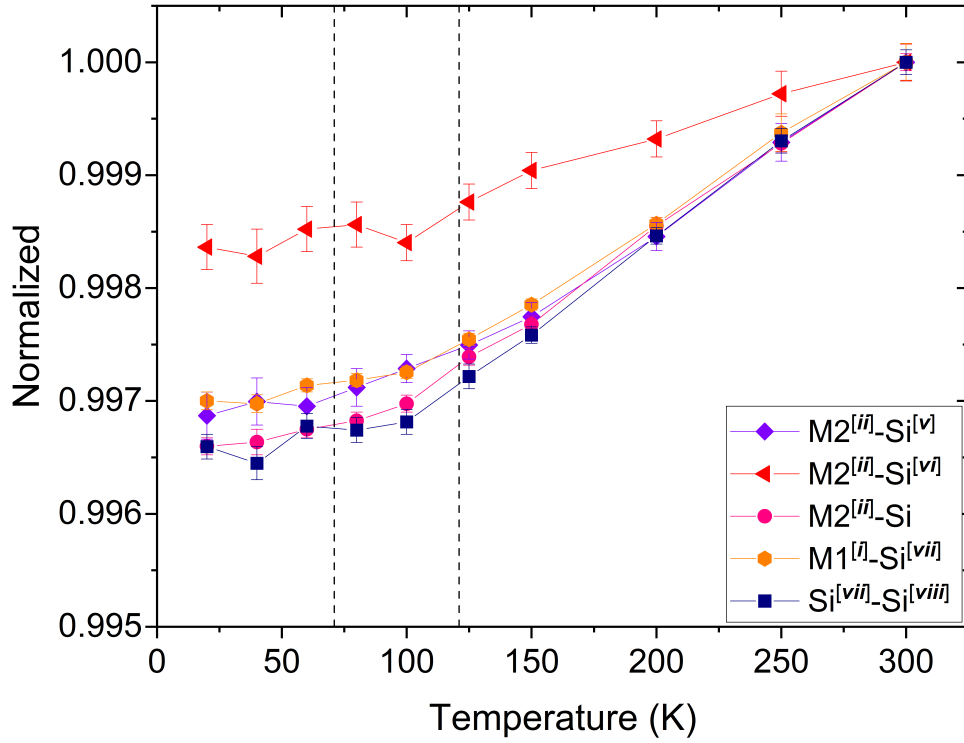


Fig. S.3. Temperature dependence of M-Si and Si-Si interatomic distances of $\text{Mn}_3\text{Fe}_2\text{Si}_3$, normalized to the value at 300 K, obtained on the basis of refinements from synchrotron X-ray single crystal diffraction data. Temperatures of the AF1-AF2 and AF2-PM transitions are indicated by dashed lines.

Table S.6. *Unit cell parameters of $Mn_3Fe_2Si_3$ described
in space group $Ccmm$*

T	<i>a</i>	<i>b</i>	<i>c</i>
105 K	6.8429 (1)Å	11.8523Å	4.7450(1)Å
90 K	6.8421 (1)Å	11.8509Å	4.7441(1)Å
50 K	6.8405 (1)Å	11.8482Å	4.7427(1)Å
20 K	6.8395 (2)Å	11.8464Å	4.7423(1)Å

Table S.7. Atomic coordinates and isotropic displacement parameters of $Mn_3Fe_2Si_3$ described in space group C_{6mm} for the different temperatures. All atomic parameters are restricted to obey the higher hexagonal symmetry $P6_3/mcm$ ($x=y(Mn22/Fe22)=0.5x(Mn21/Fe21)$ and $x=y(Si2)=0.5x(Si1)$). Displacement parameters for all atoms were restricted to be equal.

T	Mn1/Fe1			Mn21/Fe21			Mn22/Fe22			Si1			Si2			$U_{i,so}$
	x	y	z	x	y	z	x	y	z	x	y	z	x	y	z	
105 K	1/2	-1/6	0	-0.2260(5)	0	1/4	-0.1130	x	1/4	-0.5980(2)	0	0.25	-0.2990	x	1/4	0.0024(1)
90 K	1/2	-1/6	0	-0.2258(5)	0	1/4	-0.1130	x	1/4	-0.5981(3)	0	0.25	-0.2991	x	1/4	0.0024(1)
50 K	1/2	-1/6	0	-0.2261(5)	0	1/4	-0.1130	x	1/4	-0.5979(3)	0	0.25	-0.2990	x	1/4	0.0022(1)
20 K	1/2	-1/6	0	-0.2260(5)	0	1/4	-0.1130	x	1/4	-0.5981(4)	0	0.25	-0.2991	x	1/4	0.0022(1)

Table S.8. *Derived magnetic space groups (MSG) for the magnetic structure of $Mn_3Fe_2Si_3$ based on the symmetry $Ccmm$ and the propagation vector $k=(010)$. The allowed directions of the magnetic moments are given.*

MSG	Fe1/Mn1		Fe21/Mn21			Fe22/Mn22		
P_{Cnm}	0	M_y	0	0	0	0	0	M_z
P_{Cnam}	M_x	0	M_z	0	0	M_z	0	M_z
P_{Cnmn}	0	M_y	0	0	M_y	0	M_x	M_y
P_{Ccan}	M_x	0	M_z	M_x	0	0	M_x	M_y
P_{Cnan}	0	M_y	0	M_x	0	0	M_x	M_y
P_{Ccmn}	M_x	0	M_z	0	M_y	0	M_x	M_y
P_{Ccam}	0	M_y	0	0	0	M_z	0	M_z
P_{Cnmm}	M_x	0	M_z	0	0	0	0	M_z

Table S.9. $R(\text{obs/all})$ and $wR(\text{obs/all})$ factors for magnetic Bragg reflections of $\text{Mn}_3\text{Fe}_2\text{Si}_3$ based on the neutron powder data measured on POWGEN at different temperatures for a center wavelength of 2.665 \AA . Magnetic space groups are derived from symmetry C_{cmm} of the nuclear structure.

		$R(\text{obs/all})$						
T (K)	$P_{C_{cmm}}$	$P_{C_{nam}}$	$P_{C_{nmn}}$	$P_{C_{can}}$	$P_{C_{nan}}$	$P_{C_{cmn}}$	$P_{C_{cam}}$	$P_{C_{nmm}}$
105	30.87/	16.14/	29.86/	20.60/	5.44/	18.62/	32.53/	27.16/
	58.42	48.09	53.59	39.30	17.80	38.92	64.00	58.28
90	37.61/	22.28/	32.06/	29.23/	8.16/	20.00/	30.98/	37.31/
	52.63	40.20	59.67	42.56	17.17	37.18	55.74	52.47
50	29.99/	21.11/	29.46/	24.43/	10.06/	21.18/	28.34/	31.14/
	42.48	34.17	34.56	38.64	19.72	36.54	43.27	42.21
20	26.31/	21.29/	31.91/	23.02/	12.82/	25.42/	29.42/	31.76/
	29.36	34.86	46.37	32.47	26.69	39.71	41.70	37.94
		$wR(\text{obs/all})$						
T (K)	$P_{C_{cmm}}$	$P_{C_{nam}}$	$P_{C_{nmn}}$	$P_{C_{can}}$	$P_{C_{nan}}$	$P_{C_{cmn}}$	$P_{C_{cam}}$	$P_{C_{nmm}}$
105	8.07/	8.38/	10.03/	8.35/	5.95/	7.81/	9.68/	8.48/
	9.07	10.31	10.58	9.05	6.19	8.18	11.28	9.92
90	12.42/	8.74/	12.25/	12.57/	5.61/	9.24/	8.79/	8.70/
	12.64	9.16	12.89	13.30	5.91	9.99	10.03	9.41
50	14.25/	10.84/	12.65/	12.63/	6.81/	9.76/	10.99/	11.51/
	14.77	11.29	12.89	12.82	7.22	10.51	11.76	11.74
20	13.51/	10.86/	14.42/	12.63/	9.28/	11.30/	12.50/	11.87/
	13.78	11.74	14.95	12.93	11.52	14.33	14.62	12.16

Table S.10. $R(\text{obs/all})$ and $wR(\text{obs/all})$ factors for magnetic Bragg reflections of $\text{Mn}_3\text{Fe}_2\text{Si}_3$ based on the neutron powder data measured on POWGEN at 50 K for a center wavelength of 2.665 Å. Magnetic space groups (MSG) were derived assuming different non-isomorphic, maximal subgroups of $C_{2/m}$ as symmetry of the nuclear structure (NP: number of parameters in the refinement).

Ama2								
MSG	$P_{Cc}2m$	$P_{Cn}2n$	$P_{Cc}2_1n$	$P_{Cn}2_1m$	$P_{Cc}2m$	$P_{Cn}2n$	$P_{Cc}2_1n$	$P_{Cn}2_1m$
$R(\text{obs/all})$	27.24/31.33	9.64/13.08	23.43/27.58	21.79/28.60	25.14/30.13	9.58/13.00	22.35/26.98	21.79/28.60
$wR(\text{obs/all})$	13.18/13.54	6.65/6.94	11.90/12.10	10.06/10.56	11.98/12.32	6.66/6.96	11.58/11.87	10.06/10.56
NP	6	9	11	8	6	9	11	8
Amm2								
MSG	P_C2mm		P_C2an		P_C2_1am		P_C2_1mn	
$R(\text{obs/all})$	26.55/30.29		9.00/12.85		19.78/28.85		19.63/28.40	
$wR(\text{obs/all})$	13.04/13.17		6.16/6.46		9.43/10.31		9.82/10.31	
NP	6		10		8		10	
Cmc2 ₁								
MSG	$P_{Ccm}2_1$		$P_{Cna}2_1$		$P_{Cnm}2_1$		$P_{Cca}2_1$	
$R(\text{obs/all})$	24.68/28.60		7.67/13.44		21.96/30.43		24.31/30.65	
$wR(\text{obs/all})$	11.57/11.82		6.24/6.44		10.29/10.69		11.60/12.10	
NP	8		9		8		9	
C222 ₁								
MSG	P_C222_1		$P_C2_12_12_1$		$P_C22_12_1$		$P_C2_122_1$	
$R(\text{obs/all})$	7.27/12.25		21.37/28.18		24.27/26.37		21.30/29.67	
$wR(\text{obs/all})$	6.20/6.30		11.07/11.85		12.09/12.18		10.58/11.22	
NP	7		10		9		8	
C2/c								
MSG	$P_{C\bar{1}}$		$P_{C\bar{1}}$		$P_{C\bar{1}}$		$P_{C\bar{1}}$	
$R(\text{obs/all})$	20.46/24.67		20.47/25.08		10.52/14.22		10.50/14.20	
$wR(\text{obs/all})$	10.84/11.13		10.94/11.25		7.05/7.33		7.05/7.32	
NP	16		16		16		16	
C2/m								
MSG	P_C2/m		P_C2_1/a		P_C2/a		P_C2_1/m	
$R(\text{obs/all})$	22.66/29.49		20.83/25.15		10.98/14.83		21.67/31.41	
$wR(\text{obs/all})$	11.09/11.39		10.62/10.92		7.35/7.59		9.95/10.49	
NP	7		10		8		9	
C2 ₁ /m								
MSG	P_C2_1/m		P_C2_1/n		P_C2_1/n		P_C2_1/m	
$R(\text{obs/all})$	22.48/26.81		10.84/14.67		20.43/25.51		24.21/34.28	
$wR(\text{obs/all})$	11.41/11.71		6.99/7.27		10.75/11.06		10.26/10.70	
NP	7		10		10		7	

Table S.11. $R(\text{obs/all})$ and $wR(\text{obs/all})$ factors for magnetic Bragg reflections of $Mn_3Fe_2Si_3$ based on the neutron powder data measured on POWGEN at 20 K for a center wavelength of 2.665 Å. Magnetic space groups (MSG) were derived assuming different non-isomorphic, maximal subgroups of $Ccmm$ as symmetry of the nuclear structure (NP: number of parameters in the refinement).

Ama2								
MSG	P_Cc2m	P_Cn2n	P_Cc2_1n	P_Cn2_1m	P_Cc2m	P_Cn2n	P_Cc2_1n	P_Cn2_1m
$R(\text{obs/all})$	24.95/32.99	10.04/18.37	25.05/33.22	30.08/47.73	24.79/31.53	12.37/20.27	22.84/26.41	23.98/35.83
$wR(\text{obs/all})$	12.68/12.97	7.55/7.75	13.45/13.75	11.91/12.76	12.23/12.39	7.86/8.03	12.66/12.81	11.09/13.35
NP	6	9	11	8	6	9	11	8
Amm2								
MSG	P_C2mm		P_C2an		P_C2_1am		P_C2_1mn	
$R(\text{obs/all})$	29.83/34.49		8.83/16.89		26.29/34.00		21.82/31.11	
$wR(\text{obs/all})$	13.54/13.62		6.49/6.82		12.13/12.34		9.72/10.20	
NP	6		10		8		10	
Cmc2 ₁								
MSG	P_Ccm2_1		P_Cna2_1		P_Cnm2_1		P_Cca2_1	
$R(\text{obs/all})$	22.79/27.72		13.23/17.35		21.25/34.93		23.97/31.42	
$wR(\text{obs/all})$	11.23/11.39		8.73/8.86		10.99/11.60		12.78/13.25	
NP	8		9		8		9	
C222 ₁								
MSG	P_C222_1		$P_C2_12_12_1$		$P_C22_12_1$		$P_C2_122_1$	
$R(\text{obs/all})$	8.02/13.42		19.29/29.72		21.06/28.31		18.29/27.98	
$wR(\text{obs/all})$	6.91/7.01		13.14/13.32		12.61/12.78		10.71/11.31	
NP	7		10		9		8	
C2/c								
MSG	$P_C\bar{1}$		$P_C\bar{1}$		$P_C\bar{1}$		$P_C\bar{1}$	
$R(\text{obs/all})$	22.16/31.17		19.85/31.69		10.62/19.67		10.77/19.23	
$wR(\text{obs/all})$	10.94/11.31		10.77/11.27		7.76/8.03		7.65/8.19	
NP	16		16		16		16	
C2/m								
MSG	P_C2/m		P_C2_1/a		P_C2/a		P_C2_1/m	
$R(\text{obs/all})$	23.38/31.07		20.97/32.97		11.73/19.82		21.92/32.86	
$wR(\text{obs/all})$	10.73/11.07		11.46/12.13		8.17/8.65		10.38/10.85	
NP	7		10		8		9	
C2 ₁ /m								
MSG	P_C2_1/m		P_C2_1/n		P_C2_1/n		P_C2_1/m	
$R(\text{obs/all})$	26.43/34.07		8.87/18.74		21.63/27.82		41.08/53.62	
$wR(\text{obs/all})$	11.95/12.20		7.33/7.53		11.23/13.06		9.69/10.05	
NP	7		10		10		7	