

Supporting Online Material

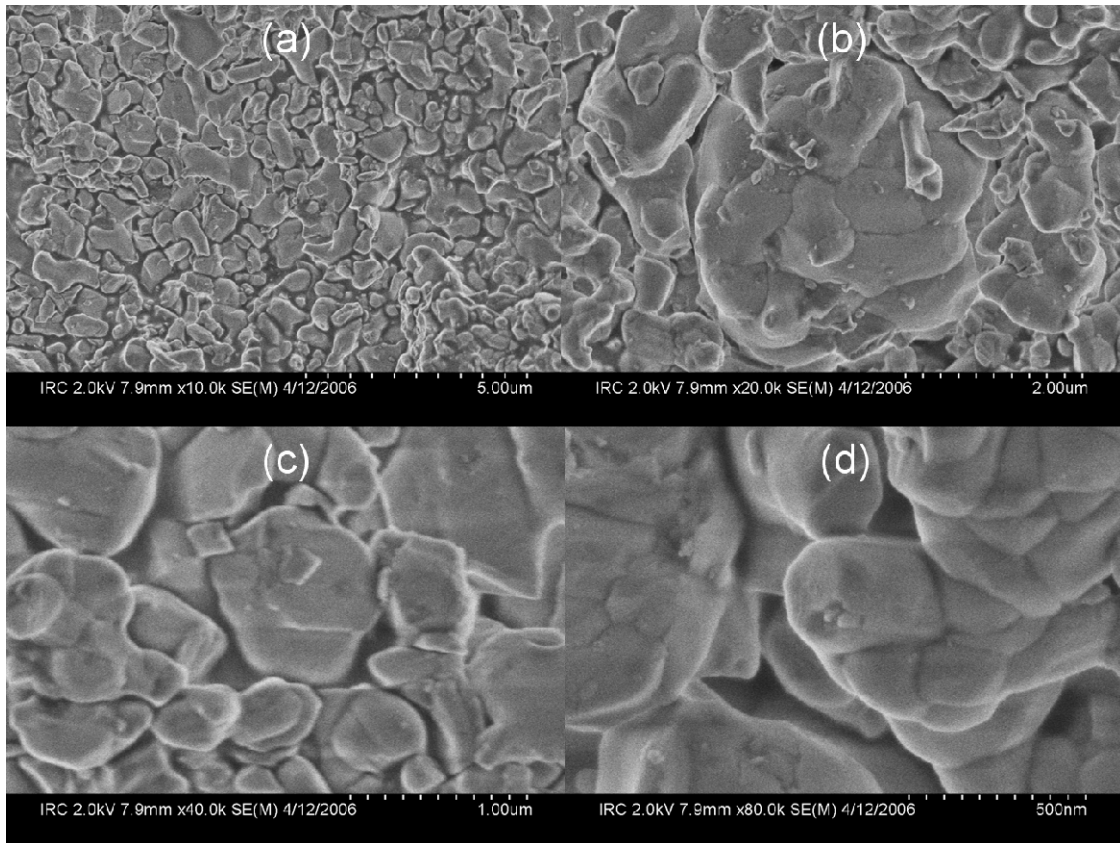


Figure S1a. SEI of $\text{Ca}_{10}(\text{AsO}_4)_6\text{F}_2$. (a) 10 (b) 20 (c) 40 (d) 80 magnification ($\times 1000$).

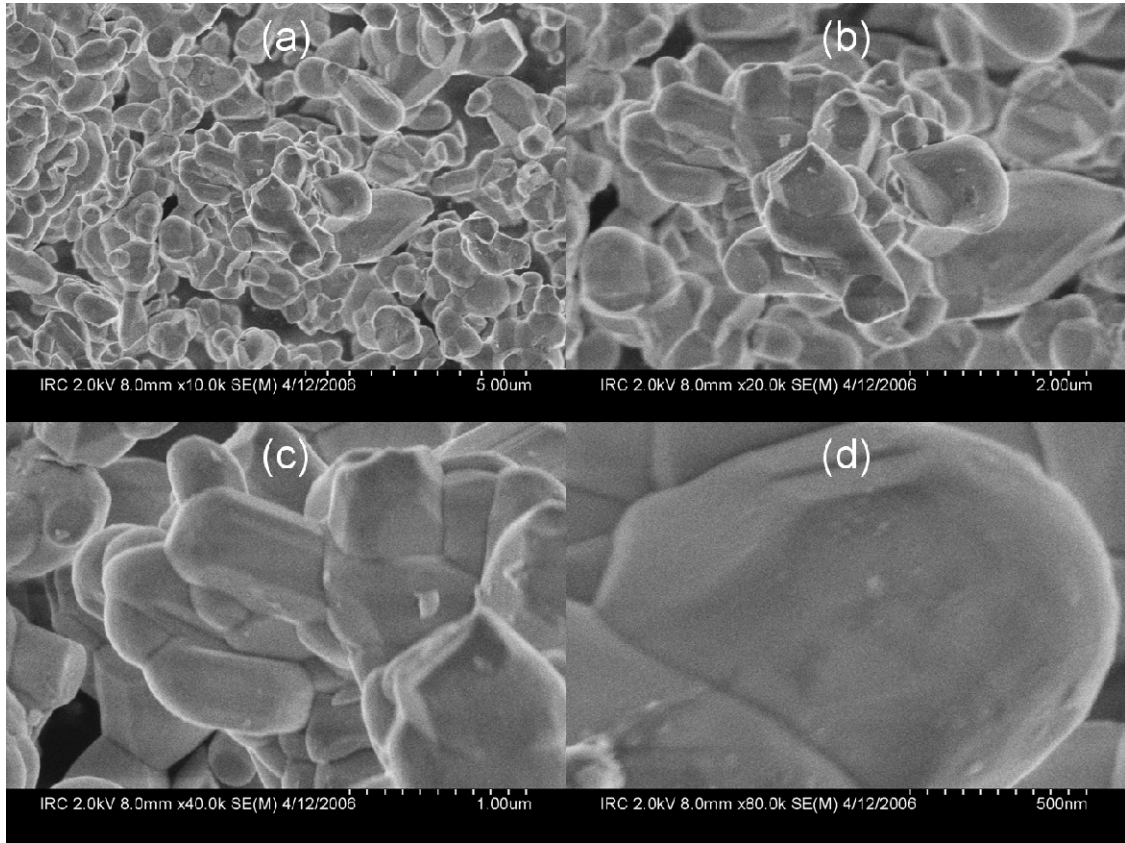


Figure S1b. SEI of $\text{Ca}_{10}(\text{VO}_4)_6\text{F}_2$. (a) 10 (b) 20 (c) 40 (d) 80 magnification ($\times 1000$).

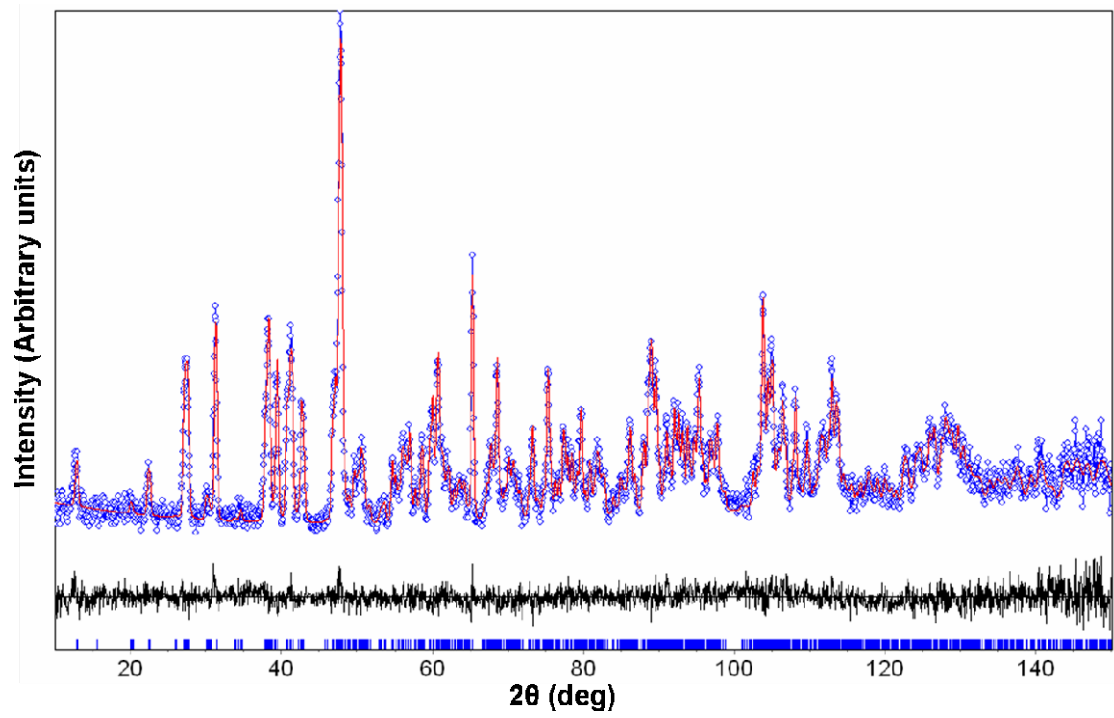
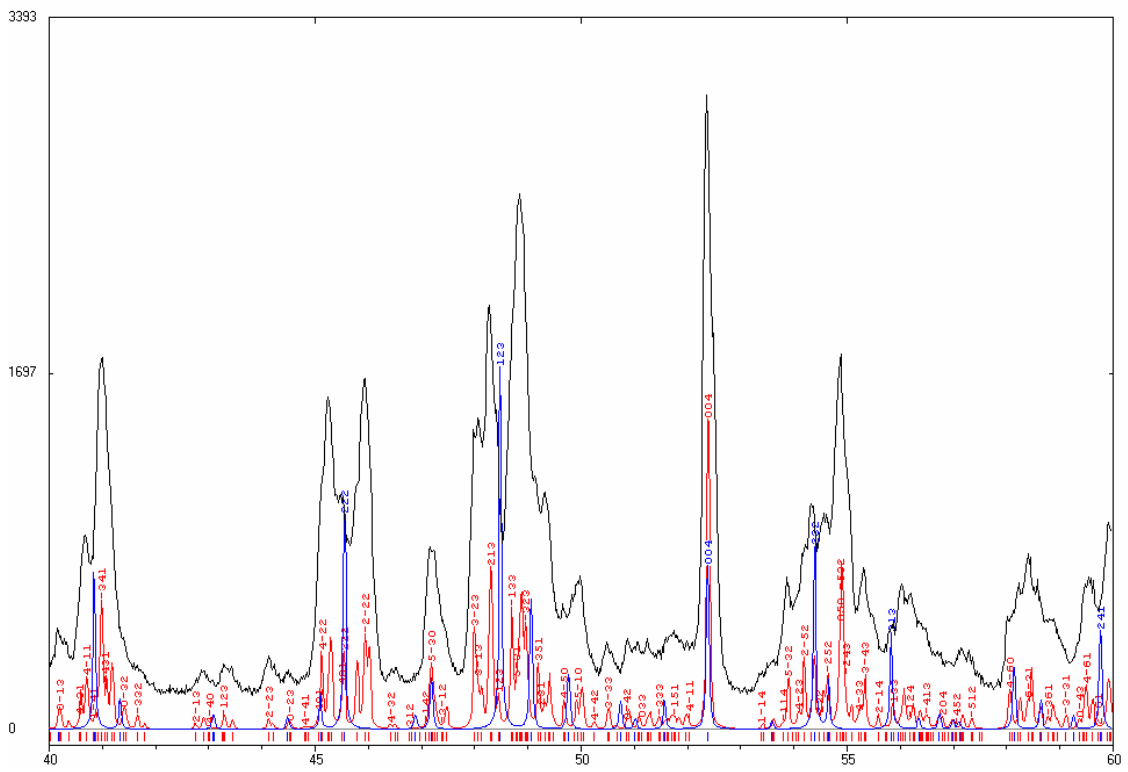
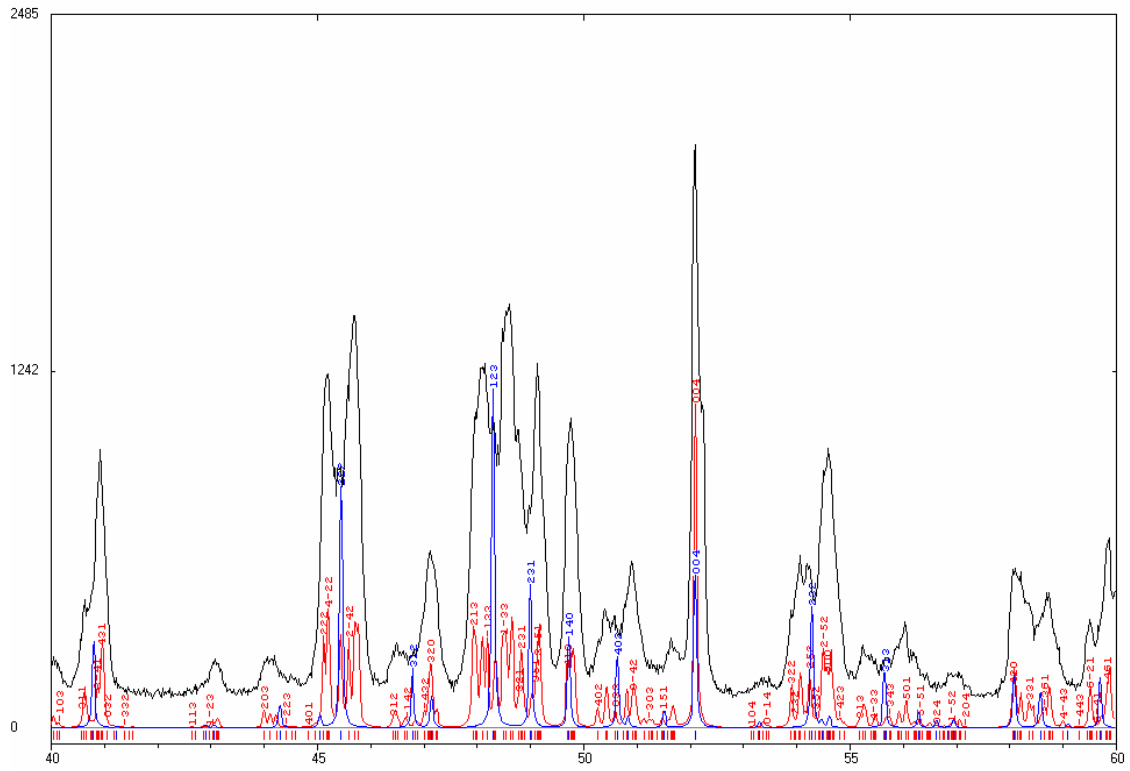


Figure S2a. (top) PXRD pattern of $\text{Ca}_{10}(\text{AsO}_4)_6\text{F}_2$ (black) compared with calculated reflection positions for hexagonal $P6_3/m$ (blue) and $P-1$ (red) symmetries. (bottom) Neutron diffraction refinement profile for $\text{Ca}_{10}(\text{AsO}_4)_6\text{F}_2$, showing the observed (blue), calculated (red) and difference profiles (black).



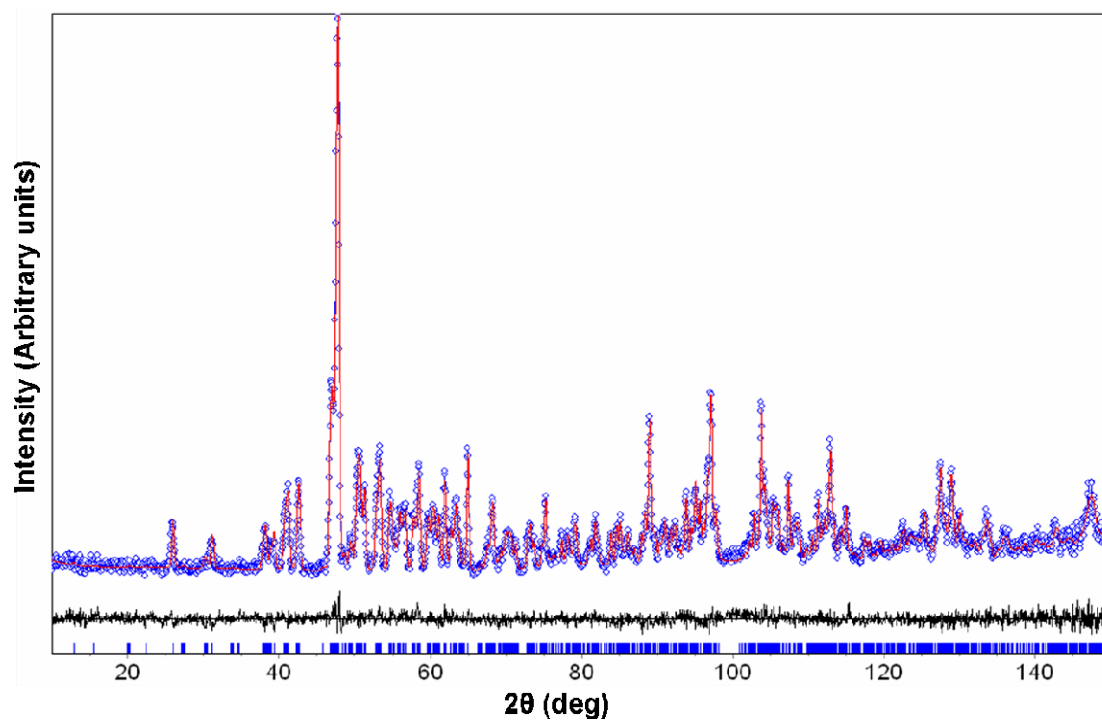


Figure S2b. (top) PXRD pattern of $\text{Ca}_{10}(\text{VO}_4)_6\text{F}_2$ (black) compared with calculated reflection positions for hexagonal $P6_3/m$ (blue) and $P-1$ (red) symmetries. (bottom) Neutron diffraction refinement profile for $\text{Ca}_{10}(\text{VO}_4)_6\text{F}_2$, showing the observed (blue), calculated (red) and difference profiles (black).

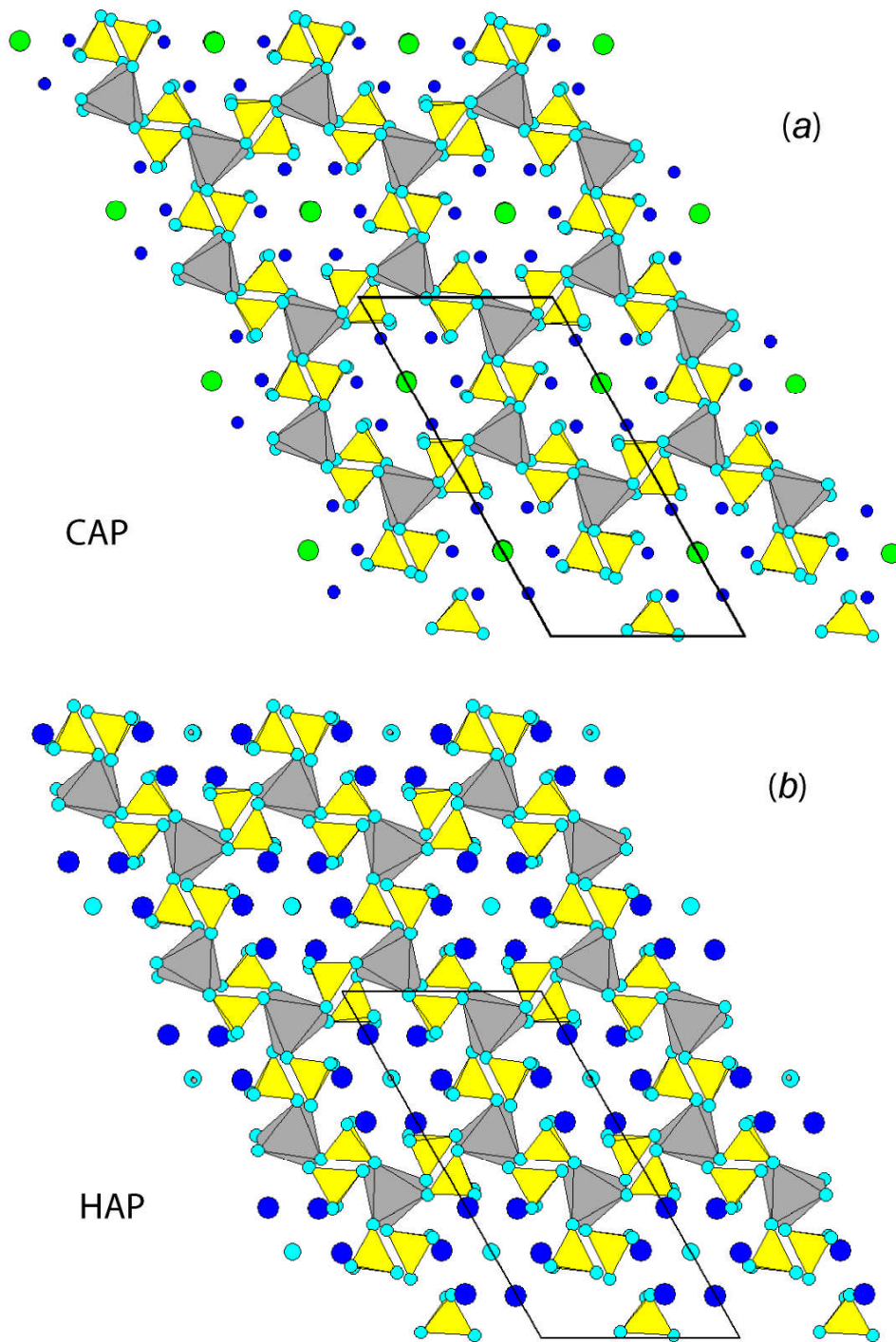


Figure S3. Polyhedral representation of monoclinic (a) $\text{Ca}_{10}(\text{PO}_4)_6\text{Cl}_2$ and (b) $\text{Ca}_{10}(\text{PO}_4)_6(\text{OH})_2$. The $\text{Ca}_4^{\text{I}}(\text{PO}_4)_6$ framework creates channels containing $\text{Ca}_6^{\text{II}}\text{Cl}_2$ or $\text{Ca}_6^{\text{II}}(\text{OH})_2$. Note the slight rotation of the

PO₄ tetrahedra to satisfy bond valence requirements and the doubling of the *b*-axis through destruction of the mirror plane and the creation of a *b*-glide.

Table S1a. Neutron diffraction Rietveld refinement of Ca₁₀(AsO₄)₆F₂.

| Space Group | | <i>P</i> -1 | | |
|---|--------------------------------|------------------------|----------|----------|
| <i>a</i> = 9.6841(5) Å | <i>b</i> = 9.6906(5) Å | <i>c</i> = 6.9815(3) Å | | |
| <i>α</i> = 90.623(3)° | <i>β</i> = 88.869(3)° | <i>γ</i> = 120.371(3)° | | |
| <i>R</i> _{Bragg} = 1.7 % | <i>R</i> _{wp} = 6.8 % | | | |
| <i>a/b</i> = 0.9993 | <i>c/b</i> = 0.7204 | | | |
| Atom | <i>x</i> | <i>y</i> | <i>z</i> | <i>B</i> |
| Ca1 | 0.234(2) | 0.990(2) | 0.249(3) | 0.8(3) |
| Ca2 | 0.005(2) | 0.251(2) | 0.262(3) | 0.7(2) |
| Ca3 | 0.770(2) | 0.767(2) | 0.245(2) | 0.7(3) |
| Ca4 | 0.345(2) | 0.653(2) | 0.003(2) | 0.9(4) |
| Ca5 | 0.343(2) | 0.681(2) | 0.499(2) | 1.0(3) |
| As1 | 0.398(1) | 0.374(1) | 0.261(2) | 0.4(2) |
| As2 | 0.628(1) | 0.024(1) | 0.239(2) | 0.5(2) |
| As3 | 0.975(2) | 0.606(1) | 0.243(2) | 0.7(2) |
| O1 | 0.311(2) | 0.480(2) | 0.275(2) | 0.6(2) |
| O2 | 0.510(2) | 0.827(2) | 0.243(2) | 0.8(2) |
| O3 | 0.173(2) | 0.681(2) | 0.226(2) | 1.0(3) |
| O4 | 0.604(2) | 0.475(2) | 0.277(2) | 0.8(2) |
| O5 | 0.530(2) | 0.124(2) | 0.220(2) | 1.1(2) |
| O6 | 0.878(2) | 0.407(2) | 0.274(2) | 1.2(2) |
| O7 | 0.351(2) | 0.263(2) | 0.063(2) | 1.4(3) |
| O8 | 0.774(2) | 0.079(2) | 0.072(2) | 1.4(3) |
| O9 | 0.905(2) | 0.639(2) | 0.040(2) | 1.1(2) |
| O10 | 0.669(2) | 0.766(2) | 0.552(2) | 0.9(2) |
| O11 | 0.274(2) | 0.907(2) | 0.555(2) | 1.1(2) |
| O12 | 0.068(2) | 0.301(2) | 0.584(2) | 1.3(2) |
| F1 | 0.007(2) | 0.007(2) | 0.245(2) | 0.8(2) |
| All sites are fully occupied Wyckoff positions of the type 2i | | | | |

Table S1b. Combined neutron/X-ray Rietveld refinement of Ca₁₀(VO₄)₆F₂.

| Space Group | | <i>P</i> -1 | | |
|------------------------|------------------------|------------------------|--|--|
| <i>a</i> = 9.6987(4) Å | <i>b</i> = 9.6933(4) Å | <i>c</i> = 7.0171(2) Å | | |

| Site | x | y | z | Beq. |
|------------|----------|----------|----------|--------|
| Ca1 | 0.244(2) | 0.004(2) | 0.250(2) | 0.7(2) |
| Ca2 | 0.001(2) | 0.245(2) | 0.261(2) | 0.7(2) |
| Ca3 | 0.762(2) | 0.769(1) | 0.244(2) | 0.4(2) |
| Ca4 | 0.339(2) | 0.654(2) | 0.000(2) | 1.0(3) |
| Ca5 | 0.336(2) | 0.677(2) | 0.497(2) | 1.5(3) |
| V1 | 0.396* | 0.373* | 0.257* | 1.0* |
| V2 | 0.633* | 0.026* | 0.248* | 1.0* |
| V3 | 0.970* | 0.602* | 0.240* | 1.0* |
| O1 | 0.310(1) | 0.486(1) | 0.267(2) | 0.9(2) |
| O2 | 0.510(1) | 0.827(1) | 0.249(2) | 1.2(2) |
| O3 | 0.176(2) | 0.689(2) | 0.230(2) | 2.0(3) |
| O4 | 0.604(2) | 0.474(1) | 0.270(2) | 1.4(2) |
| O5 | 0.527(1) | 0.129(1) | 0.224(1) | 0.7(2) |
| O6 | 0.870(2) | 0.404(2) | 0.271(2) | 2.0(3) |
| O7 | 0.342(1) | 0.256(2) | 0.064(2) | 1.2(2) |
| O8 | 0.765(2) | 0.074(1) | 0.071(2) | 1.5(2) |
| O9 | 0.901(2) | 0.647(1) | 0.049(2) | 1.7(2) |
| O10 | 0.662(2) | 0.758(2) | 0.555(2) | 1.3(2) |
| O11 | 0.266(2) | 0.903(2) | 0.550(2) | 1.4(2) |
| O12 | 0.069(1) | 0.308(1) | 0.575(2) | 0.7(2) |
| F | 0.006(2) | 0.005(2) | 0.252(2) | 2.1(2) |

All sites are fully occupied Wyckoff positions of the type 2i.
*Atom coordinates for V sites were evaluated by Rietveld refinement of XRD powder data; the same value of isotropic thermal displacement parameter *Beq* was assumed for all three V sites.

Table S2. Selected bond distances (Å) for Ca₁₀(AsO₄)₆F₂.

| | | | | | |
|---------|----------|---------|----------|---------|----------|
| Ca1-O3 | 2.744(3) | Ca2-O1 | 2.658(2) | Ca3-O2 | 2.853(2) |
| Ca1-O5 | 2.486(2) | Ca2-O6 | 2.376(2) | Ca3-O4 | 2.455(2) |
| Ca1-O7 | 2.636(3) | Ca2-O8 | 2.410(2) | Ca3-O7 | 2.414(2) |
| Ca1-O8 | 2.328(2) | Ca2-O9 | 2.319(2) | Ca3-O9 | 2.611(2) |
| Ca1-O10 | 2.482(2) | Ca2-O11 | 2.645(2) | Ca3-O10 | 2.329(2) |
| Ca1-O11 | 2.400(3) | Ca2-O12 | 2.322(2) | Ca3-O12 | 2.339(2) |
| Ca1-F1 | 2.290(2) | Ca2-F1 | 2.371(3) | Ca3-F1 | 2.301(1) |
| Ca4-O1 | 2.455(2) | Ca5-O1 | 2.376(2) | | |
| Ca4-O2 | 2.352(2) | Ca5-O2 | 2.326(2) | | |

| | | | | | |
|---------|----------|---------|----------|---------|----------|
| Ca4-O3 | 2.371(3) | Ca5-O3 | 2.540(3) | | |
| Ca4-O4 | 2.476(2) | Ca5-O4 | 2.420(3) | | |
| Ca4-O5 | 2.434(2) | Ca5-O5 | 2.573(2) | | |
| Ca4-O6 | 2.756(2) | Ca5-O6 | 2.430(2) | | |
| Ca4-O7 | 2.656(3) | Ca5-O10 | 2.860(3) | | |
| Ca4-O9 | 2.650(2) | Ca5-O11 | 2.617(3) | | |
| As1-O1 | 1.628(2) | As2-O2 | 1.664(2) | As3-O3 | 1.676(2) |
| As1-O4 | 1.726(2) | As2-O5 | 1.667(3) | As3-O6 | 1.679(2) |
| As1-O7 | 1.668(2) | As2-O8 | 1.681(2) | As3-O9 | 1.688(2) |
| As1-O10 | 1.756(2) | As2-O11 | 1.669(2) | As3-O12 | 1.674(2) |
| <As1-O> | 1.695 | <As2-O> | 1.670 | <As3-O> | 1.679 |

Table S3. Comparison of the number of refined parameters and agreement factors R_{wp} and R_{Bragg} for different structural models of $\text{Ca}_{10}(\text{AsO}_4)_6\text{F}_2$ and $\text{Ca}_{10}(\text{VO}_4)_6\text{F}_2$.

| Space Group | $P6_3/m$ | | $P2_1/m$ | | $P-1$ | |
|------------------------------|----------|------|----------|------|-------|------|
| | As-AP | V-AP | As-AP | V-AP | As-AP | V-AP |
| Formula | | | | | | |
| Number of refined parameters | 30 | 30 | 67 | 67 | 101 | 101 |
| Number of unique reflections | 236 | 236 | 699 | 700 | 1278 | 1291 |
| R_{wp} | 15.7 | 17.0 | 15.5 | 16.7 | 6.8 | 5.7 |
| R_{Bragg} | 4.9 | 6.7 | 7.0 | 8.7 | 1.7 | 1.7 |

Note: Unless otherwise stated all atom sites given in Tables 3-9 are Wyckoff positions of the type 2i of the P-1 space group.

Table S4. Energy minimised *ab initio* structure of $\text{Ca}_{10}(\text{AsO}_4)_6\text{F}_2$.

| Space group | | $P-1$ |
|---------------------------|---------------------------|---------------------------|
| $a = 9.61608 \text{ \AA}$ | $b = 9.64372 \text{ \AA}$ | $c = 6.95712 \text{ \AA}$ |
| $\alpha = 90.779^\circ$ | $\beta = 88.528^\circ$ | $\gamma = 120.613^\circ$ |
| $a/b = 0.9971$ | $c/b = 0.7214$ | |

| Atom | x | y | z |
|------|---------|---------|---------|
| Ca1 | 0.23637 | 0.99456 | 0.25593 |
| Ca2 | 0.00493 | 0.24847 | 0.26412 |
| Ca3 | 0.76322 | 0.77124 | 0.23253 |
| Ca4 | 0.33899 | 0.64542 | 0.00121 |
| Ca5 | 0.34103 | 0.68771 | 0.49738 |
| As1 | 0.39836 | 0.37301 | 0.27354 |
| As2 | 0.63190 | 0.02683 | 0.23482 |
| As3 | 0.97770 | 0.61118 | 0.23576 |
| O1 | 0.30497 | 0.48335 | 0.28035 |
| O2 | 0.51222 | 0.82182 | 0.24163 |
| O3 | 0.18134 | 0.68997 | 0.22524 |
| O4 | 0.60559 | 0.48247 | 0.27908 |
| O5 | 0.52775 | 0.12661 | 0.20795 |
| O6 | 0.87568 | 0.40704 | 0.27131 |
| O7 | 0.35471 | 0.26566 | 0.06263 |
| O8 | 0.78115 | 0.08036 | 0.06649 |
| O9 | 0.89257 | 0.63895 | 0.03605 |
| O10 | 0.66596 | 0.76920 | 0.54600 |
| O11 | 0.27134 | 0.90136 | 0.54994 |
| O12 | 0.06161 | 0.28672 | 0.58705 |
| F | 0.00820 | 0.01189 | 0.24512 |

Table S5. Crystal structure model for $\text{Ca}_{10}(\text{VO}_4)_6\text{F}_2$ in the metrically hexagonal cell equivalent to that of Dong and White (2004). It is derived from Table 1 by 2% expansion of V-O bond lengths to accommodate the larger V^{5+} ion. Average valence sums are respectively 1.972, 1.948 and 5.022 v.u. at A^{I} , A^{II} and B showing that the triclinic distortion of apatites can relieve stresses at A^{II} and B sites through tilting/rotation of BO_4 tetrahedra, even in a metrically hexagonal cell.

| Space group | | <i>P</i> -1 | |
|--------------------------|--------------------------|--------------------------|---------|
| $a = 9.7364 \text{ \AA}$ | $b = 9.7364 \text{ \AA}$ | $c = 7.0057 \text{ \AA}$ | |
| $\alpha = 90.000^\circ$ | $\beta = 90.000^\circ$ | $\gamma = 120.000^\circ$ | |
| $a/b = 1.0000$ | $c/b = 0.7195$ | | |
| Atom | x | y | z |
| Ca1 | 0.23380 | 0.98980 | 0.24940 |
| Ca2 | 0.00470 | 0.25070 | 0.26170 |
| Ca3 | 0.76950 | 0.76690 | 0.24520 |
| Ca4 | 0.34470 | 0.65270 | 0.00260 |
| Ca5 | 0.34320 | 0.68050 | 0.49860 |

| | | | |
|------------|---------|---------|---------|
| V1 | 0.39800 | 0.37400 | 0.26090 |
| V2 | 0.62830 | 0.02430 | 0.23930 |
| V3 | 0.97500 | 0.60560 | 0.24300 |
| O1 | 0.30875 | 0.48181 | 0.27569 |
| O2 | 0.50712 | 0.82554 | 0.24328 |
| O3 | 0.17737 | 0.68281 | 0.22586 |
| O4 | 0.60802 | 0.47722 | 0.27687 |
| O5 | 0.52824 | 0.12569 | 0.21972 |
| O6 | 0.87626 | 0.40252 | 0.27421 |
| O7 | 0.35047 | 0.26032 | 0.05894 |
| O8 | 0.77712 | 0.08030 | 0.06906 |
| O9 | 0.90319 | 0.63997 | 0.03614 |
| O10 | 0.67024 | 0.76839 | 0.54775 |
| O11 | 0.27245 | 0.90532 | 0.55129 |
| O12 | 0.06886 | 0.29883 | 0.58013 |
| F | 0.00680 | 0.00730 | 0.24460 |

Table S6. *Ab initio* results for V-AP starting from metrically hexagonal cell in Table S4.

| | | | |
|---------------------------|---------------------------|---------------------------|----------|
| Space group | <i>P</i> -1 | | |
| $a = 9.62264 \text{ \AA}$ | $b = 9.63036 \text{ \AA}$ | $c = 6.96677 \text{ \AA}$ | |
| $\alpha = 90.507^\circ$ | $\beta = 89.253^\circ$ | $\gamma = 120.303^\circ$ | |
| $a/b = 0.9992$ | $c/b = 0.7234$ | | |
| Atom | x | y | z |
| Ca1 | 0.23765 | 0.99587 | 0.25306 |
| Ca2 | 0.00351 | 0.24451 | 0.26189 |
| Ca3 | 0.76442 | 0.76823 | 0.23846 |
| Ca4 | 0.33494 | 0.64545 | 0.00217 |
| Ca5 | 0.34095 | 0.68622 | 0.49860 |
| V1 | 0.39926 | 0.37066 | 0.26743 |
| V2 | 0.63261 | 0.02909 | 0.23595 |
| V3 | 0.97575 | 0.60757 | 0.23575 |
| O1 | 0.30631 | 0.48353 | 0.27772 |
| O2 | 0.51325 | 0.82190 | 0.24444 |
| O3 | 0.17948 | 0.68888 | 0.22890 |
| O4 | 0.60835 | 0.48095 | 0.27070 |
| O5 | 0.52748 | 0.13122 | 0.21307 |
| O6 | 0.87263 | 0.40052 | 0.26687 |
| O7 | 0.34705 | 0.26128 | 0.05912 |
| O8 | 0.77806 | 0.08245 | 0.06231 |
| O9 | 0.89473 | 0.64320 | 0.03600 |
| O10 | 0.66790 | 0.76959 | 0.55244 |
| O11 | 0.26475 | 0.90250 | 0.55249 |

| | | | |
|------------|---------|---------|---------|
| O12 | 0.06265 | 0.29382 | 0.58446 |
| F | 0.00709 | 0.00841 | 0.24574 |

Table S7. *Ab initio* results for Oxy-HAP (all atom sites are Wyckoff positions of the type 1a in space group *P1*)

| Space Group | <i>P1</i> | | |
|---------------------------|---------------------------|---------------------------|----------|
| $a = 9.35862 \text{ \AA}$ | $b = 9.35096 \text{ \AA}$ | $c = 6.86607 \text{ \AA}$ | |
| $\alpha = 90.162^\circ$ | $\beta = 89.583^\circ$ | $\gamma = 120.052^\circ$ | |
| $a/b = 1.0008$ | $c/b = 0.7343$ | | |
| Atom | <i>x</i> | <i>y</i> | <i>z</i> |
| Ca1 | 0.33643 | -0.35332 | 0.00424 |
| Ca2 | -0.33568 | 0.34440 | 0.00421 |
| Ca3 | -0.33113 | 0.32622 | -0.50586 |
| Ca4 | 0.33220 | -0.31872 | 0.49320 |
| Ca5 | 0.23047 | -0.00426 | 0.23792 |
| Ca6 | -0.26964 | 0.01118 | -0.24624 |
| Ca7 | 0.00516 | 0.22961 | 0.25978 |
| Ca8 | -0.01363 | -0.28005 | -0.26145 |
| Ca9 | -0.22780 | -0.22341 | 0.24676 |
| Ca10 | 0.27364 | 0.25878 | -0.24411 |
| P1 | 0.40713 | 0.37643 | 0.26260 |
| P2 | -0.38710 | -0.35769 | -0.25863 |
| P3 | -0.37476 | 0.02869 | 0.24547 |
| P4 | 0.35540 | -0.02776 | -0.25620 |
| P5 | -0.02886 | -0.40542 | 0.23929 |
| P6 | 0.02918 | 0.38281 | -0.23952 |
| O1 | 0.32380 | 0.48343 | 0.26972 |
| O2 | -0.32112 | -0.48035 | -0.26227 |
| O3 | -0.48698 | -0.16188 | 0.24904 |
| O4 | 0.48507 | 0.15989 | -0.25651 |
| O5 | 0.16144 | -0.32331 | 0.22752 |
| O6 | -0.15847 | 0.32130 | -0.23514 |
| O7 | -0.40139 | 0.47902 | 0.27305 |
| O8 | 0.42086 | -0.45519 | -0.27579 |
| O9 | -0.47357 | 0.12083 | 0.22803 |
| O10 | 0.44462 | -0.12738 | -0.21330 |
| O11 | -0.11718 | 0.40324 | 0.25454 |
| O12 | 0.12468 | -0.42489 | -0.26524 |
| O13 | 0.36833 | 0.28111 | 0.06622 |
| O14 | -0.34306 | -0.25631 | -0.06784 |
| O15 | -0.25184 | 0.08268 | 0.07297 |
| O16 | 0.21720 | -0.06044 | -0.10600 |

| | | | |
|------------|----------|----------|----------|
| O17 | -0.09765 | -0.36477 | 0.05497 |
| O18 | 0.09933 | 0.34634 | -0.05463 |
| O19 | -0.31013 | -0.22715 | -0.42339 |
| O20 | 0.34601 | 0.25224 | 0.43402 |
| O21 | 0.26490 | -0.09479 | -0.45161 |
| O22 | -0.27678 | 0.08930 | 0.43908 |
| O23 | 0.06727 | 0.29448 | -0.40609 |
| O24 | -0.07898 | -0.34288 | 0.42185 |
| O25 | 0.00468 | 0.00138 | 0.24145 |

Table S8. *Ab initio* results for $\text{La}_{10}(\text{GeO}_4)_6\text{O}_3$

| | | | |
|---------------------------|---------------------------|---------------------------|----------|
| Space group | <i>P</i> -1 | | |
| $a = 9.87262 \text{ \AA}$ | $b = 9.85491 \text{ \AA}$ | $c = 7.32819 \text{ \AA}$ | |
| $\alpha = 89.628^\circ$ | $\beta = 89.721^\circ$ | $\gamma = 120.405^\circ$ | |
| $a/b = 1.0018$ | $c/b = 0.7436$ | | |
| Atom | x | y | z |
| La1 | 0.21498 | 0.99029 | 0.25994 |
| La2 | 0.00786 | 0.21908 | 0.27932 |
| La3 | 0.78668 | 0.79776 | 0.23764 |
| La4 | 0.33665 | 0.64320 | 0.00013 |
| La5 | 0.33555 | 0.68324 | 0.49800 |
| Ge1 | 0.41127 | 0.38439 | 0.26094 |
| Ge2 | 0.62586 | 0.03161 | 0.23163 |
| Ge3 | 0.97573 | 0.60027 | 0.21891 |
| O1 | 0.30730 | 0.48758 | 0.27832 |
| O2 | 0.50400 | 0.82074 | 0.24199 |
| O3 | 0.18119 | 0.68583 | 0.22673 |
| O4 | 0.62138 | 0.49247 | 0.27319 |
| O5 | 0.52304 | 0.13718 | 0.21747 |
| O6 | 0.86682 | 0.39162 | 0.24810 |
| O7 | 0.37605 | 0.29064 | 0.04411 |
| O8 | 0.77228 | 0.07916 | 0.06320 |
| O9 | 0.89064 | 0.63960 | 0.02450 |
| O10 | 0.65118 | 0.76346 | 0.54891 |
| O11 | 0.26780 | 0.90147 | 0.55119 |
| O12 | 0.06681 | 0.31200 | 0.59227 |
| O13 | 0.02644 | 0.01791 | 0.16306 |
| O14 | 0 | 0 | 0.5 |

N.B Atom site O14 occupies a Wyckoff position of type 1b

Table S9. *Ab initio* results for $\text{Cd}_{10}(\text{PO}_4)_6\text{F}_2$

| Space group | <i>P</i> -1 | | |
|---------------------------|---------------------------|---------------------------|----------|
| $a = 9.33872 \text{ \AA}$ | $b = 9.32307 \text{ \AA}$ | $c = 6.69183 \text{ \AA}$ | |
| $\alpha = 90.509^\circ$ | $\beta = 88.874^\circ$ | $\gamma = 120.283^\circ$ | |
| $a/b = 1.0017$ | $c/b = 0.7178$ | | |
| Atom | <i>x</i> | <i>y</i> | <i>z</i> |
| Cd1 | 0.24021 | 0.99050 | 0.25184 |
| Cd2 | 0.00838 | 0.25379 | 0.26238 |
| Cd3 | 0.75764 | 0.76730 | 0.23626 |
| Cd4 | 0.33568 | 0.64884 | 0.00014 |
| Cd5 | 0.33921 | 0.68196 | 0.49735 |
| P1 | 0.39446 | 0.36815 | 0.25917 |
| P2 | 0.63458 | 0.02682 | 0.23517 |
| P3 | 0.97932 | 0.61293 | 0.23454 |
| O1 | 0.31723 | 0.48183 | 0.27038 |
| O2 | 0.51441 | 0.83394 | 0.24887 |
| O3 | 0.16759 | 0.68212 | 0.22793 |
| O4 | 0.58879 | 0.47175 | 0.26753 |
| O5 | 0.53695 | 0.11940 | 0.19650 |
| O6 | 0.88799 | 0.42269 | 0.27948 |
| O7 | 0.34868 | 0.26925 | 0.06078 |
| O8 | 0.77056 | 0.07104 | 0.07203 |
| O9 | 0.90293 | 0.63580 | 0.04072 |
| O10 | 0.67030 | 0.76067 | 0.56817 |
| O11 | 0.27562 | 0.90698 | 0.56316 |
| O12 | 0.05732 | 0.29263 | 0.59845 |
| F1 | 0.00818 | 0.00906 | 0.24623 |

Table S10. *Ab initio* results for $\text{Ca}_{10}(\text{CrO}_4)_6\text{F}_2$

| Space group | <i>P</i> -1 | | |
|---------------------------|---------------------------|---------------------------|----------|
| $a = 9.55250 \text{ \AA}$ | $b = 9.57319 \text{ \AA}$ | $c = 6.98317 \text{ \AA}$ | |
| $\alpha = 90.659^\circ$ | $\beta = 89.084^\circ$ | $\gamma = 120.313^\circ$ | |
| $a/b = 0.9978$ | $c/b = 0.6992$ | | |
| Atom | <i>x</i> | <i>y</i> | <i>z</i> |
| Ca1 | 0.23704 | 0.99507 | 0.25775 |
| Ca2 | 0.00429 | 0.24656 | 0.26195 |
| Ca3 | 0.76370 | 0.76922 | 0.23586 |
| Ca4 | 0.33621 | 0.64444 | 0.00113 |

| | | | |
|------------|---------|---------|---------|
| Ca5 | 0.34396 | 0.68787 | 0.50189 |
| Cr1 | 0.39942 | 0.37179 | 0.26962 |
| Cr2 | 0.63226 | 0.02777 | 0.23290 |
| Cr3 | 0.97718 | 0.60928 | 0.23445 |
| O1 | 0.30220 | 0.48046 | 0.27997 |
| O2 | 0.51705 | 0.82070 | 0.24385 |
| O3 | 0.18147 | 0.69421 | 0.22870 |
| O4 | 0.60816 | 0.48128 | 0.27128 |
| O5 | 0.52797 | 0.12989 | 0.21182 |
| O6 | 0.87329 | 0.40250 | 0.26307 |
| O7 | 0.34917 | 0.26359 | 0.06168 |
| O8 | 0.77649 | 0.08050 | 0.06001 |
| O9 | 0.89529 | 0.64457 | 0.03696 |
| O10 | 0.66269 | 0.76693 | 0.55081 |
| O11 | 0.26539 | 0.90307 | 0.55644 |
| O12 | 0.06222 | 0.29378 | 0.58624 |
| F1 | 0.00724 | 0.00931 | 0.24718 |
