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Supporting information for article:

Local distortion and octahedral tilting in BaCexTi_{1-x}O₃ perovskite

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Supporting Information

Local distortion and octahedral tilting in BaCe_xTi_{1-x}O₃ perovskite

Authors

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Results and Discussion - Oxygen disorder and tilt model

The following tables report:

- Ti/Ce-oxygen bond lengths for each octahedron type obtained by tilt model.
- Average bond length, distortion index (Baur, 1974), quadratic elongation (Robinson *et al.*, 1971) and the bond angle variance (Robinson *et al.*, 1971) for each octahedron type obtained by tilt model
- Range of octahedra O-O distances obtained by tilt model
- Angle variations in the octahedra faces obtained by tilt model
- Example of comparison between isotropic thermal parameters obtained on the average and local structure (simple and tilt model).

Table S1 $x=0.05$ at 200K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near to those with cerium (TiC), those far from cerium (TiF) and those between these two last groups (TiB)). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported. Parameters of TiC and TiB groups are affected by high correlation.

$x=0.05$ 200K							
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>		<i>TiF: Ti-O</i>	
l(Ce3-O108)	2.143 Å	l(Ti3-O4)	1.915 Å	l(Ti5-O136)	2.330 Å	l(Ti4-O133)	2.049 Å
l(Ce3-O172)	2.143 Å	l(Ti3-O1)	1.772 Å	l(Ti5-O8)	2.330 Å	l(Ti4-O5)	2.049 Å
l(Ce3-O44)	2.143 Å	l(Ti3-O68)	1.813 Å	l(Ti5-O72)	2.043 Å	l(Ti4-O69)	2.049 Å
l(Ce3-O41)	2.143 Å	l(Ti3-O132)	1.813 Å	l(Ti5-O5)	1.991 Å	l(Ti4-O6)	1.989 Å
l(Ce3-O176)	2.143 Å	l(Ti3-O136)	1.772 Å	l(Ti5-O140)	1.991 Å	l(Ti4-O137)	1.989 Å
l(Ce3-O124)	2.143 Å	l(Ti3-O84)	1.77 Å	l(Ti5-O88)	1.991 Å	l(Ti4-O85)	1.989 Å
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Average bond length (Å)	2.14	Average bond length (Å)	1.81	Average bond length (Å)	2.11	Average bond length (Å)	2.02
Polyhedral volume (Å ³)	13.13	Polyhedral volume (Å ³)	7.26	Polyhedral volume (Å ³)	12.31	Polyhedral volume (Å ³)	10.88
Distortion index (bond length)	0	Distortion index (bond length)	0.02	Distortion index (bond length)	0.07	Distortion index (bond length)	0.02
Quadratic elongation	1	Quadratic elongation	1.06	Quadratic elongation	1.02	Quadratic elongation	1.00
Bond angle variance (deg. ²)	0.02	Bond angle variance (deg. ²)	167.50	Bond angle variance (deg. ²)	39.69	Bond angle variance (deg. ²)	23.03

Table S2 $x=0.05$ at 300K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near to those with cerium (TiC), those far from cerium (TiF) and those between these two last groups (TiB). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported. Parameters of TiC and TiB groups are affected by high correlation.

$x=0.05$ 300K							
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>		<i>TiF: Ti-O</i>	
l(Ce3-O108)	2.151 Å	l(Ti3-O4)	1.917 Å	l(Ti5-O136)	2.391 Å	l(Ti4-O133)	2.057 Å
l(Ce3-O172)	2.151 Å	l(Ti3-O1)	1.783 Å	l(Ti5-O8)	2.052 Å	l(Ti4-O5)	2.057 Å
l(Ce3-O44)	2.151 Å	l(Ti3-O68)	1.783 Å	l(Ti5-O72)	2.052 Å	l(Ti4-O69)	2.057 Å
l(Ce3-O41)	2.151 Å	l(Ti3-O132)	1.735 Å	l(Ti5-O5)	2.304 Å	l(Ti4-O6)	1.981 Å
l(Ce3-O176)	2.151 Å	l(Ti3-O136)	1.735 Å	l(Ti5-O140)	2.304 Å	l(Ti4-O137)	1.981 Å
l(Ce3-O124)	2.151 Å	l(Ti3-O84)	1.735 Å	l(Ti5-O88)	2.304 Å	l(Ti4-O85)	1.981 Å
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Average bond length (Å)	2.15	Average bond length (Å)	1.78	Average bond length (Å)	2.23	Average bond length (Å)	2.02
Polyhedral volume (Å ³)	13.27	Polyhedral volume (Å ³)	6.72	Polyhedral volume (Å ³)	14.26	Polyhedral volume (Å ³)	10.90
Distortion index (bond length)	0	Distortion index (bond length)	0.03	Distortion index (bond length)	0.05	Distortion index (bond length)	0.02
Quadratic elongation	1.00	Quadratic elongation	1.08	Quadratic elongation	1.03	Quadratic elongation	1.00
Bond angle variance (deg. ²)	0.29	Bond angle variance (deg. ²)	217.41	Bond angle variance (deg. ²)	97.98	Bond angle variance (deg. ²)	17.25

Table S3 $x=0.05$ at 350K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near to those with cerium (TiC), those far from cerium (TiF) and those between these two last groups (TiB). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported. Parameters of TiC and TiB groups are affected by high correlation.

$x=0.05$ 350K							
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>		<i>TiF: Ti-O</i>	
l(Ce3-O108)	2.143 Å	l(Ti3-O4)	1.921 Å	l(Ti5-O136)	2.325 Å	l(Ti4-O133)	2.046 Å
l(Ce3-O172)	2.143 Å	l(Ti3-O1)	1.786 Å	l(Ti5-O8)	2.049 Å	l(Ti4-O5)	2.046 Å
l(Ce3-O44)	2.143 Å	l(Ti3-O68)	1.828 Å	l(Ti5-O72)	2.049 Å	l(Ti4-O69)	2.046 Å
l(Ce3-O41)	2.143 Å	l(Ti3-O132)	1.828 Å	l(Ti5-O5)	2.254 Å	l(Ti4-O6)	1.988 Å
l(Ce3-O176)	2.143 Å	l(Ti3-O136)	1.786 Å	l(Ti5-O140)	2.254 Å	l(Ti4-O137)	1.988 Å
l(Ce3-O124)	2.143 Å	l(Ti3-O84)	1.786 Å	l(Ti5-O88)	2.254 Å	l(Ti4-O85)	1.988 Å
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Average bond length (Å)	2.14	Average bond length (Å)	1.82	Average bond length (Å)	2.20	Average bond length (Å)	2.02
Polyhedral volume (Å ³)	13.08	Polyhedral volume (Å ³)	7.35	Polyhedral volume (Å ³)	13.51	Polyhedral volume (Å ³)	10.93
Distortion index (bond length)	0	Distortion index (bond length)	0.02	Distortion index (bond length)	0.05	Distortion index (bond length)	0.01
Quadratic elongation	1.00	Quadratic elongation	1.07	Quadratic elongation	1.03	Quadratic elongation	1.00
Bond angle variance (deg. ²)	6.10	Bond angle variance (deg. ²)	182.40	Bond angle variance (deg. ²)	113.37	Bond angle variance (deg. ²)	4.23

Table S4 $x=0.05$ at 380K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near to those with cerium (TiC), those far from cerium (TiF) and those between these two last groups (TiB). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported. Parameters of TiC and TiB groups are affected by high correlation.

$x=0.05$ 380K							
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>		<i>TiF: Ti-O</i>	
I(Ce3-O108)	2.150 Å	I(Ti3-O4)	1.914 Å	I(Ti5-O136)	2.335 Å	I(Ti4-O133)	2.047 Å
I(Ce3-O172)	2.150 Å	I(Ti3-O1)	1.776 Å	I(Ti5-O8)	2.047 Å	I(Ti4-O5)	2.047 Å
I(Ce3-O44)	2.15 Å	I(Ti3-O68)	1.818 Å	I(Ti5-O72)	2.047 Å	I(Ti4-O69)	2.047 Å
I(Ce3-O41)	2.150 Å	I(Ti3-O132)	1.8178 Å	I(Ti5-O5)	2.264 Å	I(Ti4-O6)	1.988 Å
I(Ce3-O176)	2.150 Å	I(Ti3-O136)	1.776 Å	I(Ti5-O140)	2.264 Å	I(Ti4-O137)	1.988 Å
I(Ce3-O124)	2.150 Å	I(Ti3-O84)	1.776 Å	I(Ti5-O88)	2.264 Å	I(Ti4-O85)	1.988 Å
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Average bond length (Å)	2.15	Average bond length (Å)	1.81	Average bond length (Å)	2.20	Average bond length (Å)	2.02
Polyhedral volume (Å ³)	13.19	Polyhedral volume (Å ³)	7.23	Polyhedral volume (Å ³)	13.68	Polyhedral volume (Å ³)	10.94
Distortion index (bond length)	0	Distortion index (bond length)	0.02	Distortion index (bond length)	0.05	Distortion index (bond length)	0.02
Quadratic elongation	1.00	Quadratic elongation	1.07	Quadratic elongation	1.03	Quadratic elongation	1.00
Bond angle variance (deg. ²)	11.85	Bond angle variance (deg. ²)	184.25	Bond angle variance (deg. ²)	100.69	Bond angle variance (deg. ²)	1.64

Table S5 $x=0.05$ at 420K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near to those with cerium (TiC), those far from cerium (TiF) and those between these two last groups (TiB). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported. Parameters of Tic and TiB groups are affected by high correlation.

$x=0.05$ 420K							
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>		<i>TiF: Ti-O</i>	
I(Ce3-O108)	2.145 Å	I(Ti3-O4)	1.923 Å	I(Ti5-O136)	2.302 Å	I(Ti4-O133)	2.047 Å
I(Ce3-O172)	2.145 Å	I(Ti3-O1)	1.810 Å	I(Ti5-O8)	2.047 Å	I(Ti4-O5)	2.047 Å
I(Ce3-O44)	2.145 Å	I(Ti3-O68)	1.852 Å	I(Ti5-O72)	2.047 Å	I(Ti4-O69)	2.047 Å
I(Ce3-O41)	2.145 Å	I(Ti3-O132)	1.852 Å	I(Ti5-O5)	2.232 Å	I(Ti4-O6)	1.989 Å
I(Ce3-O176)	2.145 Å	I(Ti3-O136)	1.810 Å	I(Ti5-O140)	2.232 Å	I(Ti4-O137)	1.989 Å
I(Ce3-O124)	2.145 Å	I(Ti3-O84)	1.810 Å	I(Ti5-O88)	2.232 Å	I(Ti4-O85)	1.989 Å
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Average bond length (Å)	2.14	Average bond length (Å)	1.84	Average bond length (Å)	2.18	Average bond length (Å)	2.02
Polyhedral volume (Å ³)	13.03	Polyhedral volume (Å ³)	7.59	Polyhedral volume (Å ³)	13.27	Polyhedral volume (Å ³)	10.95
Distortion index (bond length)	0	Distortion index (bond length)	0.02	Distortion index (bond length)	0.04	Distortion index (bond length)	0.01
Quadratic elongation	1.01	Quadratic elongation	1.07	Quadratic elongation	1.03	Quadratic elongation	1.00
Bond angle variance (deg. ²)	22.74	Bond angle variance (deg. ²)	183.29	Bond angle variance (deg. ²)	105.37	Bond angle variance (deg. ²)	1.63

Table S6 $x=0.10$ at 100K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near (TiC) and those not near (TiB) to cerium polyhedra). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.10$ 100K					
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>	
l(Ce5-O108)	2.139 Å	l(Ti25-O92)	2.051 Å	l(Ti22-O88)	2.062 Å
l(Ce5-O172)	2.13 Å	l(Ti25-O156)	2.051 Å	l(Ti22-O152)	2.062 Å
l(Ce5-O44)	2.139 Å	l(Ti25-O28)	2.051 Å	l(Ti22-O24)	2.062 Å
l(Ce5-O41)	2.139 Å	l(Ti25-O25)	2.018 Å	l(Ti22-O21)	2.016 Å
l(Ce5-O176)	2.139 Å	l(Ti25-O160)	2.018 Å	l(Ti22-O156)	2.016 Å
l(Ce5-O124)	2.139 Å	l(Ti25-O108)	1.890 Å	l(Ti22-O104)	2.016 Å
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Average bond length (Å)	2.14	Average bond length (Å)	2.01	Average bond length (Å)	2.04
Polyhedral volume (Å ³)	13.06	Polyhedral volume (Å ³)	10.62	Polyhedral volume (Å ³)	10.88
Distortion index (bond length)	0	Distortion index (bond length)	0.02	Distortion index (bond length)	0.01
Quadratic elongation	1	Quadratic elongation	1.02	Quadratic elongation	1.03
Bond angle variance (deg. ²)	0.01	Bond angle variance (deg. ²)	51.22	Bond angle variance (deg. ²)	99.20

Table S7 $x=0.10$ at 200K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near (TiC) and those not near (TiB) to cerium polyhedra). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.10$ 200K					
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>	
l(Ce5-O108)	2.169 Å	l(Ti25-O92)	2.061 Å	l(Ti22-O88)	2.076 Å
l(Ce5-O172)	2.169 Å	l(Ti25-O156)	2.061 Å	l(Ti22-O152)	2.076 Å
l(Ce5-O44)	2.169 Å	l(Ti25-O28)	2.061 Å	l(Ti22-O24)	2.076 Å
l(Ce5-O41)	2.169 Å	l(Ti25-O25)	2.010 Å	l(Ti22-O21)	2.006 Å
l(Ce5-O176)	2.169 Å	l(Ti25-O160)	2.010 Å	l(Ti22-O156)	2.006 Å
l(Ce5-O124)	2.169 Å	l(Ti25-O108)	1.853 Å	l(Ti22-O104)	2.006 Å
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Average bond length (Å)	2.169	Average bond length (Å)	2.01	Average bond length (Å)	2.04
Polyhedral volume (Å ³)	13.60	Polyhedral volume (Å ³)	10.58	Polyhedral volume (Å ³)	10.91
Distortion index (bond length)	0	Distortion index (bond length)	0.03	Distortion index (bond length)	0.02
Quadratic elongation	1	Quadratic elongation	1.02	Quadratic elongation	1.03
Bond angle variance (deg. ²)	0.01	Bond angle variance (deg. ²)	48.06	Bond angle variance (deg. ²)	95.65

Table S8 $x=0.10$ at 300K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near (TiC) and those not near (TiB) to cerium polyhedra). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.10$ 300K					
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>	
l(Ce5-O108)	2.166 Å	l(Ti25-O92)	2.059 Å	l(Ti22-O88)	2.072 Å
l(Ce5-O172)	2.166 Å	l(Ti25-O156)	2.059 Å	l(Ti22-O152)	2.072 Å
l(Ce5-O44)	2.166 Å	l(Ti25-O28)	2.059 Å	l(Ti22-O24)	2.072 Å
l(Ce5-O41)	2.166 Å	l(Ti25-O25)	2.015 Å	l(Ti22-O21)	2.012 Å
l(Ce5-O176)	2.166 Å	l(Ti25-O160)	2.015 Å	l(Ti22-O156)	2.012 Å
l(Ce5-O124)	2.166 Å	l(Ti25-O108)	1.864 Å	l(Ti22-O104)	2.012 Å

Average bond length (Å)	2.17	Average bond length (Å)	2.01	Average bond length (Å)	2.04
Polyhedral volume (Å ³)	13.54	Polyhedral volume (Å ³)	10.61	Polyhedral volume (Å ³)	10.93
Distortion index (bond length)	0	Distortion index (bond length)	0.03	Distortion index (bond length)	0.02
Quadratic elongation	1	Quadratic elongation	1.02	Quadratic elongation	1.03
Bond angle variance (deg. ²)	0.00	Bond angle variance (deg. ²)	48.60	Bond angle variance (deg. ²)	98.51

Table S9 $x=0.10$ at 400K (tilt model): characterization of cerium octahedra and titanium octahedra groups (Ti octahedra near (TiC) and those not near (TiB) to cerium polyhedra). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.10$ 400K					
<i>Ce-O</i>		<i>TiC: Ti-O</i>		<i>TiB: Ti-O</i>	
l(Ce5-O108)	2.186 Å	l(Ti25-O92)	2.066 Å	l(Ti22-O88)	2.080 Å
l(Ce5-O172)	2.186 Å	l(Ti25-O156)	2.066 Å	l(Ti22-O152)	2.080 Å
l(Ce5-O44)	2.186 Å	l(Ti25-O28)	2.066 Å	l(Ti22-O24)	2.080 Å
l(Ce5-O41)	2.186 Å	l(Ti25-O25)	2.008 Å	l(Ti22-O21)	2.004 Å
l(Ce5-O176)	2.186 Å	l(Ti25-O160)	2.008 Å	l(Ti22-O156)	2.004 Å
l(Ce5-O124)	2.186 Å	l(Ti25-O108)	1.841 Å	l(Ti22-O104)	2.004 Å

Average bond length (Å)	2.19	Average bond length (Å)	2.01	Average bond length (Å)	2.04
Polyhedral volume (Å ³)	13.88	Polyhedral volume (Å ³)	10.62	Polyhedral volume (Å ³)	10.98
Distortion index (bond length)	0	Distortion index (bond length)	0.03	Distortion index (bond length)	0.02
Quadratic elongation	1.00	Quadratic elongation	1.01	Quadratic elongation	1.02
Bond angle variance (deg. ²)	7.87	Bond angle variance (deg. ²)	37.48	Bond angle variance (deg. ²)	86.61

Table S10 $x=0.20$ at 100K (tilt model): characterization of cerium octahedra and titanium octahedra (TiC). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.20$ 100K			
<i>Ce-O</i>		<i>TiC: Ti-O</i>	
l(Ce2-O16)	2.152 Å	l(Ti1-O2)	1.939 Å
l(Ce2-O24)	2.152 Å	l(Ti1-O10)	2.075 Å
l(Ce2-O8)	2.152 Å	l(Ti1-O18)	2.075 Å
l(Ce2-O7)	2.152 Å	l(Ti1-O1)	1.949 Å
l(Ce2-O22)	2.152 Å	l(Ti1-O20)	2.075 Å
l(Ce2-O12)	2.152 Å	l(Ti1-O14)	2.075 Å
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Average bond length (Å)	2.15	Average bond length (Å)	2.03
Polyhedral volume (Å ³)	13.27	Polyhedral volume (Å ³)	10.86
Distortion index (bond length)	0	Distortion index (bond length)	0.03
Quadratic elongation	1.00	Quadratic elongation	1.02
Bond angle variance (deg. ²)	4.28	Bond angle variance (deg. ²)	65.81

Table S11 $x=0.20$ at 200K (tilt model): characterization of cerium octahedra and titanium octahedra (TiC). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.20$ 200K			
<i>Ce-O</i>		<i>TiC: Ti-O</i>	
l(Ce2-O16)	2.154 Å	l(Ti1-O2)	1.940 Å
l(Ce2-O24)	2.154 Å	l(Ti1-O10)	2.074 Å
l(Ce2-O8)	2.154 Å	l(Ti1-O18)	2.074 Å
l(Ce2-O7)	2.154 Å	l(Ti1-O1)	1.946 Å
l(Ce2-O22)	2.154 Å	l(Ti1-O20)	2.071 Å
l(Ce2-O12)	2.154 Å	l(Ti1-O14)	2.071 Å
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Average bond length (Å)	2.15	Average bond length (Å)	2.03
Polyhedral volume (Å ³)	13.32	Polyhedral volume (Å ³)	10.87
Distortion index (bond length)	0	Distortion index (bond length)	0.03
Quadratic elongation	1.00	Quadratic elongation	1.02
Bond angle variance (deg. ²)	0.82	Bond angle variance (deg. ²)	55.12

Table S12 $x=0.20$ at 300K (tilt model): characterization of cerium octahedra and titanium octahedra (TiC). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.20$ 300K			
<i>Ce-O</i>		<i>TiC: Ti-O</i>	
l(Ce2-O16)	2.165 Å	l(Ti1-O2)	2.081 Å
l(Ce2-O24)	2.165 Å	l(Ti1-O10)	2.081 Å
l(Ce2-O8)	2.165 Å	l(Ti1-O18)	1.931 Å
l(Ce2-O7)	2.165 Å	l(Ti1-O1)	1.940 Å
l(Ce2-O22)	2.165 Å	l(Ti1-O20)	2.063 Å
l(Ce2-O12)	2.165 Å	l(Ti1-O14)	2.063 Å
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Average bond length (Å)	2.17	Average bond length (Å)	2.03
Polyhedral volume (Å ³)	13.53	Polyhedral volume (Å ³)	10.84
Distortion index (bond length)	0	Distortion index (bond length)	0.03
Quadratic elongation	1	Quadratic elongation	1.02
Bond angle variance (deg. ²)	0.12	Bond angle variance (deg. ²)	50.72

Table S13 $x=0.20$ at 400K (tilt model): characterization of cerium octahedra and titanium octahedra (TiC). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.20$ 400K			
<i>Ce-O</i>		<i>TiC: Ti-O</i>	
l(Ce2-O16)	2.176 Å	l(Ti1-O2)	2.081 Å
l(Ce2-O24)	2.176 Å	l(Ti1-O10)	2.081 Å
l(Ce2-O8)	2.176 Å	l(Ti1-O18)	1.924 Å
l(Ce2-O7)	2.176 Å	l(Ti1-O1)	1.932 Å
l(Ce2-O22)	2.176 Å	l(Ti1-O20)	2.064 Å
l(Ce2-O12)	2.176 Å	l(Ti1-O14)	2.064 Å
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Average bond length (Å)	2.176	Average bond length (Å)	2.02
Polyhedral volume (Å ³)	13.73	Polyhedral volume (Å ³)	10.82
Distortion index (bond length)	0	Distortion index (bond length)	0.03
Quadratic elongation	1	Quadratic elongation	1.02
Bond angle variance (deg. ²)	0.17	Bond angle variance (deg. ²)	47.87

Table S14 $x=0.30$ at 100K (tilt model): characterization of cerium octahedra and titanium octahedra (TiC). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.30$ 100K			
<i>Ce-O</i>		<i>TiC: Ti-O</i>	
l(Ce2-O16)	2.240 Å	l(Ti1-O2)	1.890 Å
l(Ce2-O24)	2.240 Å	l(Ti1-O10)	1.901 Å
l(Ce2-O8)	2.240 Å	l(Ti1-O18)	1.901 Å
l(Ce2-O7)	2.240 Å	l(Ti1-O1)	1.890 Å
l(Ce2-O22)	2.240 Å	l(Ti1-O20)	1.901 Å
l(Ce2-O12)	2.240 Å	l(Ti1-O14)	1.890 Å
-----		-----	
Average bond length (Å)	2.24	Average bond length (Å)	1.90
Polyhedral volume (Å ³)	14.89	Polyhedral volume (Å ³)	9.04
Distortion index (bond length)	0	Distortion index (bond length)	0.00
Quadratic elongation	1.00	Quadratic elongation	1.00
Bond angle variance (deg. ²)	14.82	Bond angle variance (deg. ²)	9.58

Table S15 $x=0.30$ at 200K (tilt model): characterization of cerium octahedra and titanium octahedra (TiC). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.30$ 200K			
<i>Ce-O</i>		<i>TiC: Ti-O</i>	
l(Ce2-O16)	2.220 Å	l(Ti1-O2)	1.917 Å
l(Ce2-O24)	2.220 Å	l(Ti1-O10)	1.925 Å
l(Ce2-O8)	2.220 Å	l(Ti1-O18)	1.925 Å
l(Ce2-O7)	2.220 Å	l(Ti1-O1)	1.917 Å
l(Ce2-O22)	2.220 Å	l(Ti1-O20)	1.925 Å
l(Ce2-O12)	2.220 Å	l(Ti1-O14)	1.917 Å
-----		-----	
Average bond length (Å)	2.22	Average bond length (Å)	1.92
Polyhedral volume (Å ³)	14.41	Polyhedral volume (Å ³)	9.37
Distortion index (bond length)	0	Distortion index (bond length)	0.00
Quadratic elongation	1.00	Quadratic elongation	1.00
Bond angle variance (deg. ²)	29.01	Bond angle variance (deg. ²)	21.54

Table S16 $x=0.30$ at 300K (tilt model): characterization of cerium octahedra and titanium octahedra (TiC). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.30$ 300K			
<i>Ce-O</i>		<i>TiC: Ti-O</i>	
l(Ce2-O16)	2.191 Å	l(Ti1-O2)	1.958 Å
l(Ce2-O24)	2.191 Å	l(Ti1-O10)	1.954 Å
l(Ce2-O8)	2.191 Å	l(Ti1-O18)	1.954 Å
l(Ce2-O7)	2.191 Å	l(Ti1-O1)	1.958 Å
l(Ce2-O22)	2.191 Å	l(Ti1-O20)	1.954 Å
l(Ce2-O12)	2.191 Å	l(Ti1-O14)	1.958 Å
-----		-----	
Average bond length (Å)	2.19	Average bond length (Å)	1.96
Polyhedral volume (Å ³)	13.79	Polyhedral volume (Å ³)	9.84
Distortion index (bond length)	0	Distortion index (bond length)	0.00
Quadratic elongation	1.01	Quadratic elongation	1.00
Bond angle variance (deg. ²)	43.23	Bond angle variance (deg. ²)	31.99

Table S17 $x=0.30$ at 400K (tilt model): characterization of cerium octahedra and titanium octahedra (TiC). Ce/Ti bond lengths, average Ce/Ti bond lengths, polyhedra volume, distortion index, quadratic elongation and bond angle variance are reported.

$x=0.30$ 400K			
<i>Ce-O</i>		<i>TiC: Ti-O</i>	
l(Ce2-O16)	2.119 Å	l(Ti1-O2)	2.035 Å
l(Ce2-O24)	2.119 Å	l(Ti1-O10)	2.044 Å
l(Ce2-O8)	2.119 Å	l(Ti1-O18)	2.044 Å
l(Ce2-O7)	2.119 Å	l(Ti1-O1)	2.035 Å
l(Ce2-O22)	2.119 Å	l(Ti1-O20)	2.044 Å
l(Ce2-O12)	2.119 Å	l(Ti1-O14)	2.035 Å
-----		-----	
Average bond length (Å)	2.12	Average bond length (Å)	2.034
Polyhedral volume (Å ³)	12.32	Polyhedral volume (Å ³)	11.06
Distortion index (bond length)	0	Distortion index (bond length)	0.00
Quadratic elongation	1.02	Quadratic elongation	1.02
Bond angle variance (deg. ²)	76.01	Bond angle variance (deg. ²)	50.61

Table S18 Range of octahedra oxygen-oxygen bond distances obtained refining different data set by tilt model. Values obtained by referenced BaTiO₃ rhombohedral structure at 100K (Kwei *et al.*, 1993) are also reported. Values in $x=0.05$, are affected by the high correlation of some oxygen parameters as explained in the text.

BaTiO ₃		x=0.05		x=0.10		x=0.20		x=0.30	
Temp. (K)	Distance range (Å)	Temp. (K)	Distance range (Å)	Temp. (K)	Distance range (Å)	Temp. (K)	Distance range (Å)	Temp. (K)	Distance range (Å)
100	2.78-2.88	200	2.21-3.17	100	2.63-3.11	100	2.54-3.29	100	2.61-3.27
		300	2.12-3.23	200	2.64-3.11	200	2.57-3.26	200	2.61-3.28
		350	2.22-3.25	300	2.64-3.12	300	2.59-3.24	300	2.63-3.26
		380	2.21-3.23	400	2.57-3.20	400	2.603.23	400	2.71-3.21
		420	2.25-3.21						

Table S19 Angle variations in the octahedra faces obtained refining different data set by tilt model. Values obtained by referenced BaTiO₃ rhombohedral structure at 100K (Kwei *et al.*, 1993) are also reported. Values in $x=0.05$, are affected by the high correlation of some oxygen parameters as explained in the text.

BaTiO ₃		x=0.05		x=0.10		x=0.20		x=0.30	
Temp. (K)	Angle range (°)	Temp. (K)	Angle range (°)	Temp. (K)	Angle range (°)	Temp. (K)	Angle range (°)	Temp. (K)	Angle range (°)
100	58.66-60.95	200	48.07-80.77	100	50.07-70.29	100	49.39-73.21	100	55.92-63.53
		300	46.31-82.62	200	50.26-69.93	200	50.34-72.58	200	54.38-65.41
		350	47.81-80.01	300	50.11-70.01	300	50.55-72.11	300	53.22-66.68
		380	47.78-79.93	400	50.70-69.13	400	50.68-71.90	400	51.19-68.56
		420	48.44-79.62						

Table S20 Comparison of isotropic thermal parameter values obtained on the average structure and on the local (simple and tilt model) for the sample $x=0.10$.

x=0.10	Temp. (K)	Uiso Ba (Å ²)	Uiso Ti (Å ²)	Uiso Ce (Å ²)	Uiso O (Å ²)
Average	100 K	0.003(4)	0.006(1)	0.006(1)	0.0101(5)
Local simple model		0.003(3)	0.005(1)	0.03(3)	0.02(1)
Local tilt model		0.003(3)	0.005(2)	0.009(1)	0.014(3)
Average	200 K	0.0055(5)	0.008(1)	0.008(1)	0.0124(1)
Local simple model		0.004(4)	0.004(1)	0.03(4)	0.02(1)
Local tilt model		0.004(3)	0.006(9)	0.008(4)	0.015(3)
Average	300 K	0.0073(8)	0.009(4)	0.009(4)	0.009(1)
Local simple model		0.005(8)	0.005(7)	0.009(3)	0.026(1)
Local tilt model		0.005(5)	0.008(1)	0.009(3)	0.015(4)
Average	400 K	0.0098(5)	0.0125(1)	0.0125(1)	0.0196(4)
Local simple model		0.007(1)	0.009(6)	0.006(2)	0.025(6)
Local tilt model		0.006(7)	0.008(2)	0.009(3)	0.015(4)

References of Supporting Information

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