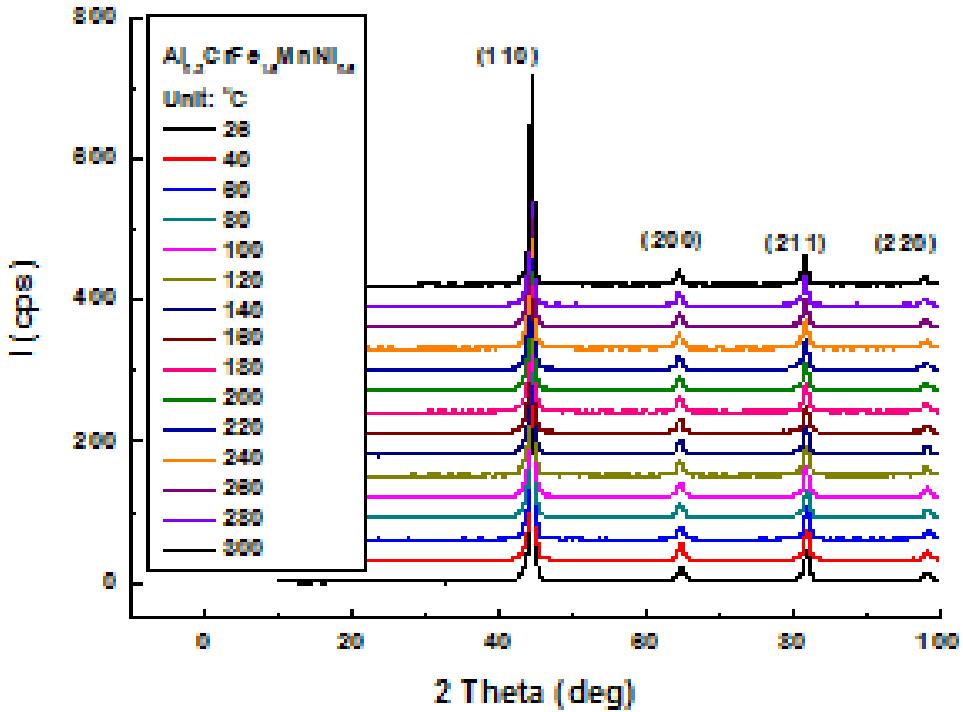


## Supplementary materials

1.



Temperature dependent XRD profiles of HEAs.

2.

Find the  $\rho(T)$  at 75°C, 150°C, and 225°C. So we have three equations:

$$\rho(348) = \rho(0) + A \left( \frac{348}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx \quad (1)$$

$$\rho(423) = \rho(0) + A \left( \frac{423}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx \quad (2)$$

$$\rho(498) = \rho(0) + A \left( \frac{498}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx \quad (3)$$

(1) - (2) and (1) - (3) to eliminate  $\rho(0)$ ,

$$\rho(348) - \rho(423) = A \left\{ \left( \frac{348}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx - \left( \frac{423}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx \right\} \quad (4)$$

$$\rho(348) - \rho(498) = A \left\{ \left( \frac{348}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx - \left( \frac{498}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx \right\}$$

(5)

(4)/(5) to eliminate A,

$$\frac{\rho(348) - \rho(423)}{\rho(348) - \rho(498)} = \frac{\left\{ \left( \frac{348}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx - \left( \frac{423}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx \right\}}{\left\{ \left( \frac{348}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx - \left( \frac{498}{\theta_D} \right)^n \int_0^{\theta_D} \frac{x^n}{(e^x - 1)(1 - e^{-x})} dx \right\}}$$

The n becomes the remaining unknown parameter.