

Supplementary material: Structural building principles of complex face-centered cubic intermetallics

Julia Dshemuchadse, Daniel Y. Jung and Walter Steurer*

Laboratory of Crystallography, Department of Materials, ETH Zurich, Wolfgang-Pauli-Strasse 10, 8093 Zurich, Switzerland
Correspondence e-mail: steurer@mat.ethz.ch

Submitted to *Acta Crystallographica B*, 14 February 2011

1. Atomic sites – Superstructure description

Table 1

Symmetry relations between basic and modulated structures.

$F43m$	$cF16$	→ maximal non-isomorphic subgroup	$\vec{a}' = 3\vec{a}$	index 27 → $F43m$	$cF464$
$Fd\bar{3}m$	$cF16$	→ maximal non-isomorphic subgroup (& origin shift $-(\frac{1}{4}, \frac{1}{4}, \frac{1}{4})$ with origin choice 1)	$\vec{a}' = 3\vec{a}$	index 27 → $Fd\bar{3}m$	$cF464$
$P43m$	$cP16$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}' = 2\vec{a}$	index 2 → $F43m$	$cF128$
$F\bar{4}3m$	$cF128$	→ maximal isomorphic subgroup (loss of centering)	-	index 4 → $P\bar{4}3m$	$cP128$
$P\bar{4}3m$	$cP128$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}'' = 2\vec{a}'$	index 2 → $F\bar{4}3m$	$cF1024$
$Pm\bar{3}m$	$cP16$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}' = 2\vec{a}$	index 2 → $Fm\bar{3}m$	$cF128$
$Fm\bar{3}m$	$cF128$	→ maximal isomorphic subgroup (loss of centering)	-	index 4 → $Pn\bar{3}m$	$cP128$
$Pn\bar{3}m$	$cP128$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}'' = 2\vec{a}'$	index 2 → $Fd\bar{3}m$	$cF1024$
$Pm\bar{3}m$	$cP16$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}' = 2\vec{a}$	index 2 → $Fm\bar{3}m$	$cF128$
$Fm\bar{3}m$	$cF128$	→ maximal isomorphic subgroup (loss of centering)	-	index 4 → $Pm\bar{3}m$	$cP128$
$Pm\bar{3}m$	$cP128$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}'' = 2\vec{a}'$	index 2 → $Fm\bar{3}m$	$cF1024$
$Pm\bar{3}m$	$cP16$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}' = 2\vec{a}$	index 2 → $Fm\bar{3}m$	$cF128$
$Fm\bar{3}m$	$cF128$	→ maximal isomorphic subgroup (loss of centering)	-	index 4 → $Pm\bar{3}m$	$cP128$
$Pm\bar{3}m$	$cP128$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}'' = 2\vec{a}'$	index 2 → $Fm\bar{3}c$	$cF1024$
$Pm\bar{3}$	$cP16$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}' = 2\vec{a}$	index 2 → $Fm\bar{3}$	$cF128$
$Fm\bar{3}$	$cF128$	→ maximal isomorphic subgroup (loss of centering)	-	index 4 → $Pn\bar{3}$	$cP128$
$Pn\bar{3}$	$cP128$	→ maximal non-isomorphic subgroup (<i>klassengleich</i>)	$\vec{a}'' = 2\vec{a}'$	index 2 → $Fd\bar{3}$	$cF1024$

The basic structures of all cubic compounds discussed in this work correspond to a $cF16$ -NaTl structure ($Fd\bar{3}m$, *ab*) or to derivatives of it, which exhibit lower symmetry.

The average structure of the $cF464$ -structures in $F\bar{4}3m$ preserve the space group symmetry the basic structure contains four Wyckoff positions, each one resulting from six Wyckoff positions of the original structure:

- site 1 – $4a$ 0, 0, 0 ⇐ $4a$, 16e3, 16e6, 24f2, 48h1, 48h6;
- site 2 – $4c$ $\frac{1}{4}, \frac{1}{4}, \frac{1}{4}$ ⇐ $4d$, 16e2, 16e5, 24g1, 48h4, 48h5;
- site 3 – $4b$ $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$ ⇐ $4b$, 16e1, 16e8, 24f1, 48h3, 48h8;
- site 4 – $4d$ $\frac{3}{4}, \frac{3}{4}, \frac{3}{4}$ ⇐ $4c$, 16e4, 16e7, 24g2, 48h2, 48h7.

The average structure of the $cF464$ -structures in $Fd\bar{3}m$ also exhibit the same symmetry as the original structures. The Wyckoff positions of the basic structure and the corresponding ones in the original unit cell are the following¹:

- site 1 – $8a$ 0, 0, 0 ⇐ $8b$, 32e1, 32e2, 96g2, 96g3;
- site 2 – $8b$ $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$ ⇐ $8a$, 96g1, 96g4.

The average structure of $cF1124$ -Cu_{56.9}Cd_{43.1} ($F\bar{4}3m$) has space group symmetry $P\bar{4}3m$. The atomic sites of the basic structure are: 1a 0, 0, 0; 1b $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$; 3c 0, $\frac{1}{2}, \frac{1}{2}$; 3d $\frac{1}{2}, 0, 0$; 4e x, x, x ($x = \frac{1}{4}$); 4e x, x, x ($x = \frac{3}{4}$).

The average structures of $cF(1192-40)$ -Cd_{66.7}Na_{33.3} and $cF(1192-23)$ -Al_{53.6}Mg_{46.4} ($Fd\bar{3}m$) has space group symmetry $Pm\bar{3}m$. The atomic sites of the basic structure are: 1a 0, 0, 0; 1b $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$; 3c 0, $\frac{1}{2}, \frac{1}{2}$; 3d $\frac{1}{2}, 0, 0$; 8g x, x, x ($x = \frac{1}{4}$). The symmetry and sites are the same for the (4 × 4 × 4)-fold superstructures in space groups $Fm\bar{3}m$ and $Fm\bar{3}c$.

The average structure of the (4 × 4 × 4)-fold superstructure in space group $Fd\bar{3}$ has space group symmetry $Pm\bar{3}$. The atomic sites of the basic structure are: 1a 0, 0, 0; 1b $\frac{1}{2}, \frac{1}{2}, \frac{1}{2}$; 3c 0, $\frac{1}{2}, \frac{1}{2}$; 3d $\frac{1}{2}, 0, 0$; 8g x, x, x ($x = \frac{1}{4}$)².

¹ The classification of sites 96g2 and 96g4 is slightly ambiguous, since they have similar distances to both, sites 1 and 2 of the basic structure.

² The coordinates of the Wyckoff positions are the same as in space group $Pm\bar{3}m$ (see above), but their site symmetry is lower.

2. Symmetry relations

Table 2

Details on the structure types between $cI2$ -W and the investigated complex intermetallic structures. Space groups in parentheses belong to the same lattice complex / exhibit the same Wyckoff coordinates.

Structure type	Pearson symbol	Space group	Wyckoff sequence	Represented structures	Comments
W	$cI2$	$Im\bar{3}m$	a	$Im\bar{3}m - cI2, (Pn\bar{3}m - cP2)$	
CsCl	$cP2$	$Pm\bar{3}m$	ab	$Pm\bar{3}m - cP2, (P\bar{4}3m - cP2)$	
$Fe_{15}Ge_3^\dagger$	$cP16$	$Pm\bar{3}m$	$abcdg$	$Pm\bar{3}m - cP16, (Pm\bar{3} - cP16)$	
$CuHg_2Ti$	$cF16$	$F\bar{4}3m$	$abcd$	$F\bar{4}3m - cF16$	
$NaTl$	$cF16$	$Fd\bar{3}m$	ab	$Fd\bar{3}m - cF16$	
Ir_4Sc_{11}	$cF120$	$F\bar{m}\bar{3}m$	$abdef^2$	$F\bar{m}\bar{3}m - cF128, (Fm\bar{3} - cF128)$	+ site c
$Ti_6Co_7Al_{17}$	$cF120$	$F\bar{4}3m$	abe^4fg	$F\bar{4}3m - cF128$	+ sites cd
Tl_7Sb_2	$cI54$	$Im\bar{3}m$	$aefh$	$Im\bar{3}m - cI54$	
Al_4Cu_9	$cP52$	$P\bar{4}3m$	e^4fgi^2	$P\bar{4}3m - cP54$	+ sites ab
Cu_5Zn_8	$cI52$	$I\bar{4}3m$	$(e^2gk)^\ddagger$	$(Pn\bar{3}m - cP52)$	+ site a

\dagger $Fe_{15}Co$ and Fe_9Co_7 exhibit the same Wyckoff sequence with different occupations due to a differing composition.

\ddagger These sites refer to space group $Pn\bar{3}m$. The Wyckoff sequence in space group $I\bar{4}3m$ is c^2eg .

Table 3

Wyckoff sites in space group $Im\bar{3}m$ of the Bärnighausen tree, $cI2$, $cI16$, $cI432$.

Site	Site symmetry	x	y	z	Generating site
$Im\bar{3}m, (229), cI2, a \times a \times a - a$					
2a	$m\bar{3}m$	0	0	0	
$Im\bar{3}m, (229), cI16, 2a \times 2a \times 2a - abc$					
2a	$m\bar{3}m$	0	0	0	1a ($Im\bar{3}m, cP2$)
6b	$4/mm.m$	0	1/2	1/2	1a ($Im\bar{3}m, cP2$)
8c	$.3m$	1/4	1/4	1/4	1b ($Im\bar{3}m, cP2$)
$Im\bar{3}m, (229), cI432, 6a \times 6a \times 6a - abce^2f^2gh^2ijk^4$					
2a	$m\bar{3}m$	0	0	0	2a ($Im\bar{3}m, cI16$)
6b	$4/mm.m$	0	1/2	1/2	6b ($Im\bar{3}m, cI16$)
8c	$.3m$	1/4	1/4	1/4	8c ($Im\bar{3}m, cI16$)
12e	$4m.m$	1/3	0	0	2a ($Im\bar{3}m, cI16$)
12e	$4m.m$	1/6	0	0	6b ($Im\bar{3}m, cI16$)
16f	$.3m$	1/3	1/3	1/3	2a ($Im\bar{3}m, cI16$)
16f	$.3m$	1/12	1/12	1/12	8c ($Im\bar{3}m, cI16$)
24g	$mm2..$	1/6	0	1/2	6b ($Im\bar{3}m, cI16$)
24h	$m.m2$	1/3	0	0	2a ($Im\bar{3}m, cI16$)
24h	$m.m2$	0	1/6	1/6	6b ($Im\bar{3}m, cI16$)
48i	$.2$	1/4	1/12	5/12	8c ($Im\bar{3}m, cI16$)
48j	$m..$	0	1/6	1/3	6b ($Im\bar{3}m, cI16$)
48k	$.m..$	1/4	1/4	1/12	8c ($Im\bar{3}m, cI16$)
48k	$.m..$	1/6	1/6	1/3	6b ($Im\bar{3}m, cI16$)
48k	$.m..$	1/12	1/12	1/4	8c ($Im\bar{3}m, cI16$)
48k	$.m..$	5/12	5/12	1/12	8c ($Im\bar{3}m, cI16$)

Table 4

Wyckoff sites in space group $Pm\bar{3}m$ of the Bärnighausen tree, $cP2$, $cP16$, $cP128$.

Site	Site symmetry	x	y	z	Generating site
$Pm\bar{3}m, (221), cP2, a \times a \times a - ab$					
1a	$m\bar{3}m$	0	0	0	2a ($Im\bar{3}m, cI2$)
1b	$m\bar{3}m$	1/2	1/2	1/2	2a ($Im\bar{3}m, cI2$)
$Pm\bar{3}m, (221), cP16, 2a \times 2a \times 2a - abcdg$					
1a	$m\bar{3}m$	0	0	0	2a ($Im\bar{3}m, cI16$)
1b	$m\bar{3}m$	1/2	1/2	1/2	2a ($Im\bar{3}m, cI16$)
3c	$4/mm.m$	0	1/2	1/2	6b ($Im\bar{3}m, cI16$)
3d	$4/mm.m$	1/2	0	0	6b ($Im\bar{3}m, cI16$)
8g	$.3m$	1/4	1/4	1/4	8c ($Im\bar{3}m, cI16$)
$Pm\bar{3}m, (221), cP128, 4a \times 4a \times 4a - abcdefg^3hijm^2$					
1a	$m\bar{3}m$	0	0	0	4a ($Fm\bar{3}m, cF128$)
1b	$m\bar{3}m$	1/2	1/2	1/2	4b ($Fm\bar{3}m, cF128$)
3c	$4/mm.m$	0	1/2	1/2	4a ($Fm\bar{3}m, cF128$)
3d	$4/mm.m$	1/2	0	0	4b ($Fm\bar{3}m, cF128$)
6e	$4m.m$	1/4	0	0	24e ($Fm\bar{3}m, cF128$)
6f	$4m.m$	1/4	1/2	1/2	24e ($Fm\bar{3}m, cF128$)
8g	$.3m$	1/4	1/4	1/4	8c ($Fm\bar{3}m, cF128$)
8g	$.3m$	1/8	1/8	1/8	32f ($Fm\bar{3}m, cF128$)
8g	$.3m$	3/8	3/8	3/8	32f ($Fm\bar{3}m, cF128$)
12h	$mm2..$	1/4	1/2	0	24e ($Fm\bar{3}m, cF128$)
12i	$m.m2$	0	1/4	1/4	24d ($Fm\bar{3}m, cF128$)
12j	$m.m2$	1/2	1/4	1/4	24d ($Fm\bar{3}m, cF128$)
24m	$..m$	5/8	5/8	1/8	32f ($Fm\bar{3}m, cF128$)
24m	$..m$	7/8	7/8	3/8	32f ($Fm\bar{3}m, cF128$)

Table 10Wyckoff sites in space group $Fm\bar{3}c$ of the Bärnighausen tree, $cF1024$.

Site	Site symmetry	x	y	z	Generating site
$Fm\bar{3}c$, (226), $cF1024$, $8a \times 8a \times 8a - abcdefg^3hi^2j^2$					
8a	432	1/4	1/4	1/4	1b ($Pm\bar{3}m$, $cP128$)
8b	$m\bar{3}$.	0	0	0	1a ($Pm\bar{3}m$, $cP128$)
24c	$\bar{4}m.2$	1/4	0	0	3d ($Pm\bar{3}m$, $cP128$)
24d	$4/m..$	0	1/4	1/4	3c ($Pm\bar{3}m$, $cP128$)
48e	$mm2..$	1/8	0	0	6e ($Pm\bar{3}m$, $cP128$)
48f	4..	1/8	1/2	1/2	6f ($Pm\bar{3}m$, $cP128$)
64g	.3.	1/8	1/8	1/8	8g ($Pm\bar{3}m$, $cP128$)
64g	.3.	1/16	1/16	1/16	8g ($Pm\bar{3}m$, $cP128$)
64g	.3.	3/16	3/16	3/16	8g ($Pm\bar{3}m$, $cP128$)
96h	.2	1/4	1/8	1/8	12j ($Pm\bar{3}m$, $cP128$)
96i	$m..$	0	1/8	1/4	12h ($Pm\bar{3}m$, $cP128$)
96i	$m..$	0	1/8	1/8	12i ($Pm\bar{3}m$, $cP128$)
192j	1	5/16	5/16	1/16	24m ($Pm\bar{3}m$, $cP128$)
192j	1	7/16	7/16	3/16	24m ($Pm\bar{3}m$, $cP128$)

Table 12Wyckoff sites in space group $F\bar{4}3m$ of the Bärnighausen tree, $cF1024$.

Site	Site symm.	x	y	z	Generating site
$F\bar{4}3m$, (216), $cF1024$, $8a \times 8a \times 8a - abcde^{12}f^3g^3h^{12}i$					
4a	$\bar{4}3m$	0	0	0	1a ($P\bar{4}3m$, $cF128$)
4b	$\bar{4}3m$	1/2	1/2	1/2	1a ($P\bar{4}3m$, $cP128$)
4c	$\bar{4}3m$	1/4	1/4	1/4	1b ($P\bar{4}3m$, $cP128$)
4d	$\bar{4}3m$	3/4	3/4	3/4	1b ($P\bar{4}3m$, $cP128$)
16e	.3m	1/8	1/8	1/8	4e ($P\bar{4}3m$, $cP128$)
16e	.3m	3/8	3/8	3/8	4e ($P\bar{4}3m$, $cP128$)
16e	.3m	5/8	5/8	5/8	4e ($P\bar{4}3m$, $cP128$)
16e	.3m	7/8	7/8	7/8	4e ($P\bar{4}3m$, $cP128$)
24f	2.mm	1/4	0	0	3d ($P\bar{4}3m$, $cP128$)
24g	2.mm	0	1/4	1/4	3c ($P\bar{4}3m$, $cP128$)
48h	..m	1/8	1/8	0	12i ($P\bar{4}3m$, $cP128$)
48h	..m	5/8	5/8	1/2	12i ($P\bar{4}3m$, $cP128$)
48h	..m	1/8	1/8	1/4	12i ($P\bar{4}3m$, $cP128$)
48h	..m	5/8	5/8	3/4	12i ($P\bar{4}3m$, $cP128$)
48h	..m	5/16	5/16	1/16	12i ($P\bar{4}3m$, $cP128$)
48h	..m	7/16	7/16	3/16	12i ($P\bar{4}3m$, $cP128$)
48h	..m	1/16	1/16	5/16	12i ($P\bar{4}3m$, $cP128$)
48h	..m	3/16	3/16	7/16	12i ($P\bar{4}3m$, $cP128$)
48h	..m	13/16	13/16	9/16	12i ($P\bar{4}3m$, $cP128$)
48h	..m	15/16	15/16	11/16	12i ($P\bar{4}3m$, $cP128$)
48h	..m	9/16	9/16	13/16	12i ($P\bar{4}3m$, $cP128$)
48h	..m	11/16	11/16	15/16	12i ($P\bar{4}3m$, $cP128$)
96i	1	1/8	1/4	0	12h ($P\bar{4}3m$, $cP128$)

Table 11Wyckoff sites in space group $F\bar{4}3m$ of the Bärnighausen tree, $cF16$, $cF128$, $cF432$.

Site	Site symmetry	x	y	z	Generating site
$F\bar{4}3m$, (216), $cF16$, $2a \times 2a \times 2a - abcd$					
4a	$\bar{4}3m$	0	0	0	8a ($Fd\bar{3}m$, $cF16$)
4b	$\bar{4}3m$	1/2	1/2	1/2	8b ($Fd\bar{3}m$, $cF16$)
4c	$\bar{4}3m$	1/4	1/4	1/4	8a ($Fd\bar{3}m$, $cP16$)
4d	$\bar{4}3m$	3/4	3/4	3/4	8b ($Fd\bar{3}m$, $cP16$)
16e	.3m	1/8	1/8	1/8	4e ($F\bar{4}3m$, $cP16$)
16e	.3m	3/8	3/8	3/8	4e ($F\bar{4}3m$, $cP16$)
16e	.3m	5/8	5/8	5/8	4e ($F\bar{4}3m$, $cP16$)
16e	.3m	7/8	7/8	7/8	4e ($F\bar{4}3m$, $cP16$)
24f	2.mm	1/4	0	0	3d ($F\bar{4}3m$, $cP16$)
24g	2.mm	0	1/4	1/4	3c ($F\bar{4}3m$, $cP16$)
$F\bar{4}3m$, (216), $cF432$, $6a \times 6a \times 6a - abcde^8f^2g^2h^4$					
4a	$\bar{4}3m$	0	0	0	4a ($F\bar{4}3m$, $cF16$)
4b	$\bar{4}3m$	1/2	1/2	1/2	4b ($F\bar{4}3m$, $cF16$)
4c	$\bar{4}3m$	1/4	1/4	1/4	4c ($F\bar{4}3m$, $cF16$)
4d	$\bar{4}3m$	3/4	3/4	3/4	4d ($F\bar{4}3m$, $cF16$)
16e	.3m	1/3	1/3	1/3	4a ($F\bar{4}3m$, $cF16$)
16e	.3m	2/3	2/3	2/3	4a ($F\bar{4}3m$, $cF16$)
16e	.3m	1/6	1/6	1/6	4b ($F\bar{4}3m$, $cF16$)
16e	.3m	5/6	5/6	5/6	4b ($F\bar{4}3m$, $cF16$)
16e	.3m	1/12	1/12	1/12	4d ($F\bar{4}3m$, $cF16$)
16e	.3m	5/12	5/12	5/12	4d ($F\bar{4}3m$, $cF16$)
16e	.3m	7/12	7/12	7/12	4c ($F\bar{4}3m$, $cF16$)
16e	.3m	11/12	11/12	11/12	4c ($F\bar{4}3m$, $cF16$)
24f	2.mm	1/3	0	0	4a ($F\bar{4}3m$, $cF16$)
24f	2.mm	1/6	0	0	4b ($F\bar{4}3m$, $cF16$)
24g	2.mm	1/12	1/4	1/4	4d ($F\bar{4}3m$, $cF16$)
24g	2.mm	7/12	1/4	1/4	4c ($F\bar{4}3m$, $cF16$)
48h	..m	1/3	1/3	0	4a ($F\bar{4}3m$, $cF16$)
48h	..m	1/6	1/6	1/2	4b ($F\bar{4}3m$, $cF16$)
48h	..m	5/12	5/12	1/4	4c ($F\bar{4}3m$, $cF16$)
48h	..m	1/12	1/12	3/4	4d ($F\bar{4}3m$, $cF16$)

Table 13Wyckoff sites in space group $Fd\bar{3}m$ of the Bärnighausen tree, $cF16$, $cF432$.

Site	Site symmetry	x	y	z	Generating site
$Fd\bar{3}m$, (227), $cF16$, $2a \times 2a \times 2a - ab$					
8a	$\bar{4}3m$	0	0	0	2a ($Pn\bar{3}m$, $cP2$)
8b	$\bar{4}3m$	1/2	1/2	1/2	2a ($Pn\bar{3}m$, $cP2$)
$Fd\bar{3}m$, (227), $cF432$, $6a \times 6a \times 6a - abe^4f^2g^2$					
8a	$\bar{4}3m$	0	0	0	8a ($Fd\bar{3}m$, $cF16$)
8b	$\bar{4}3m$	1/2	1/2	1/2	8b ($Fd\bar{3}m$, $cF16$)
32e	.3m	1/3	1/3	1/3	8a ($Fd\bar{3}m$, $cF16$)
32e	.3m	1/12	1/12	1/12	8b ($Fd\bar{3}m$, $cF16$)
32e	.3m	5/12	5/12	5/12	8b ($Fd\bar{3}m$, $cF16$)
32e	.3m	7/12	7/12	7/12	8a ($Fd\bar{3}m$, $cF16$)
48f	2.mm	1/3	0	0	8a ($Fd\bar{3}m$, $cF16$)
48f	2.mm	5/6	0	0	8b ($Fd\bar{3}m$, $cF16$)
96g	..2	7/12	7/12	1/4	8a ($Fd\bar{3}m$, $cF16$)
96g	..2	1/12	1/12	3/4	8b ($Fd\bar{3}m$, $cF16$)

Table 14Wyckoff sites in space group $Fd\bar{3}m$ of the Bärnighausen tree, $cF1024$.

Site	Site symm.	x	y	z	Generating site
$Fd\bar{3}m$, (227), $cF1024$, $8a \times 8a \times 8a - abcde^5f^3g^6h$					
8a	$\bar{4}3m$	0	0	0	$2a(Pn\bar{3}m, cP128)$
8b	$\bar{4}3m$	1/2	1/2	1/2	$2a(Pn\bar{3}m, cP128)$
16c	$.3m$	1/8	1/8	1/8	$4b(Pn\bar{3}m, cP128)$
16d	$.3m$	5/8	5/8	5/8	$4b(Pn\bar{3}m, cP128)$
32e	$.3m$	3/8	3/8	3/8	$4c(Pn\bar{3}m, cP128)$
32e	$.3m$	3/16	3/16	3/16	$8e(Pn\bar{3}m, cP128)$
32e	$.3m$	5/16	5/16	5/16	$8e(Pn\bar{3}m, cP128)$
32e	$.3m$	11/16	11/16	11/16	$8e(Pn\bar{3}m, cP128)$
32e	$.3m$	13/16	13/16	13/16	$8e(Pn\bar{3}m, cP128)$
48f	$2.m$	1/4	0	0	$6d(Pn\bar{3}m, cP128)$
48f	$2.m$	1/8	0	0	$12g(Pn\bar{3}m, cP128)$
48f	$2.m$	5/8	0	0	$12g(Pn\bar{3}m, cP128)$
96g	$..m$	1/8	1/8	1/4	$24k(Pn\bar{3}m, cP128)$
96g	$..m$	5/8	5/8	3/4	$24k(Pn\bar{3}m, cP128)$
96g	$..m$	7/16	7/16	3/16	$24k(Pn\bar{3}m, cP128)$
96g	$..m$	1/16	1/16	5/16	$24k(Pn\bar{3}m, cP128)$
96g	$..m$	15/16	15/16	11/16	$24k(Pn\bar{3}m, cP128)$
96g	$..m$	9/16	9/16	13/16	$24k(Pn\bar{3}m, cP128)$
96h	$.2$	1/8	0	1/4	$12f(Pn\bar{3}m, cP128)$

Table 15Wyckoff sites in space group $Fm\bar{3}$ of the Bärnighausen tree, $cF128$.

Site	Site symmetry	x	y	z	Generating site
$Fm\bar{3}$, (202), $cF128$, $4a \times 4a \times 4a - abcdef^2$					
4a	$m\bar{3}.$	0	0	0	$1a(Pm\bar{3}, cP16)$
4b	$m\bar{3}.$	1/2	1/2	1/2	$1a(Pm\bar{3}, cP16)$
8c	$23.$	1/4	1/4	1/4	$1b(Pm\bar{3}, cP16)$
24d	$2/m..$	0	1/4	1/4	$3c(Pm\bar{3}, cP16)$
24e	$mm2..$	1/4	0	0	$3d(Pm\bar{3}, cP16)$
32f	$.3.$	1/8	1/8	1/8	$8i(Pm\bar{3}, cP16)$
32f	$.3.$	3/8	3/8	3/8	$8i(Pm\bar{3}, cP16)$

Table 16Wyckoff sites in space group $Fd\bar{3}$ of the Bärnighausen tree, $cF1024$.

Site	Site symmetry	x	y	z	Generating site
$Fd\bar{3}$, (203), $cF1024$, $4a \times 4a \times 4a - abcde^5f^3g^7$					
8a	23.	0	0	0	$2a(Pn\bar{3}, cP128)$
8b	23.	1/2	1/2	1/2	$2a(Pn\bar{3}, cP128)$
16c	$.3.$	1/8	1/8	1/8	$4b(Pn\bar{3}, cP128)$
16d	$.3.$	5/8	5/8	5/8	$4b(Pn\bar{3}, cP128)$
32e	$.3.$	3/8	3/8	3/8	$4c(Pn\bar{3}, cP128)$
32e	$.3.$	3/16	3/16	3/16	$8e(Pn\bar{3}, cP128)$
32e	$.3.$	5/16	5/16	5/16	$8e(Pn\bar{3}, cP128)$
32e	$.3.$	11/16	11/16	11/16	$8e(Pn\bar{3}, cP128)$
32e	$.3.$	13/16	13/16	13/16	$8e(Pn\bar{3}, cP128)$
48f	$2..$	1/4	0	0	$6d(Pn\bar{3}, cP128)$
48f	$2..$	1/8	0	0	$12f(Pn\bar{3}, cP128)$
48f	$2..$	5/8	0	0	$12f(Pn\bar{3}, cP128)$
96g	1	1/8	1/4	0	$12g(Pn\bar{3}, cP128)$
96g	1	1/4	1/8	1/8	$24h(Pn\bar{3}, cP128)$
96g	1	3/4	5/8	5/8	$24h(Pn\bar{3}, cP128)$
96g	1	3/16	7/16	7/16	$32f(Pn\bar{3}, cP128)$
96g	1	5/16	1/16	1/16	$32f(Pn\bar{3}, cP128)$
96g	1	11/16	15/16	15/16	$32f(Pn\bar{3}, cP128)$
96g	1	13/16	9/16	9/16	$32f(Pn\bar{3}, cP128)$

Table 17Wyckoff sites in the additional space groups of the inset to the Bärnighausen tree, $Im\bar{3}m - cI54$, $Pm\bar{3}m - cP54$, $P\bar{4}3m - cP54$, $Pn\bar{3}m - cP54$.

Site	Site symmetry	x	y	z	Generating site
$Im\bar{3}m$, (229), $cI54$, $3a \times 3a \times 3a - aefh$					
2a	$m\bar{3}m$	0	0	0	$2a(Im\bar{3}m, cI2)$
12e	$4m.m$	1/3	0	0	$2a(Im\bar{3}m, cI2)$
16f	$.3m$	1/3	1/3	1/3	$2a(Im\bar{3}m, cI2)$
24h	$m.m2$	0	1/3	1/3	$2a(Im\bar{3}m, cI2)$
$Pm\bar{3}m$, (221), $cP54$, $3a \times 3a \times 3a - abefg^i j$					
1a	$m\bar{3}m$	0	0	0	$1a(Pm\bar{3}m, cP2)$
1b	$m\bar{3}m$	1/2	1/2	1/2	$1b(Pm\bar{3}m, cP2)$
6e	$4m.m$	1/3	0	0	$1a(Pm\bar{3}m, cP2)$
6f	$4m.m$	1/6	1/2	1/2	$1b(Pm\bar{3}m, cP2)$
8g	$.3m$	1/3	1/3	1/3	$1a(Pm\bar{3}m, cP2)$
8g	$.3m$	1/6	1/6	1/6	$1b(Pm\bar{3}m, cP2)$
12i	$m.m2$	0	1/3	1/3	$1a(Pm\bar{3}m, cP2)$
12j	$m.m2$	1/2	1/6	1/6	$1b(Pm\bar{3}m, cP2)$
$P\bar{4}3m$, (215), $cP54$, $3a \times 3a \times 3a - abc^4fg^i t^2$					
1a	$\bar{4}3m$	0	0	0	$1a(Pm\bar{3}m, cP54)$
1b	$\bar{4}3m$	1/2	1/2	1/2	$1b(Pm\bar{3}m, cP54)$
4e	$.3m$	1/3	1/3	1/3	$8g(Pm\bar{3}m, cP54)$
4e	$.3m$	2/3	2/3	2/3	$8g(Pm\bar{3}m, cP54)$
4e	$.3m$	1/6	1/6	1/6	$8g(Pm\bar{3}m, cP54)$
4e	$.3m$	5/6	5/6	5/6	$8g(Pm\bar{3}m, cP54)$
6f	$2.m$	1/3	0	0	$6e(Pm\bar{3}m, cP54)$
6g	$2.m$	1/6	1/2	1/2	$6f(Pm\bar{3}m, cP54)$
12i	$..m$	1/3	1/3	0	$12i(Pm\bar{3}m, cP54)$
12i	$..m$	1/6	1/6	1/2	$12j(Pm\bar{3}m, cP54)$
$Pn\bar{3}m$, (224), $cP54$, $3a \times 3a \times 3a - ae^2gk$					
2a	$\bar{4}3m$	0	0	0	$2a(Pn\bar{3}m, cP2)$
8e	$.3m$	1/3	1/3	1/3	$2a(Pn\bar{3}m, cP2)$
8e	$.3m$	2/3	2/3	2/3	$2a(Pn\bar{3}m, cP2)$
12g	$2.m$	1/3	0	0	$2a(Pn\bar{3}m, cP2)$
24k	$..m$	1/3	1/3	0	$2a(Pn\bar{3}m, cP2)$

The Wyckoff sites of the two largest structures in space group $P\bar{4}3m$, also shown in the Bärnighausen tree as $cF5488$ and $cF21296$, are not given. They may be derived using the *International Tables for Crystallography - Volume A1: Symmetry Relations Between Space Group* (Ed.s Hans Wondratschek and Ulrich Müller, 2006).

3. Atomic sites – Coordinates

The sites belonging to the different clusters in cubic complex intermetallic structures in space group $F\bar{4}3m$ are given in Table 18. The ones of the hypothetic subtype V are given in Table 19.

Table 18

Main cluster found in the structure of cubic complex intermetallics of space group $F\bar{4}3m$. Given are the sites belonging to a certain cluster (shell), the number of atoms, and the polyhedron built up by them. The following shells correspond to special clusters: 1st shell, 1st variant – (14 atoms) rhombic dodecahedron, 1st shell, 2nd variant – FK_{16}^{28} / Friauf polyhedron, 2nd shell – FK_{40}^{76} / Frank-Kasper polyhedron with 76 faces and 40 vertices, 3rd shell, 6th variant – F_{76}^{40} / fullerene polyhedron with 40 faces and 76 vertices. The subtypes I..IV in which the respective clusters occur are indicated in columns ST.

Nr. of atoms	(0, 0, 0)		$(\frac{1}{4}, \frac{1}{4}, \frac{1}{4})$		Sites around cluster center		$(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$		$(\frac{3}{4}, \frac{3}{4}, \frac{3}{4})$	
	Cluster center	1	4a	ST	4c	ST	4b	ST	4d	ST
First cluster shell										
14	16e4/5, 24f1	I..IV	16e1/6, 24g1		I..III	16e2/7, 24f2		I	16e3/8, 24g2	I,II
16	-	-	16e1, 48h5		IV	16e2, 48h6		II..IV	16e3, 48h7	III,IV
Second cluster shell										
40	16e1, 48h1/2/4	I..IV	16e2, 48h1/2/3		I..IV	16e3, 48h2/3/4		I..IV	16e4, 48h1/3/4	I..IV
Third cluster shell										
58	16e6/8, 24f2/g2, 48h3	I	16e5/7, 24f1/g2, 48h4	I	16e6/8, 24f1/g1, 48h1	I, II	16e5/7, 24f2/g1, 48h2	I		
64	16e6/8, 24g2, 48h3/6	II	16e5, 24f1/g2, 48h4/6	II			16e5, 24g1, 48h2/6	II,III		
70							16e5, 48h2/5/6	IV		
54										
60	16e6, 48h3/6/7	III	16e5, 24f1, 48h4/6/7	III,IV						
76										
70										
72	48h3/5/6/7	IV								
66										

Table 19

Main cluster found in the hypothetical structure of subtype V of cubic complex intermetallics in space group $F\bar{4}3m$. The clusters which do not occur in the above-discussed other subtypes are highlighted by bold letters. Given are the sites belonging to a certain cluster (shell), the number of atoms, and the polyhedron built up by them.

Cluster shell	Polyhedron	Nr. of atoms	(0, 0, 0)	$(\frac{1}{4}, \frac{1}{4}, \frac{1}{4})$	Sites around cluster center	$(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$	$(\frac{3}{4}, \frac{3}{4}, \frac{3}{4})$
Center	-	1	4a	4c	4b	4d	
1st	FK_{16}^{28}	16	16e4, 48h8	16e1, 48h5	16e2, 48h6	16e3, 48h7	
2nd	FK_{40}^{76}	40	16e1, 48h1, 2, 4	16e2, 48h1, 2, 3	16e3, 48h2, 3, 4	16e4, 48h1, 3, 4	
3rd		72	48h3, 5, 6, 7	48h4, 6, 7, 8	48h1, 5, 7, 8	48h2, 5, 6, 8	

Table 20

Development of the third cluster shells throughout the subtypes I..V (ST) with number of vertices and different faces (t triangular, q quadrangular, p pentagonal, h hexagon) for the sites of highest symmetry $4a \cdots d$ (000, $\frac{1}{2}\frac{1}{2}\frac{1}{2}$, $\frac{1}{4}\frac{1}{4}\frac{1}{4}$, and $\frac{3}{4}\frac{3}{4}\frac{3}{4}$, respectively).

ST	No. of vertices				No. of different faces			
	4a	4c	4b	4d	4a	4c	4b	4d
I	58	58	58	58	$t^4q^{12}p^{12}h^{12}$	$t^4q^{12}p^{12}h^{12}$	$t^4q^{12}p^{12}h^{12}$	$t^4q^{12}p^{12}h^{12}$
II	64	70	58	54	$t^4p^{24}h^{12}$	$p^{24}h^{16}$	$t^4p^{12}h^{12}$	$t^8q^{12}p^{24}$
III	60	76	70	54	t^8p^{36}	$p^{12}h^{28}$	$p^{24}h^{16}$	$t^8q^{12}p^{24}$
IV	72	76	66	60	$t^4p^{24}h^{16}$	$p^{12}h^{28}$	$t^4p^{36}h^4$	t^8p^{36}
V	72	72	72	72	$t^4p^{24}h^{16}$	$t^4p^{24}h^{16}$	$t^4p^{24}h^{16}$	$t^4p^{24}h^{16}$

The sites of the clusters in structures in space group $Fd\bar{3}m$ are listed in Table 21. The sites of the one-shell clusters used in the modular explanation of the $cF464$ -structures in space group $Fd\bar{3}m$ are given in Table 22.

Table 21

Clusters found in the structure of cubic complex intermetallics of space group $Fd\bar{3}m$. Given are the sites belonging to a certain cluster (shell), the number of atoms, and the polyhedron built up by them.

Cluster shell	Shape	Polyhedron		Shape	Capped polyhedron		Atoms
		Atoms	Sites		Add. atoms	Additional sites	
Center	-	1	8a				1
1st	tt	12	$12 \times 96g2$	FK_{16}^{28}	+4	$+4 \times 32e1$	16
2nd	F_{28}^{16}	28	$4 \times 32e2, 24 \times 96g1$	FK_{44}^{84}	+16	$+4 \times 32e1, 12 \times 96g3$	40
3rd	F_{84}^{44}	84	$24 \times 96g2, 24 \times 96g3, 36 \times 96g4$				
Center	-	0	16d	icosahedron	12	$6 \times 96g3, 6 \times 96g4$	0
1st	dodecahedron	20	$2 \times 8b, 6 \times 32e2, 12 \times 96g1$				
2nd							

Table 22

Atomic sites of one-shell clusters used in the modular explanation of cubic complex intermetallics of space group $Fd\bar{3}m$. Given are the sites belonging to the cluster around a specified cluster center, the number of atoms, and the polyhedron built up by them.

Center	Polyhedron	Atoms	Sites
8a	truncated tetrahedron	12	$12 \times 96g2$
	Friauf polyhedron	16	+ $4 \times 32e1$
32e2	truncated tetrahedron	12	$3 \times 96g2, 3 \times 96g3, 6 \times 96g4$
	Friauf polyhedron	16	+ $3 \times 96g1, 1 \times 8b$
96g1	truncated tetrahedron	12	$2 \times 32e1, 4 \times 96g2, 4 \times 96g3, 2 \times 96g4$
	Friauf polyhedron	16	+ $3 \times 96g1, 1 \times 32e1$
16d	icosahedron	12	$6 \times 96g3, 6 \times 96g4$
8b	truncated tetrahedron	12	$12 \times 96g4$
	Friauf polyhedron	16	+ $4 \times 32e2$

The sites of both structure types can be directly related to one another as shown in Table 23. The site symmetry is preserved except for $32e/16e$ sites, which have symmetry $.3m$ in space group $Fd\bar{3}m$ and $.3m$ in $F\bar{4}3m$. Not listed are the $24f$ and $24g$ sites, which contribute to rhombic dodecahedra around $\bar{4}3m$ sites, which do not occur in the $Fd\bar{3}m$ structures. Correspondingly, only half of the $16e$ sites are related to the $32e$ sites of space group $Fd\bar{3}m$. Of sites $96g3$ and $96g4$, only half of the positions could be related to sites in $F\bar{4}3m$ structures: $48h5$ is part of site $96g2$, as $48h6$ relates directly to $96g4$. When we investigate the relationship between the structures it becomes clear that the inner cluster shells, which have the shape of Friauf polyhedra, should contain sites $16e3$ and $16e4$ instead of $16e5$ and $16e8$. They can be regarded as being oriented conversely and accordingly, not sites $48h7$ and $48h8$ are occupied but their counterparts, corresponding to half of the positions described by sites $96g3$ and $96g4$ in space group $Fd\bar{3}m$. Therein, one half of the polyhedra have an opposite orientation with respect to the other half, whereas in the $F\bar{4}3m$ structures, all sub-units are oriented similarly.

Table 23

Relations of the atomic sites in cubic complex intermetallics of space groups $Fd\bar{3}m$ and $F\bar{4}3m$.

Site	$Fd\bar{3}m$		$F\bar{4}3m$	
	Site symmetry		Site	Site symmetry
8a	$43m$		4a, 4c	$43m$
8b	$43m$		4b, 4d	$\bar{4}3m$
32e1	$.3m$		16e1, 16e5	$.3m$
32e2	$.3m$		16e2, 16e8	$.3m$
96g1	$..m$		48h1, 48h2	$..m$
96g2	$..m$		48h3, 48h4	$..m$
96g3	$..m$		48h5 & ..	$..m$
96g4	$..m$		48h6 & ..	$..m$

5. Coordination shells around low-symmetry sites in $\text{Al}_{63.6}\text{Ta}_{36.4}$

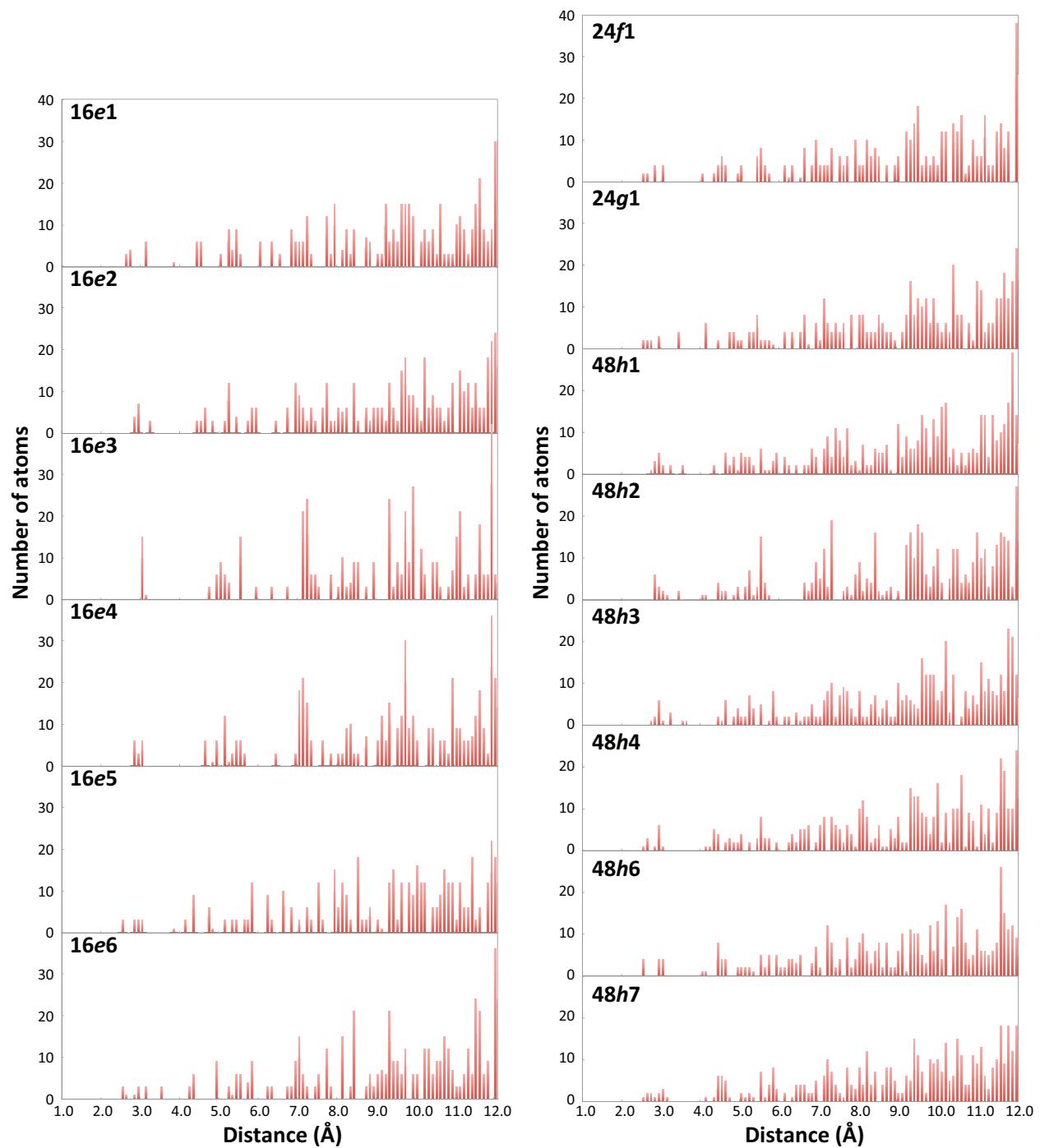


Figure 1

Frequency of interatomic distances of atoms in the environment of the lower-symmetry atomic sites in $\text{Al}_{63.6}\text{Ta}_{36.4}$.

6. (110) layers

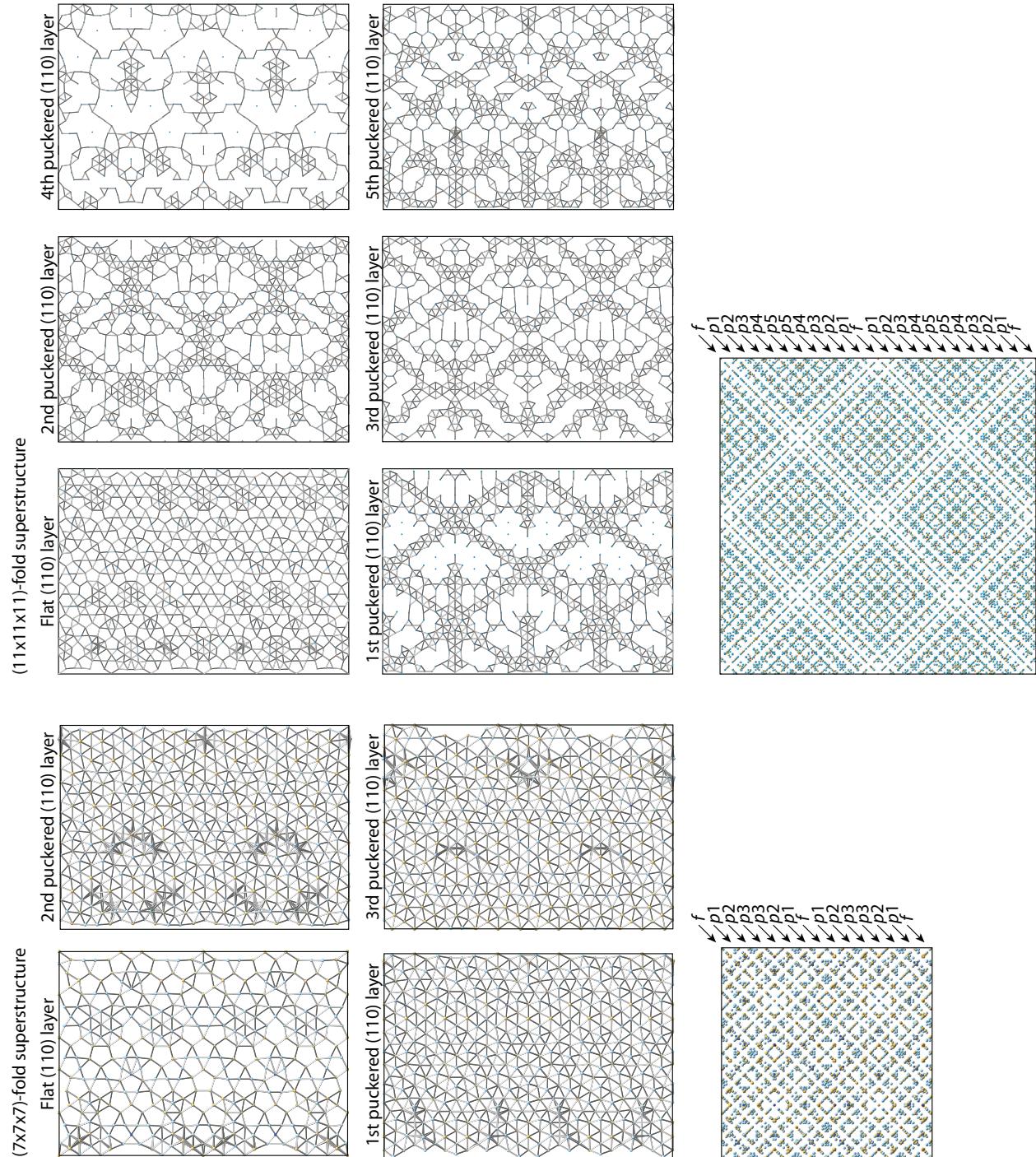


Figure 2
 (110) layers of the two giant-unit-cell Al-Cu-Ta compounds (with $p = 7$ and $p = 11$), as well as their arrangement.

7. First-principles calculations

Table 27

Details on the performed *ab initio* calculations for structures of space group $F\bar{4}3m$. Given are the number of calculated electrons per atom (e/atom) and the number of atoms in the calculated unit cell (atoms/u.c.), both values given for each atomic sort in the order of content in the unit cell, as well as the idealization steps applied to partly disordered structures. The structures $\text{Cu}_{73.9}\text{Sn}_{23.2}\text{Ni}_{2.9}$ and $\text{Zn}_{86.6}\text{Fe}_{6.7}\text{Ni}_{6.7}$ had to be calculated in the variants $\text{Cu}_{76.8}\text{Sn}_{23.2}$ and $\text{Zn}_{86.6}\text{Fe}_{13.4}$, as well as $\text{Zn}_{86.6}\text{Ni}_{13.4}$, respectively, because the Ni sites had not been specified on structure determination.

Structure	e/atom	atoms/u.c.	Applied idealization steps
<i>Subtype I</i> (14 structures)			
$\text{Li}_{64.3}\text{In}_{26.5}\text{Ag}_{9.2}$	3, 13, 11	59, 38, 11	$4b: 0.8 \text{ Li}, 0.2 \text{ Ag} \rightarrow 1 \text{ Li}; 4d: 0.82 \text{ Ag}, 0.18 \text{ Li} \rightarrow 1 \text{ Ag}; 16e5: 0.57 \text{ Li}, 0.43 \text{ Ag} \rightarrow 1 \text{ Li}; 16e8: 0.77 \text{ In}, 0.23 \text{ Li} \rightarrow 1 \text{ In}; 24g1: 0.54 \text{ Ag}, 0.46 \text{ Li} \rightarrow 1 \text{ Ag}; 48h3: 0.54 \text{ In}, 0.46 \text{ Li} \rightarrow 1 \text{ In}; 48h4: 0.75 \text{ In}, 0.25 \text{ Li} \rightarrow 1 \text{ In}$
$\text{Li}_{81.0}\text{Pb}_{19.0}$	3, 14	85, 20	-
$\text{Li}_{81.0}\text{Sn}_{19.0}$	3, 14	85, 20	-
$\text{Li}_{81.0}\text{Ge}_{19.0}$	3, 14	85, 20	$4a: 0.75 \rightarrow 1 \text{ Li}; 16e5: 0.75/0.25 \rightarrow 1 \text{ Li}$
$\text{Zn}_{80.9}\text{Pd}_{14.5}\text{Al}_{4.6}$	12, 16, 3	82, 18, 4	$16e3: 0.83/0.19 \text{ Zn} \rightarrow 1 \text{ Zn}; 16e5: 0.94 \text{ Zn}, 0.05 \text{ Al} \rightarrow 1 \text{ Zn}; 16e8: 0.78 \text{ Al}, 0.22 \text{ Zn} \rightarrow 1 \text{ Al}; 24g2: 0.52 \text{ Pd}, 0.48 \text{ Zn} \rightarrow 1 \text{ Pd}; 48h4: 0.88 \text{ Zn}, 0.12 \text{ Al} \rightarrow 1 \text{ Zn}$
$\text{Zn}_{82.7}\text{Pt}_{17.3}$	12, 10	86, 18	$16e1: 0.24/0.39 \text{ Zn}, 0.34 \text{ Pt} \rightarrow 1 \text{ Zn}; 16e4: 0.61 \text{ Zn}, 0.39 \text{ Pt} \rightarrow 1 \text{ Zn}; 16e6: 0.5/0.27 \rightarrow 1 \text{ Zn}; 24f1: 0.51 \text{ Pt}, 0.49 \text{ Zn} \rightarrow 1 \text{ Pt}; 24f2: 0.71 \rightarrow 1 \text{ Zn}; 24g1: 0.53 \text{ Zn}, 0.47 \text{ Pt} \rightarrow 1 \text{ Zn}; 24g2: 0.69 \rightarrow 1 \text{ Zn}; 48h2: 0.91 \rightarrow 1 \text{ Zn}$
$\text{Zn}_{81.6}\text{Pt}_{18.4}$	12, 10	90, 14	$16e1: 0.70/0.31 \rightarrow 1 \text{ Zn}; 16e4: 0.86/0.14 \rightarrow 1 \text{ Zn}; 16e6: 0.68/0.17 \rightarrow 1 \text{ Zn}; 24f1: 0.85 \text{ Pt}, 0.15 \text{ Zn} \rightarrow 1 \text{ Pt}; 24g1: 0.86 \text{ Pt}, 0.14 \text{ Zn} \rightarrow 1 \text{ Pt}; 48h2: 0.90 \rightarrow 1 \text{ Zn}$
$\text{Zn}_{78.7}\text{Pd}_{16.0}\text{Al}_{5.3}$	12, 16, 3	82, 18, 4	$16e3: 0.51/0.21 \rightarrow 1 \text{ Zn}; 16e5: 0.78 \text{ Zn}, 0.22 \text{ Al} \rightarrow 1 \text{ Zn}; 16e8: 0.74 \rightarrow 1 \text{ Al}; 24g2: 0.71 \text{ Pd}, 0.29 \text{ Zn} \rightarrow 1 \text{ Pd}; 48h4: 0.87 \text{ Zn}, 0.13 \text{ Al} \rightarrow 1 \text{ Zn}$
$\text{Zn}_{77.0}\text{Pt}_{23.0}$	12, 10	70, 24	$16e1: 0.5 \text{ Zn}, 0.5 \text{ Pt} \rightarrow 1 \text{ Zn}; 16e6: 0.92 \text{ Zn}, 0.18 \text{ Pt} \rightarrow 1 \text{ Zn}; 24f1: 0.67 \text{ Pt}, 0.33 \text{ Zn} \rightarrow 1 \text{ Pt}; 24f2: 0.92 \text{ Zn}, 0.18 \text{ Pt} \rightarrow 1 \text{ Zn}; 24g1: 0.67 \text{ Pt}, 0.33 \text{ Zn} \rightarrow 1 \text{ Pt}$
$\text{Zn}_{80.0}\text{Pt}_{20.0}$	12, 10	84, 20	$16e3: 0.88 \text{ Zn}, 0.12 \text{ Pt} \rightarrow 1 \text{ Zn}; 16e5: 0.62 \rightarrow 1 \text{ Zn}; 48h1: 0.87/0.12 \rightarrow 1 \text{ Zn}$
$\text{Zn}_{78.5}\text{Pd}_{14.0}\text{Al}_{7.5}$	12, 16, 3	82, 14, 4	$16e5: 0.81 \text{ Zn}, 0.19 \text{ Al} \rightarrow 1 \text{ Zn}; 48h4: 0.77 \text{ Zn}, 0.23 \text{ Al} \rightarrow 1 \text{ Zn}$
$\text{Cu}_{73.9}\text{Sn}_{26.1}$	11, 4	82, 22	$16e7: 0.75 \rightarrow 1 \text{ Cu}; 48h1: 0.75 \rightarrow 1 \text{ Cu}$ (Ni sites unspecified)
$\text{Cu}_{78.6}\text{Sn}_{21.4}$	11, 4	82, 22	$16e7: 0.75 \rightarrow 1 \text{ Cu}$
$\text{Cu}_{79.8}\text{Sn}_{20.2}$	11, 4	82, 22	$16e8: 0.83 \text{ Cu}, 0.17 \text{ Sn} \rightarrow 1 \text{ Cu}; 24f1: 0.81 \text{ Cu}, 0.19 \text{ Sn} \rightarrow 1 \text{ Cu}; 48h4: 0.86 \text{ Sn}, 0.14 \text{ Cu} \rightarrow 1 \text{ Sn}$
<i>Subtype I/II</i> (3 structures)			
$\text{Zn}_{89.1}\text{Ir}_{10.9}$	12, 9	93, 8	$4b: 0.51 \rightarrow 1 \text{ Zn}; 16e1: 0.82 \text{ Zn}, 0.18 \text{ Ir} \rightarrow 1 \text{ Zn}; 16e7: 0.64 \rightarrow 1 \text{ Zn}; 24f2: 0.62 \rightarrow 1 \text{ Zn}; 24g1: 0.62 \text{ Zn}, 0.38 \text{ Ir} \rightarrow 1 \text{ Zn}; 48h6: 0.33 \text{ Zn} \rightarrow 0$
$\text{Zn}_{90.5}\text{Ir}_{9.5}$	12, 9	95, 8	$4b: 0.63 \rightarrow 1 \text{ Zn}; 4c: 0.25 \text{ Ir} \rightarrow 0; 16e1: 0.91 \text{ Zn}, 0.09 \text{ Ir} \rightarrow 1 \text{ Zn}; 16e6: 0.62/0.25 \rightarrow 1 \text{ Zn}; 16e7: 0.45 \text{ Zn} \rightarrow 0; 24f2: 0.36 \text{ Zn} \rightarrow 0; 24g1: 0.84 \text{ Zn}, 0.16 \text{ Ir} \rightarrow 1 \text{ Zn}; 48h3: 0.62/0.40 \rightarrow 1 \text{ Zn}; 48h6: 0.57 \rightarrow 1 \text{ Zn}$
$\text{Zn}_{91.1}\text{Ir}_{8.9}$	12, 9	95, 8	$4b: 0.70 \rightarrow 1 \text{ Zn}; 4c: 0.41 \text{ Ir} \rightarrow 0; 16e1: 0.98 \text{ Zn}, 0.02 \text{ Ir} \rightarrow 1 \text{ Zn}; 16e6: 0.60/0.30 \rightarrow 1 \text{ Zn}; 16e7: 0.42 \text{ Zn} \rightarrow 0; 24f2: 0.29 \text{ Zn} \rightarrow 0; 24g1: 0.90 \text{ Zn}, 0.10 \text{ Ir} \rightarrow 1 \text{ Zn}; 48h6: 0.62 \rightarrow 1 \text{ Zn}$
<i>Subtype II</i> (14 structures)			
$\text{Na}_{86.3}\text{Tl}_{13.7}$	9, 13	88, 14	$24f1: 0.94 \rightarrow 1 \text{ Na}$
$\text{Sc}_{86.3}\text{Os}_{13.7}$	11, 14	88, 14	-
$\text{Mg}_{87.3}\text{Ru}_{12.7}$	8, 14	88, 14	$16e4: 0.75 \text{ Ru}, 0.25 \text{ Mg} \rightarrow 1 \text{ Ru}; 16e6: 0.67 \text{ Mg}, 0.33 \text{ Ru} \rightarrow 1 \text{ Mg}$
$\text{Mg}_{86.3}\text{Rh}_{13.7}$	8, 15	88, 14	-
$\text{Mg}_{87.9}\text{Ir}_{12.1}$	8, 9	87, 12	-
$\text{Mg}_{85.9}\text{Pd}_{14.1}$	8, 16	87, 12	$4b: 0.97 \rightarrow 1 \text{ Mg}; 16e2: 0.51 \text{ Mg}, 0.49 \text{ Pd} \rightarrow 1 \text{ Mg}$
$\text{Mg}_{86.3}\text{Ir}_{13.7}$	8, 9	88, 14	-
$\text{Zn}_{95.3}\text{Mo}_{4.7}$	12, 12	100, 5	$4a: 0.65 \rightarrow 1 \text{ Mo}; 4c: 0.57 \text{ Mo}, 0.43 \text{ Zn} \rightarrow 1 \text{ Mo}; 16e5: 0.35 \rightarrow 1 \text{ Zn}; 16e6: 0.44 \rightarrow 1 \text{ Zn}; 24g1: 0.70 \rightarrow 1 \text{ Zn}$
$\text{Al}_{65.3}\text{Cu}_{18.1}\text{Cr}_{16.6}$	3, 12, 17	72, 18, 12	$4b: 0.28 \text{ Cu} \rightarrow 0; 16e4: 0.74 \text{ Cr}, 0.26 \text{ Cu} \rightarrow 1 \text{ Cr}; 16e5: 0.79 \text{ Al}, 0.21 \text{ Cu} \rightarrow 1 \text{ Al}; 24g2: 0.58 \text{ Al}, 0.42 \text{ Cu} \rightarrow 1 \text{ Al}; 48h4: 0.85 \text{ Al}, 0.15 \text{ Cu} \rightarrow 1 \text{ Al}; 48h6: 0.5 \rightarrow 1 \text{ Cu}$
$\text{Zn}_{86.6}\text{Fe}_{13.4}$	12, 14	89, 15	$4c: 0.68 \text{ Fe}/\text{Ni} \rightarrow 1 \text{ Fe}; 16e3: 1 \text{ Fe}/\text{Ni} \rightarrow 1 \text{ Ni}; 16e6: 0.53 \text{ Fe}/\text{Ni}, 0.25 \text{ Fe}/\text{Ni} \rightarrow 1 \text{ Fe}; 24g1: 1 \text{ Fe}/\text{Ni} \rightarrow 1 \text{ Fe}$
$\text{Zn}_{86.6}\text{Ni}_{13.4}$	12, 16	89, 15	$4c: 0.68 \text{ Fe}/\text{Ni} \rightarrow 1 \text{ Ni}; 16e3: 1 \text{ Fe}/\text{Ni} \rightarrow 1 \text{ Ni}; 16e6: 0.53 \text{ Fe}/\text{Ni}, 0.25 \text{ Fe}/\text{Ni} \rightarrow 1 \text{ Ni}; 24g1: 1 \text{ Fe}/\text{Ni} \rightarrow 1 \text{ Ni}$
$\text{Zn}_{78.4}\text{Fe}_{21.6}$	14, 12	76, 26	$16e1: 1 \text{ Fe}/\text{Zn} \rightarrow 1 \text{ Fe}; 16e4: 1 \text{ Fe}/\text{Zn} \rightarrow 1 \text{ Fe}; 16e5: 1 \text{ Fe}/\text{Zn} \rightarrow 1 \text{ Fe}$
$\text{In}_{54.5}\text{Pd}_{29.3}\text{Ce}_{16.3}$	13, 16, 12	67, 36, 20	$48h3: 0.66/0.34 \rightarrow 1 \text{ Pd}; 48h6: 0.68/0.32 \rightarrow 1 \text{ In}$
$\text{Zn}_{67.5}\text{Ce}_{16.7}\text{Mg}_{15.8}$	12, 12, 8	81, 20, 19	-
<i>Subtype III</i> (5 structures)			
$\text{Mg}_{83.6}\text{Gd}_{16.4}$	8, 9	90, 22	$16e6: 0.70 \rightarrow 1 \text{ Mg}; 24g2: 0.86 \rightarrow 1 \text{ Mg}; 48h2: 0.68 \text{ Gd}, 0.32 \text{ Mg} \rightarrow 1 \text{ Gd}$
$\text{Cd}_{80.4}\text{Sm}_{19.6}$	12, 11	90, 22	-
$\text{Al}_{63.6}\text{Ta}_{36.4}$	3, 11	72, 39	$16e6: 0.33/0.33/0.33 \rightarrow 1 \text{ Al}; 24g1: 0.5/0.5 \rightarrow 1 \text{ Al}; 48h2: 0.79/0.21 \rightarrow 1 \text{ Al}; 48h3: 0.82/0.18 \rightarrow 1 \text{ Ta}; 48h4: 0.71/0.14/0.14 \rightarrow 1 \text{ Al}; 48h6: 0.88 \text{ Al}, 0.12 \text{ Ta} \rightarrow 1 \text{ Al}$
$\text{Mg}_{82.4}\text{Y}_{9.0}\text{Ce}_{8.6}$	8, 11, 12	90, 4, 18	$4b: 0.62 \text{ Ce}, 0.38 \text{ Y} \rightarrow 1 \text{ Ce}; 4c: 0.62 \text{ Ce}, 0.38 \text{ Y} \rightarrow 1 \text{ Ce}; 16e4: 0.62 \text{ Ce}, 0.38 \text{ Y} \rightarrow 1 \text{ Ce}; 16e6: 0.7 \rightarrow 1 \text{ Mg}; 24g1: 0.86 \rightarrow 1 \text{ Mg}; 48h2: 0.48 \text{ Ce}, 0.30 \text{ Y}, 0.23 \text{ Mg} \rightarrow 1 \text{ Ce}$
$\text{Na}_{49.2}\text{Ba}_{28.8}\text{Li}_{22.0}$	7, 10, 3	58, 38, 26	-
<i>Subtype IV</i> (1 structure)			
$\text{Na}_{49.1}\text{Sn}_{26.3}\text{In}_{24.6}$	1, 4, 3	56, 30, 28	$48h6: 0.83 \text{ In}, 0.17 \text{ Sn} \rightarrow 1 \text{ In}$

Table 28

Details on the performed *ab initio* calculations for structures of space group $Fd\bar{3}m$. The data are given as described for Table 27.

Structure	<i>e</i> /atom	atoms/u.c.	Applied idealization steps
In _{70.7} K _{29.3}	13, 9	82, 34	-
Ga _{50.0} Na _{29.3} In _{20.7}	13, 7, 13	58, 34, 24	-
Ga _{48.9} Na _{30.4} Cd _{20.7}	13, 7, 12	48, 36, 32	8b: 0.49 → 1 Na; 32e1: 0.85 Cd, 0.15 Ga → 1 Cd; 96g2: 0.71 Cd, 0.29 Ga → 1 Cd
Ga _{63.0} Na _{31.0} Ag _{6.0}	13, 7, 11	48, 36, 32	32e1: 0.67 Ga, 0.33 Ag → 1 Ag; 96g2: 0.82 Ga, 0.18 Ag → 1 Ag
Ga _{53.4} Li _{31.0} Cu _{8.6} In _{6.9}	13, 3, 17, -	72, 36, 8, 0	96g4: 0.58 Ga, 0.42 Cu → 1 Ga
Ga _{47.5} Mg _{31.2} Cu _{21.3}	13, 8, 17	56, 36, 24	8a: 0.56 → 1 Mg; 32e1: 0.70 → 1 Ga
Zn _{61.0} Ca _{35.6} Ni _{3.4}	12, 8, 16	72, 42, 4	-

8. Electron localization function – (110) layers

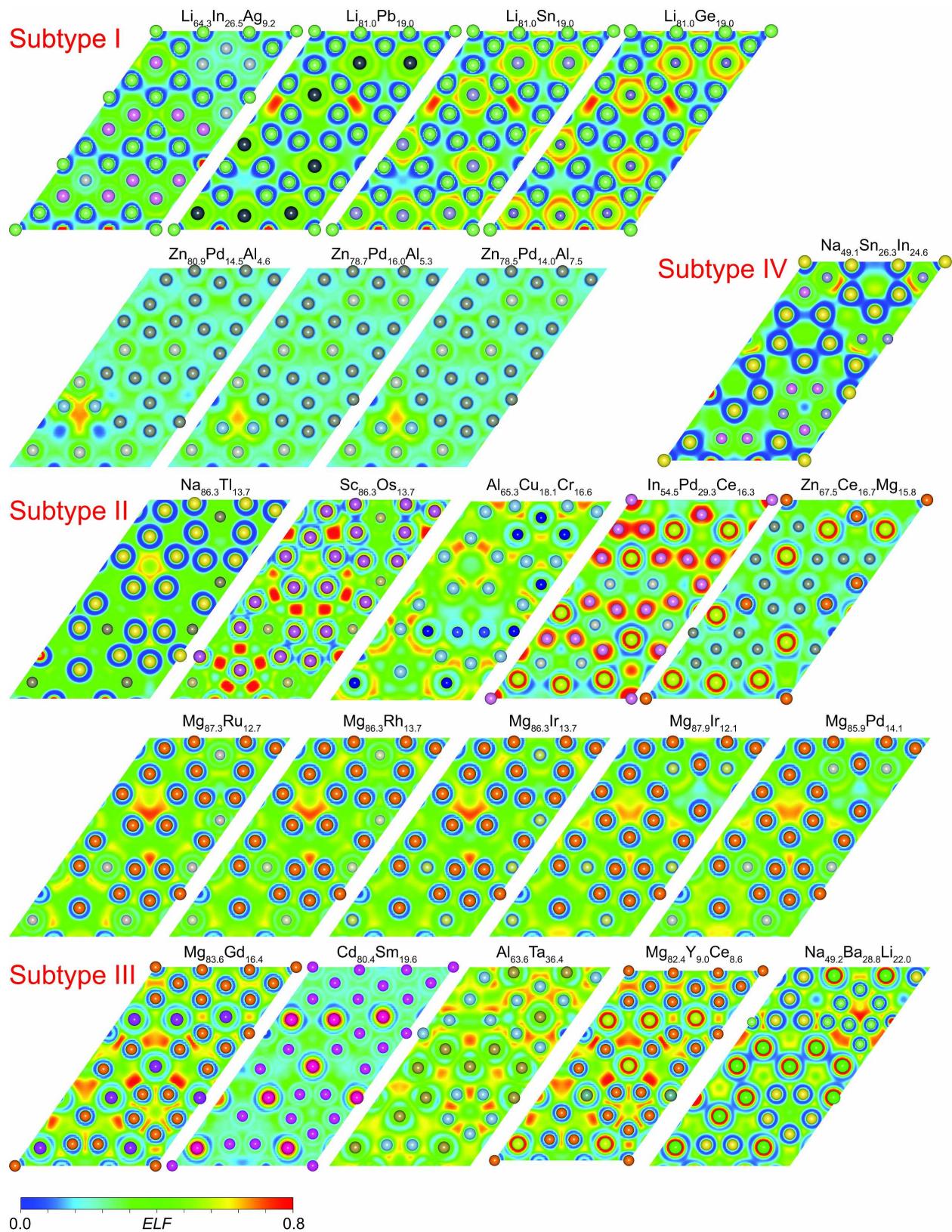


Figure 3
(110) layers of the ELFs of cubic complex intermetallics in the $F\bar{4}3m$ space group – structures with values $ELF > 0.5$.

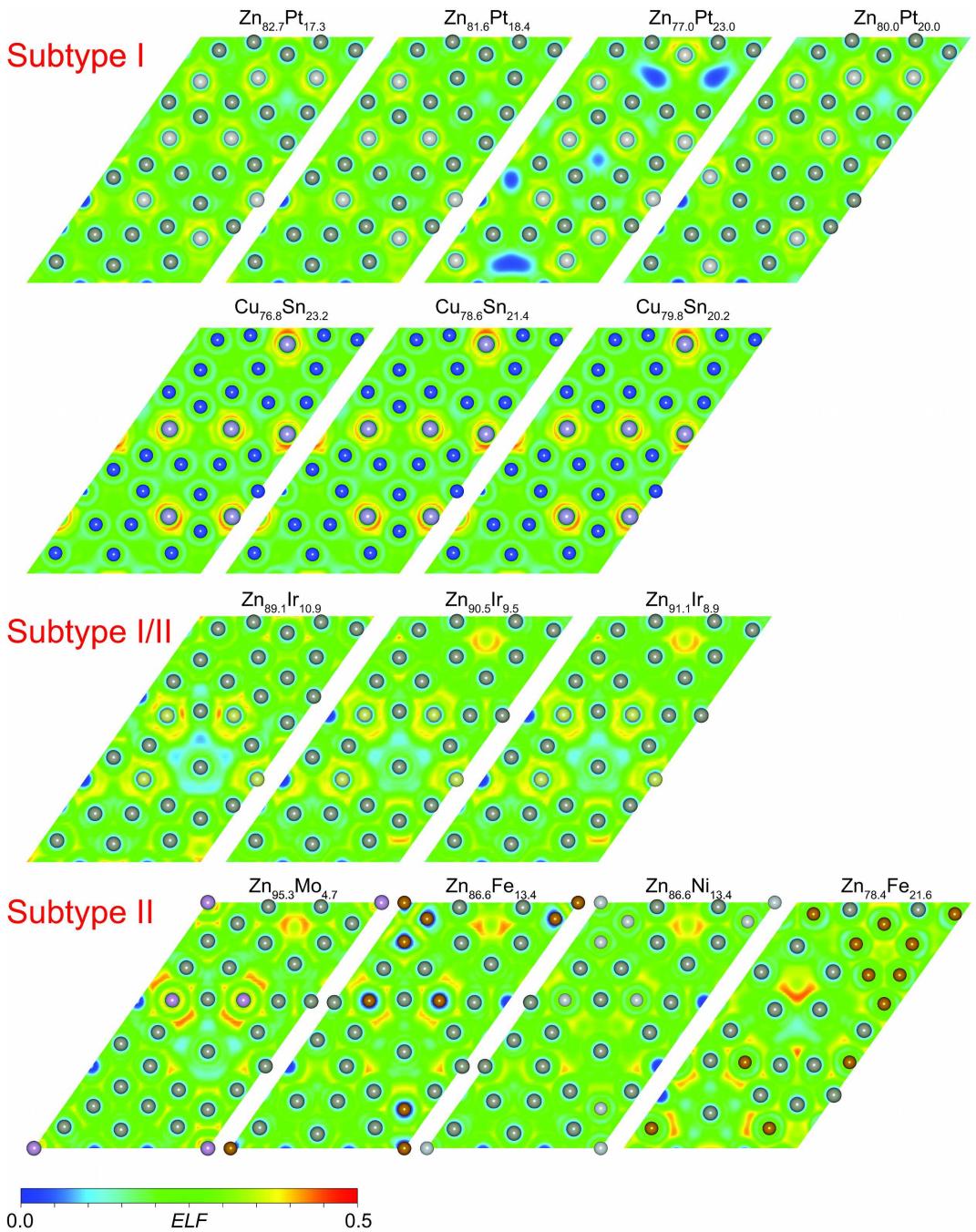


Figure 4

(110) layers of the ELFs of cubic complex intermetallics in the $F\bar{4}3m$ space group – structures only with values $ELF < 0.5$. Due to structural ambiguities as reported, the $Cu_{73.9}Sn_{23.2}Ni_{2.9}$ was simulated as $Cu_{76.8}Sn_{23.2}$ and is also inscribed in this way. Similarly, the structure of $Zn_{86.6}Fe_{6.7}Ni_{6.7}$ was simulated in the variants $Zn_{86.6}Fe_{13.4}$ and $Zn_{86.6}Ni_{13.4}$.

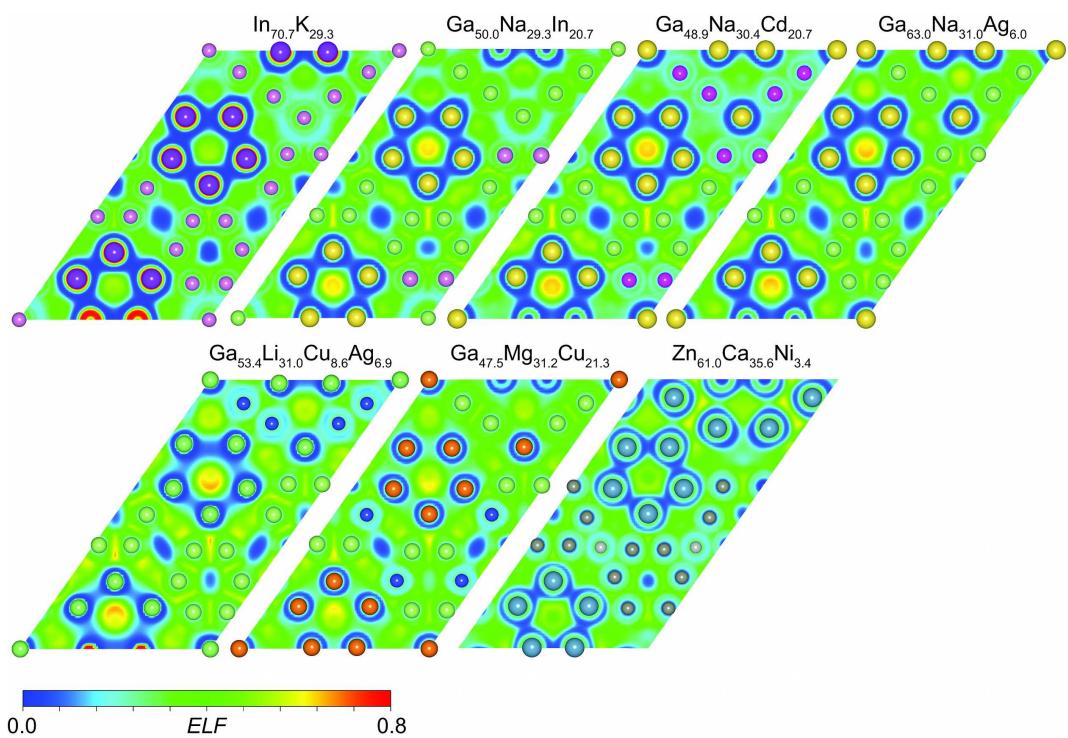


Figure 5

(110) layers of the ELFs of cubic complex intermetallics in the $Fd\bar{3}m$ space group. The structures are labeled with their respective chemical formulas.

9. Bader charge analysis

Table 29

Bader charges of cubic complex intermetallics *cF*464 in space group *F*43*m*, ($3 \times 3 \times 3$)-fold superstructures of a common basic structure. Given are for all calculated structures the Bader charges, expressed by the electron difference with respect to neutral atoms, for the different atomic sorts. The structures Cu_{73.9}Sn_{23.2}Ni_{2.9} and Zn_{86.6}Fe_{6.7}Ni_{6.7} had to be calculated in the variants Cu_{76.8}Sn_{23.2} and Zn_{86.6}Fe_{13.4}, as well as Zn_{86.6}Ni_{13.4}, respectively.

Composition	Only atomic basins				With bond basins			
	Majority atoms Element	Electrons	Minority atoms Element	Electrons	Altered atoms Element	Electrons	Bond basins No. × Electrons	Shape
Space group <i>F</i>43<i>m</i> – Subtype I								
Li _{64.3} In _{26.5} Ag _{9.2}	Li	-0.9..-0.8	In	+0.8..+1.6	no bond basins			
			Ag	+1.0..+1.3				
Li _{81.0} Pb _{19.0}	Li	-0.8..-0.7	Pb	+3.1..+3.7	Li	≈ -0.8	4×+0.1	(triangle)
Li _{81.0} Sn _{19.0}	Li	-0.8..-0.6	Sn	+3.1..+3.7	Li	≈ -0.8	4×+0.2	(triangle)
Li _{81.0} Ge _{19.0}	Li	-0.8..-0.5	Ge	+3.1..+3.6	Li	≈ -0.8	4×+0.3	(triangle)
Zn _{80.9} Pd _{14.5} Al _{4.6}	Zn	-0.2..-0.0	Pd	+0.6..+1.1	no bond basins			
			Al	≈ -1.2				
Zn _{82.7} Pt _{17.3}	Zn	-0.3..-0.1	Pt	+1.0..+1.1	no bond basins			
Zn _{81.6} Pt _{18.4}	Zn	-0.3..-0.1	Pt	+1.0..+1.1	no bond basins			
Zn _{78.7} Pd _{16.0} Al _{5.3}	Zn	-0.2..-0.0	Pd	+0.6..+1.1	no bond basins			
			Al	≈ -1.2				
Zn _{77.0} Pt _{23.0}	Zn	-0.4..-0.3	Pt	+0.9..+1.1	no bond basins			
Zn _{80.0} Pt _{20.0}	Zn	-0.3..-0.2	Pt	+1.0..+1.1	no bond basins			
Zn _{78.5} Pd _{14.0} Al _{7.5}	Zn	-0.2..-0.0	Pd	+0.6..+1.2	no bond basins			
			Al	≈ -1.3				
Cu _{76.8} Sn _{23.2}	Cu	+0.0..+0.1	Sn	-0.3..-0.2	no bond basins			
Cu _{78.6} Sn _{21.4}	Cu	+0.0..+0.1	Sn	-0.3..-0.2	no bond basins			
Cu _{79.8} Sn _{20.2}	Cu	+0.0..+0.1	Sn	-0.3..-0.2	no significant bond basins			
Space group <i>F</i>43<i>m</i> – Subtype I/II								
Zn _{89.1} Ir _{10.9}	Zn	-0.4..+0.1	Ir	≈ +1.2	no bond basins			
Zn _{90.5} Ir _{9.5}	Zn	-0.3..+0.1	Ir	≈ +1.2	no bond basins			
Zn _{91.1} Ir _{8.9}	Zn	-0.3..+0.1	Ir	≈ +1.2	no bond basins			
Space group <i>F</i>43<i>m</i> – Subtype II								
Na _{86.3} Tl _{13.7}	Na	-0.6..-0.0	Tl	+2.4..+2.8	no bond basins			
Sc _{86.3} Os _{13.7}	Sc	-1.1..+0.4	Os	+3.4..+3.5	Sc	-1.1..-0.5	41×+0.3..+0.4	(covalent bond)
Mg _{87.3} Ru _{12.7}	Mg	-1.3..-0.3	Ru	+5.5..+6.7	-	-	6×+0.9	(p)
Mg _{86.3} Rh _{13.7}	Mg	-1.3..-0.3	Rh	+5.4..+6.5	Rh	-1.3..-0.5	6×+1.1	(p)
Mg _{87.9} Ir _{12.1}	Mg	-1.4..+0.8	Ir	+5.4..+6.8	-	-	6×+0.4	(h)
Mg _{85.9} Pd _{14.1}	Mg	-1.3..+0.7	Pd	+4.6..+5.9	-	-	6×+0.5	(h)
Mg _{86.3} Ir _{13.7}	Mg	-1.4..-0.2	Ir	+5.7..+6.8	Ir	-1.4..-0.5	6×+1.3	(p)
Zn _{95.3} Mo _{4.7}	Zn	-0.8..+0.2	Mo	-0.1..+0.2	no bond basins			
Al _{65.3} Cu _{18.1} Cr _{16.6}	Al	-0.7..-0.3	Cr/Cu	+0.6..+2.3	no bond basins			
Zn _{86.6} Fe _{13.4}	Zn	-0.1..+0.1	Fe	+0.1..+0.3	no bond basins			
Zn _{86.6} Ni _{13.4}	Zn	-0.2..+0.1	Ni	+0.1..+0.4	no bond basins			
Zn _{78.4} Fe _{21.6}	Zn	-0.1..+0.0	Fe	+0.1..+0.3	no bond basins			
Space group <i>F</i>43<i>m</i> – Subtype II'								
In _{54.5} Pd _{29.3} Ce _{16.3}	In	-0.2..+0.3	Pd	+0.8..+1.0	no bond basins			
			Ce	-1.4..-1.3				
Zn _{67.5} Ce _{16.7} Mg _{15.8}	Zn	+0.2..+0.8	Ce	-1.3..-1.1	no bond basins			
			Mg	≈ -1.4				
Space group <i>F</i>43<i>m</i> – Subtype III								
Mg _{83.6} Gd _{16.4}	Mg	-0.4..+0.5	Gd	-0.6..-0.3	-	-	17×+0.2..+0.5	(covalent bond)
Cd _{80.4} Sm _{19.6}	Cd	+0.1..+0.5	Sm	-1.3..-1.2	no bond basins			
Al _{63.6} Ta _{36.4}	Al	-0.4..+0.1	Ta	-0.3..+0.6	Al	-0.4..-0.0	15×+0.2	(covalent bond)
Mg _{82.4} Y _{9.0} Ce _{8.6}	Mg	-0.6..+0.6	Y	≈ -0.9	-	-	31×+0.1..+0.8	(diverse)
			Ce	-0.4..-0.2				
Na _{49.2} Ba _{28.8} Li _{22.0}	Na	-0.1..+0.4	Ba	-0.3..+0.1	Li	≈ -0.8	65×+0.0..+4.0	(diverse)
			Li	-0.8..+3.8				
Space group <i>F</i>43<i>m</i> – Subtype IV								
Na _{49.1} Sn _{26.3} In _{24.6}	Na	-0.8..-0.7	In	+0.4..+0.6	no bond basins			
			Sn	+0.9..+1.1				

Table 30

Bader charges of cubic complex intermetallics *cF464* in space group *Fd* $\bar{3}m$, ($3 \times 3 \times 3$)-fold superstructures of a common basic structure. Given are for all calculated structures the Bader charges, expressed by the electron difference with respect to neutral atoms, for the different atomic sorts.

Composition	Only atomic basins				With bond basins			
	Majority atoms		Minority atoms		Altered atoms		Bond basins	
	Element	Electrons	Element	Electrons	Element	Electrons	No. \times Electrons	Shape
Space group <i>Fd</i>$\bar{3}m$								
In _{70.7} K _{29.3}	In	+0.0..+0.3	K	≈ -0.7	<i>no bond basins</i>			
Ga _{50.0} Na _{29.3} In _{20.7}	Ga	+0.0..+0.3	Na	≈ -0.8	<i>no bond basins</i>			
			In	$\approx +0.4$				
Ga _{48.9} Na _{30.4} Cd _{20.7}	Ga	$\approx +0.3$	Na	≈ -0.8	<i>no bond basins</i>			
			Cd	$\approx +0.4$				
Ga _{63.0} Na _{31.0} Ag _{6.0}	Ga	+0.3..+0.4	Na	≈ -0.8	<i>no bond basins</i>			
			Ag	+0.4..+0.5				
Ga _{53.4} Li _{31.0} Cu _{8.6} In _{6.9}	Ga	+0.3..+0.4	Li	≈ -0.9	<i>no bond basins</i>			
			Cu	$\approx +0.6$				
Ga _{47.5} Mg _{31.2} Cu _{21.3}	Ga	+0.5..+0.6	Mg	≈ -1.5	<i>no bond basins</i>			
			Cu	$\approx +0.1$				
Zn _{61.0} Ca _{35.6} Ni _{3.4}	Zn	+0.5..+1.0	Ca	≈ -1.2	<i>no bond basins</i>			
			Ni	$\approx +0.4$				

10. Density of states

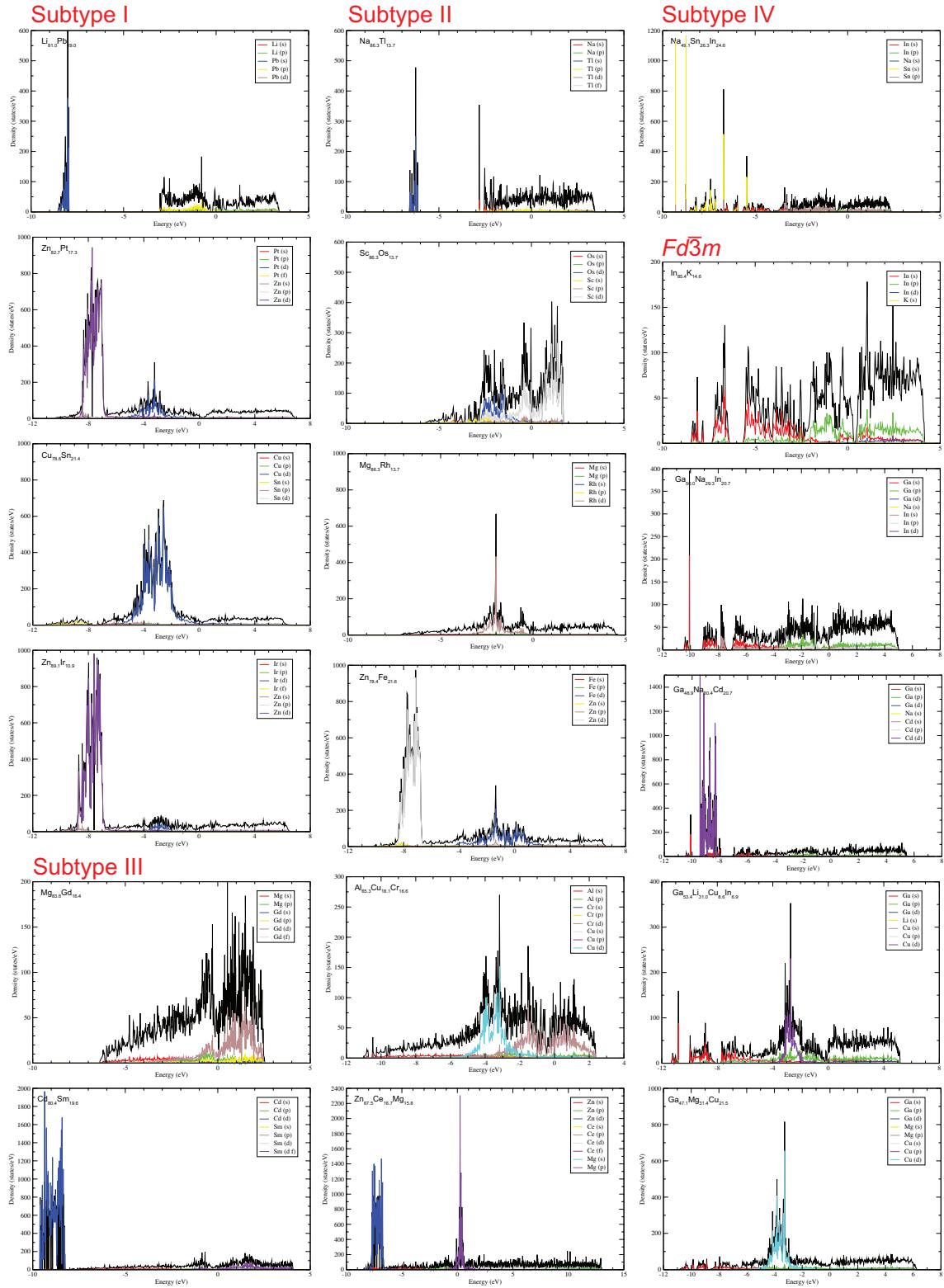


Figure 6

Density of states (DOS) graphs for representatives of the investigated structures ($cF(464 - x)$).