

Supplementary Materials

Pattern analysis and interpretation of scattering from short-range order stacking in layered composite crystal $\text{Na}_x\text{CoO}_2 \cdot y\text{D}_2\text{O}$ ($x \sim 0.35$, $y \sim 1.3$)

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Table I. Probability table for $2\text{H-Na}_x\text{CoO}_2 \cdot y\text{D}_2\text{O}$ ($x \sim 0.35$, $y \sim 1.3$).

Table II. Fractional coordinates; occupancies, g ; and isotropic atomic displacement parameters, B ; for $2\text{H-Na}_x\text{CoO}_2 \cdot y\text{D}_2\text{O}$ ($x \sim 0.35$, $y \sim 1.3$).

Table I Probability table for $2\text{H-Na}_x\text{CoO}_2 \cdot y\text{D}_2\text{O}$ ($x \sim 0.35$, $y \sim 1.3$).

| | G_1 | G_2 | G_3 | G_1 | G_2 | G_3 | H_1 | H_1 | H_1 | $H_{1'}$ | $H_{1'}$ | $H_{1'}$ |
|--------------|----------|----------|----------|----------|----------|----------|-------|-------|-------|----------|----------|----------|
| tG_1 | O | O | O | O | O | O | O | O | O | E | O | O |
| tG_2 | O | O | O | O | O | O | O | O | O | O | E | O |
| tG_3 | O | O | O | O | O | O | O | O | O | O | O | E |
| tG_1 | O | O | O | O | O | O | E | O | O | O | O | O |
| tG_2 | O | O | O | O | O | O | O | E | O | O | O | O |
| tG_3 | O | O | O | O | O | O | O | O | E | O | O | O |
| tH_1 | A_{11} | A_{12} | A_{13} | O | O | O | O | O | O | O | O | O |
| tH_1 | A_{21} | A_{22} | A_{23} | O | O | O | O | O | O | O | O | O |
| tH_1 | A_{31} | A_{32} | A_{33} | O | O | O | O | O | O | O | O | O |
| ${}^tH_{1'}$ | O | O | O | A_{44} | A_{45} | A_{46} | O | O | O | O | O | O |
| ${}^tH_{1'}$ | O | O | O | A_{54} | A_{55} | A_{56} | O | O | O | O | O | O |
| ${}^tH_{1'}$ | O | O | O | A_{64} | A_{65} | A_{66} | O | O | O | O | O | O |

Note 1: Arrays, E , O , A_{st} , G_q , tG_q , H_r , and tH_r , are defined as follows,

$$E \equiv \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}, \quad O \equiv \begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}, \quad A_{st} \equiv \begin{pmatrix} 0 & \alpha_{st} & \alpha_{st} & \alpha_{st} \\ \alpha_{st} & 0 & \alpha_{st} & \alpha_{st} \\ \alpha_{st} & \alpha_{st} & 0 & \alpha_{st} \\ \alpha_{st} & \alpha_{st} & \alpha_{st} & 0 \end{pmatrix}, \quad G_q \equiv \begin{pmatrix} G_{1q} \\ G_{2q} \\ G_{3q} \\ G_{4q} \end{pmatrix}, \quad H_r \equiv (H_r \quad H_r \quad H_r \quad H_r), \quad \text{and } {}^tH_r \equiv \begin{pmatrix} H_r \\ H_r \\ H_r \\ H_r \end{pmatrix}.$$

Note 2: When the structure is analyzed on the assumption that all A_{st} are equal to each other, or all α_{st} 's are equal to $1/9$, the commensurate model does not significantly improve the fitting results. When $A_{s3} = A_{s5} = O$, i.e. $\alpha_{s3} = \alpha_{s5} = 0$, the R factors are lowered to $R_p = 4.0\%$ and $R_{wp} = 5.8\%$ with the values from $\alpha_{s1} = \alpha_{s4} = 0.220$, $\alpha_{s2} = \alpha_{s6} = 0.113$ to $\alpha_{s1} = \alpha_{s4} = 0.141$, $\alpha_{s2} = \alpha_{s6} = 0.192$. As dependency of the R factors on the values of α_{s1} , α_{s2} , α_{s4} , α_{s6} is weak and it is difficult to know the optimum values for α_{st} , $\alpha_{s1} = \alpha_{s2} = \alpha_{s4} = \alpha_{s6} = 1/6$ and $\alpha_{s3} = \alpha_{s5} = 0$ have been selected as a typical value set of α_{st} to obtain a satisfactory convergence.

Table II Fractional coordinates; occupancies, g ; and isotropic atomic displacement parameters, B ; for $2\text{H-Na}_x\text{CoO}_2 \cdot y\text{D}_2\text{O}$ ($x \sim 0.35$, $y \sim 1.3$).

| Host part | x | y | z | g | B (\AA^2) |
|------------|-----------|------------|------------------|--------------------|------------------------|
| Co1 | 0 | 0 | 0 | 1 | 0.735(4) |
| Co2 | 1/2 | 0 | 0 | 1 | = $B(\text{Co1})$ |
| O1 | 2/3 | 1/3 | -0.2328(5) | 1 | = $B(\text{Co1})$ |
| O2 | 0.1672(7) | -0.1672 | -0.1942(2) | 1 | = $B(\text{Co1})$ |
| Guest part | x | y | z | g | B (\AA^2) |
| Na1 | 0 | 0 | 0 | 1 ^a | = $B(\text{Co1})$ |
| Na2 | 1/3 | 2/3 | 0.1596(12) | 0.192 ^a | = $B(\text{Co1})$ |
| O3 | 0.6840(6) | 0.6662(8) | 0.2808(6) | 0.857(1) | = $B(\text{Co1})$ |
| D1 | 0.7352(6) | 0.6876(11) | 0.4747(5) | = $g(\text{O3})$ | 5.73(3) |
| D2 | 0.4934(5) | 0.5496(6) | 0.2712(7) | = $g(\text{O3})$ | = $B(\text{D1})$ |
| O4 | 2/3 | 1/3 | 0.3798(10) | 0.146(3) | = $B(\text{Co1})$ |
| D3 | 0.41(3) | 0.299(2) | = $z(\text{O4})$ | = $g(\text{O4})$ | = $B(\text{D1})$ |

$a = 5.6418(2)$ \AA , $c = 4.9029(3)$ \AA , and $\gamma = 120^\circ$. Local symmetry: x, y, z ; $-y, x-y, z$; $y-x, -x, z$; $-x, -y, -z$; $y, y-x, -z$; $x-y, x, -z$. ^a Na content was fixed to the analytical value.

Reference

Takada K., Onoda M., Argyriou D.N., Choi Y.-N., Izumi F., Sakurai H., Takayama-Muromachi E. and Sasaki T. (2009). *Chem. Mater.* **21**, 3693-3700.