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Supplementary Material:

1. Examples of calculations

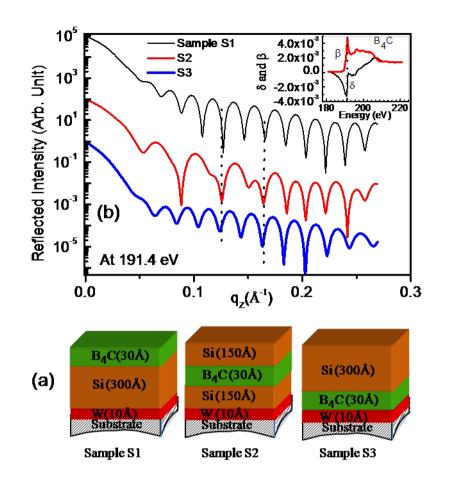
This supporting material presents the results of calculations by taking an example of partially decomposed B₄C thin films sandwich with Si. The case simulation study of multicomponent system is realized in practical B₄C films also, due to presence of unknown amount of decomposition/impurity during synthesis of films and/or generally films may get contaminated to different level basically with oxygen while exposed to ambient conditions.

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10 1.1 Sensitivity to low contrast interface

In order to study microstructural parameters at low contrast Si/B₄C interface system by 11 simulation, three different ideal thin film structures are chosen with varying spatial position 12 of B₄C layer in Si as shown in Fig. I (a). The position of B₄C layer (30 Å) is at top, middle 13 and bottom of Si in Samples S1, S2 and S3, respectively. A thin layer (10Å) of W is kept just 14 above the Si substrate in all three samples to provide contrast between underlying substrate 15 and overlying Si/B₄C layers as well to isolate substrate effect in calculated R-SoXR profiles. 16 For simulation, we choose energy 194.1 eV near B K-edge of B₄C where the optical 17 18 constants of B₄C exhibit strong variation as marked by vertical dotted lines in inset. Fig. I(b) shows simulated R-SoXR spectra from three different samples. As the spatial position of the 19 20 B₄C layer varies in Si the entire R-SoXR profile get modulated due to strong scattering from Si/B₄C interface. Two dotted lines in Fig. I(b) represent guide to show how interference 21 22 oscillations modulated in S1, S2 and S3. The modulation in amplitude of oscillation in S2 is significantly different as expected due to two interfaces via Si-on-B₄C and B₄C-on-Si 23 24 compared to S1 and S2 where only one interface is present i.e. B₄C-on-Si in S1 and Si-on-B₄C in S2. The simulated spectra clearly demonstrate R-SoXR is highly sensitivity to spatial 25 26 variation of the low contrast interface even if the ideal electron density contrast at Si/B₄C interface is very poor, $\Delta \rho / \rho = -0.05\%$. 27

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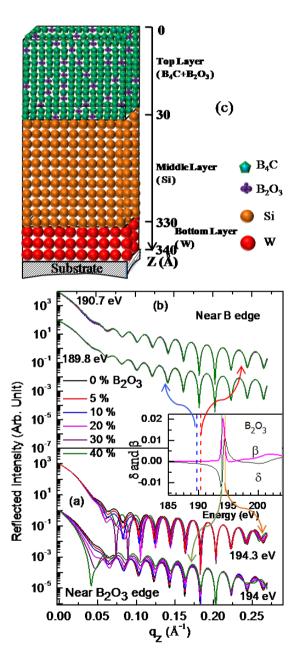
33 Figure I

34	(a) Represents the schematic layer structure of three different ideal (zero roughness) samples
35	with varying spatial position of B_4C layer in Si. The position of B_4C is at top, middle and
36	bottom of Si in Samples S1, S2 and S3, respectively. (b) Simulated R-SoXR spectra at B K-
37	edge of B ₄ C (191.4 eV) demonstrating sensitivity to low contrast Si/B ₄ C interface. Two dotted
38	lines represent guide to show how interference oscillations modulated for S1, S2 and S3. Inset
39	shows measured optical constants (δ and β) of B4C near B K-edge, the vertical dotted line
40	represents the energy at which the simulated spectra are presented.

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42 1.2 Sensitivity to atomic composition

Here we demonstrate the sensitivity of R-SoXR to the variation in atomic percent through simulations on ideal sample S1 where B₄C layer is at top of Si. Fig. II (c) shows a schematic diagram where different percent of B₂O₃ are uniformly distributed in top B₄C layer. In Fig. II (a), simulations are performed at two selected energies (194 and 194.3 eV) near B K-edge of B₂O₃ such that at these energies B₂O₃ exhibits a strong variation in optical constants as shown by two vertical lines in inset. As the content of B₂O₃ varies in B₄C, the simulated spectral features vary significantly at these energies. Even by mixing 5 % of B_2O_3 brings significant change in optical properties of the B₄C layer which is sufficient to be observed through scattered profile (*e.g.* at 194 eV, δ changes from -4.53 ×10⁻⁴ to -8.33 ×10⁻⁴ and β changes from 2.62 ×10⁻³ to 3.41 ×10⁻³). However, in Fig. II (b), near B K-edge of elementary boron, simulated profiles undergo negligible changes by incorporation of different at. % of B₂O₃. Thus low sensitivity to B₂O₃ at these energies (189.8 and 190.7 eV) is expected due to nearly flat optical behavior of B₂O₃ which are marked by two vertical dashed lines in inset.



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57 Figure II

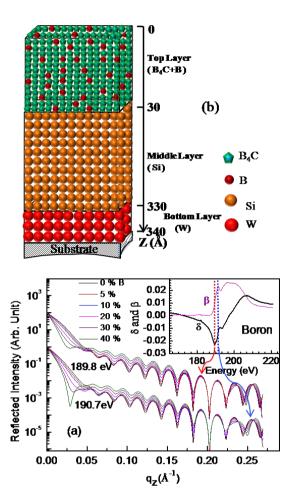
58 Simulated R-SoXR profiles at different photon energies near different absorption edges for an 59 ideal (zero roughness) thin film structures. (c) Schematic diagram of layer structure used in 60 simulation where top B₄C layer is mixed with different atomic percent of B₂O₃. (a) Simulated 61 profiles at two different selected energies near B K-edge of B₂O₃. The data at different 62 energies are vertically shifted for clarity. (b) Simulated profiles at two different selected 63 energies near B K-edge of elementary boron. Inset shows measured optical constants of B₂O₃ 64 near B K-edge.

Similar to the sensitivity of R-SoXR to variation of content of B₂O₃ in B₄C layer near 66 67 B K-edge of B₂O₃ that of elementary boron can be probe near B K-edge of elementary boron as demonstrated in Fig. III. Fig. III (b) shows a schematic diagram of ideal sample S1 where 68 69 different percent of boron are uniformly distributed in top B₄C layer. In Fig. III (a), simulations are performed at two selected energies (189.8 and 190.7 eV) near B K-edge of 70 elementary boron such that at these energies boron exhibits a strong variation in optical 71 constants as shown by two vertical dotted lines in inset. As the content of B varies in B₄C, the 72 simulated spectral features vary significantly at these energies. Even by mixing 5 % of B 73 brings significant change in optical properties of the B₄C layer which is sufficient to be 74 observed through scattered profile (e.g. at 189.8 eV, δ changes from -2.59 ×10⁻³ to -3.59 75 $\times 10^{-3}$ and β changes from 6.95 $\times 10^{-4}$ to 1.34 $\times 10^{-3}$). Thus, sensitive of the simulated resonant 76 77 reflectivity profile to the variations of few at. % provides information to probe atomic compositions in the experimentally grown films by tuning energy to the respective absorption 78 edges. 79

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83 Figure III

(a) Simulated R-SoXR profiles at selected two different photon energies near B K-edge of elementary boron for an ideal (zero roughness) thin film structures. (b) Schematic diagram of layer structure used in simulation where top B_4C layer is mixed with different atomic percent of B. Simulated data at different energies are vertically shifted for clarity. Inset shows, measured optical constants of B near B K-edge.