

**Supplementary Table 1** Atomic coordinates and equivalent displacement parameters for the subcell of  $\text{Co}_6\text{Al}_{11-x}\text{Si}_{6+x}$  (space group  $Pnma$ ,  $a = 21.3536(9)$  Å,  $b = 4.0420(3)$  Å,  $c = 7.2723(3)$  Å)

Atom	Site	$x$	$y$	$z$	$B_{\text{eq}}^*$
Co1	4c	0.54226(3)	1/4	0.49382(9)	0.58(1)
Co2	4c	0.22763(3)	1/4	0.87550(9)	0.61(1)
Co3	4c	0.91187(3)	1/4	0.46546(9)	0.55(1)
Al1	4c	0.03447(8)	1/4	0.4378(2)	0.95(3)
Al2	4c	0.11743(8)	1/4	0.7250(2)	0.91(3)
Al3	4c	0.27541(9)	1/4	0.5637(2)	1.02(3)
Al4	4c	0.79738(7)	1/4	0.3137(2)	0.77(3)
Al5	4c	0.43629(8)	1/4	0.6941(2)	0.90(3)
Si1	4c	0.64451(6)	1/4	0.4283(2)	0.86(3)
Si2	4c	0.45372(6)	1/4	0.3242(2)	0.61(2)
Al6**	4c	0.1665(2)	1/4	0.3940(6)	2.15(9)
Si3**	8d	0.32961(9)	0.4322(6)	0.8611(3)	1.16(4)

\* $B_{\text{eq}} = 1/3(B_{11}(a^*)^2a^2 + \dots + B_{33}b^*c^*bc \cos\alpha)$

\*\*Occupancy 0.50

**Supplementary Table 2** Atomic coordinates and equivalent displacement parameters for  $\text{Co}_6\text{Al}_{1-x}\text{Si}_{6+x}$  (space group  $Cmca$ ,  $a = 8.0839(6)$  Å,  $b = 14.5445(6)$  Å,  $c = 21.3536(9)$  Å)

Atom	Site	$x$	$y$	$z$	$B_{\text{eq}}/B_{\text{iso}}$
Co1a	4a	0	0.11818(4)	0.54320(4)	0.44(1)
Co1b	4a	1/2	0.12601(5)	0.54130(3)	0.61(1)
Co1c	8b	0.25068(6)	0.37188(3)	-0.04220(2)	0.536(9)
Co2a	4a	0	0.30975(5)	0.22564(3)	0.56(1)
Co2b	4a	1/2	0.31620(4)	0.22948(3)	0.58(1)
Co2c	8b	0.24445(6)	0.56261(3)	0.27231(2)	0.480(9)
Co3a	4a	0	0.10700(5)	0.91111(3)	0.51(1)
Co3b	4a	1/2	0.10836(5)	0.91275(3)	0.52(1)
Co3c	8b	0.24274(6)	0.35786(3)	-0.41175(2)	0.455(9)
Al1a	4a	0	0.0901(1)	0.03744(8)	0.98(4)
Al1b	4a	1/2	0.0965(1)	0.03168(8)	1.05(4)
Al1c	8b	0.2530(1)	0.34438(7)	0.46557(5)	0.69(2)
Al2a	4a	0	0.2310(1)	0.12011(8)	0.69(3)
Al2b	4a	1/2	0.2448(1)	0.11492(8)	0.61(3)
Al2c	8b	0.2469(1)	0.48707(7)	0.38253(5)	0.74(2)
Al3a	4a	0	0.1529(1)	0.26891(7)	0.46(3)
Al3b	4a	1/2	0.1604(1)	0.28149(7)	0.47(3)
Al3c	8b	0.2456(1)	0.40704(7)	0.22435(6)	0.88(2)
Al4a	4a	0	0.0296(1)	0.79798(8)	0.81(3)
Al4b	4a	1/2	0.0325(1)	0.79676(8)	0.80(3)
Al4c	8b	0.2411(1)	0.28261(7)	-0.29739(5)	0.55(2)
Al5a	4a	0	0.2230(1)	0.43839(8)	0.56(3)
Al5b	4a	1/2	0.2219(1)	0.43382(8)	0.69(3)
Al5c	8b	0.2415(2)	0.47172(7)	0.06359(6)	0.97(2)
Si1a	4a	0	0.08561(9)	0.64497(7)	0.66(3)
Si1b	4a	1/2	0.0940(1)	0.64266(7)	0.78(3)
Si1c	8b	0.2566(1)	0.33853(7)	-0.14521(5)	0.80(2)
Si2a	4a	0	0.03663(9)	0.45336(7)	0.53(3)
Si2b	4a	1/2	0.03691(9)	0.45489(7)	0.58(3)
Si2c	8b	0.2478(1)	0.28731(6)	0.04658(5)	0.60(2)
Al6b	4a	1/2	0.0710(1)	0.16608(8)	0.85(2)**
Al6c*	8b	0.2756(4)	0.3235(2)	0.3326(2)	2.68(6)**
Si3a*	4a	0.0667(3)	0.2997(2)	0.3293(1)	1.53(4)**
Si3b*	8b	0.6050(3)	0.3096(2)	0.3294(1)	1.78(4)**
Si3c	8b	0.3423(1)	0.55612(6)	0.17003(5)	0.15(1)**

\*Occupancy 0.50

\*\*Refined with isotropic displacement parameters

**Supplementary Table 3** Atomic coordinates and equivalent displacement parameters for  $\text{Co}_6\text{Al}_{1-x}\text{Si}_{6+x}$  described in the space group  $P2_1/c$  ( $mP92$ ,  $a = 8.0839(3)$  Å,  $b = 21.3536(9)$  Å,  $c = 8.3200(3)$  Å,  $\beta = 119.07(1)^\circ$ )

Atom	Site	$x$	$y$	$z$	$B_{\text{eq}}$
Co1a	4e	0.11939(9)	0.54291(2)	0.48884(4)	0.34(2)
Co1b	4e	0.6252(1)	0.54156(2)	0.49908(5)	0.48(2)
Co2a	4e	0.31363(8)	0.22636(2)	0.87130(4)	0.40(2)
Co2b	4e	0.80980(8)	0.22893(2)	0.87974(5)	0.38(2)
Co3a	4e	0.11219(9)	0.91134(2)	0.46455(5)	0.34(2)
Co3b	4e	0.60259(9)	0.91238(2)	0.46635(5)	0.36(2)
Al1a	4e	0.0903(2)	0.03647(4)	0.4336(1)	0.82(4)
Al1b	4e	0.5989(2)	0.03256(4)	0.4417(1)	0.73(4)
Al2a	4e	0.2341(2)	0.11922(4)	0.7153(1)	0.66(3)
Al2b	4e	0.7403(2)	0.11586(4)	0.7349(1)	0.60(3)
Al3a	4e	0.1556(2)	0.27093(4)	0.5582(1)	0.59(3)
Al3b	4e	0.6553(2)	0.27999(4)	0.5692(1)	0.60(3)
Al4a	4e	0.0379(2)	0.79780(4)	0.3118(1)	0.59(3)
Al4b	4e	0.5265(2)	0.79689(4)	0.3156(1)	0.60(3)
Al5a	4e	0.2270(2)	0.43789(4)	0.6949(1)	0.70(4)
Al5b	4e	0.7157(2)	0.43464(4)	0.6935(1)	0.74(4)
Si1a	4e	0.0808(2)	0.64537(3)	0.4227(1)	0.60(3)
Si1b	4e	0.5962(2)	0.64371(4)	0.4338(1)	0.76(3)
Si2a	4e	0.0387(2)	0.45328(3)	0.32398(9)	0.49(3)
Si2b	4e	0.5363(2)	0.45430(3)	0.32431(9)	0.54(4)
Al6a	4e	0.5850(2)	0.16641(5)	0.3946(1)	1.99(3)
Si3a	4e	0.2222(1)	0.32954(5)	0.8560(1)	1.16(3)
Si3b	4e	0.9078(1)	0.32982(5)	0.8661(1)	0.97(3)